

Arunima Singh Thakur, 180905218, Sec. C
Roll no. 31, Branch CSE, EEFM midsem,
Amr

3) ~~Initial cost = \$30000~~

~~Annual benefit =~~

The rate of return ~~i~~ is found from assuming the net present worth of cash flow is zero

NPW = present value of benefits - present value of costs

$$PV = F * (P/F, i, n) - A * (P/A, i, n)$$

net annual benefit = A = annual benefit - annual cost

$$= 27000 - 18000$$

$$= 9000$$

$$\Rightarrow 0 = -30000 + 9000 * (P/A, i, 5) + 4000 * (P/F, i, 5)$$

Suppose

$$i = 10\%$$

$$\text{then } NPW = -30000 + 9000 * 3.791 + 0.6209 * 4000$$

$$= 6602.6$$

and

if $i = 15\%$ then

$$NPW = -30000 + 9000 * 3.352 + 0.4972 * 4000$$

$$= 2156.8$$

By interpolation

$$i - 0.1 = ((0.15 - 0.1) * (0 - 6602.6)) / (2156.8 - 6602.6)$$

$$i = 17.43$$

The internal rate of return is 17.43%. - Ans

~~4) Tool B should not be considered further since its IRR < 8%.~~

~~$$PWA = -\$55,000 + (\$18,250 - \$6,250) (P/A, 8\%, 7) + \$18,000 (P/F, 8\%, 7) = \$17,980$$~~

~~$$PWC = -\$80,000 + (\$20,200 - \$3,200) (P/A, 8\%, 7) + \$22,000 (P/F, 8\%, 7) = \$21,346$$~~

~~Therefore select Tool C - Ans~~

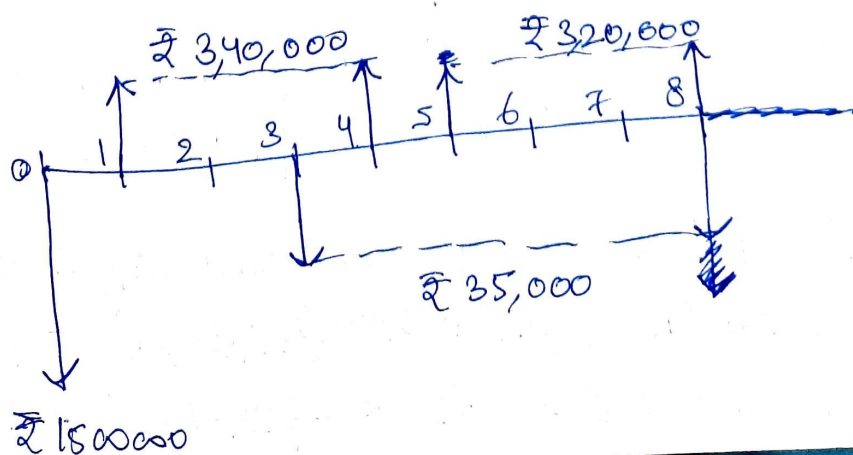
~~10) As per IRR method select D3.~~

~~Only D3 has an IRR as there is a sign change in the cash flow.~~

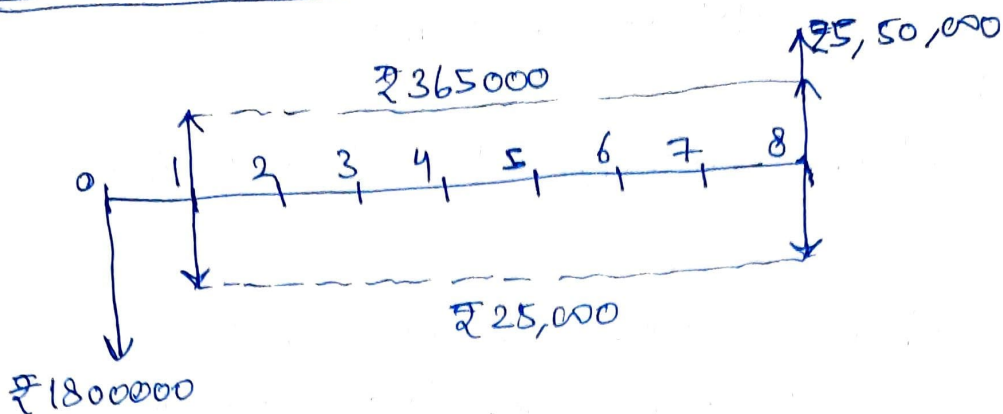
~~There are situations where there is no IRR.~~

1) Alternative 1:

$$[i = 9\%]$$



Alternative 2:



$$\begin{aligned} NPW_1 &= -1500000 + 340000 (P/A, 9\%, 4) \\ &\quad + 320000 (P/A, 9\%, 4) (P/F, 9\%, 4) \\ &\quad - 35000 (P/A, 9\%, 6) (P/F, 9\%, 2) \\ &= 203786.74 \end{aligned}$$

$$\begin{aligned} NPW_2 &= -1800000 - 25000 (P/A, 9\%, 8) + \\ &\quad 365000 (P/A, 9\%, 8) + 550000 (P/F, 9\%, 8) \\ &= 357864.95 \end{aligned}$$

$$\therefore NPW_2 > NPW_1$$

\therefore Alternative 2 is more economical - Ans

$$\begin{aligned} \text{PW of Tool A} &= -55000 - 6250 (P/A, 8\%, 7) \\ &\quad + 18250 (P/A, 8\%, 7) + 18000 (P/F, 8\%, 7) \\ &= \$17979.27 \end{aligned}$$

$$\begin{aligned} AW \text{ of Tool A} &= 8\% * \$17979.27 / (1 - (1+8\%)^{-7}) \\ &= \$3453.32 \end{aligned}$$

$$\begin{aligned} PW \text{ of Tool B} &= -45000 - 8550 (P/A, 8\%, 7) + \\ &\quad 16750 (P/A, 8\%, 7) + 3750 (P/F, 8\%, 7) = -\$119.87 \end{aligned}$$

$$AW \text{ of Tool B} = 8\% * -\$119.87 / (1 - (1+8\%)^{-7})$$

$$= -\$22.99$$

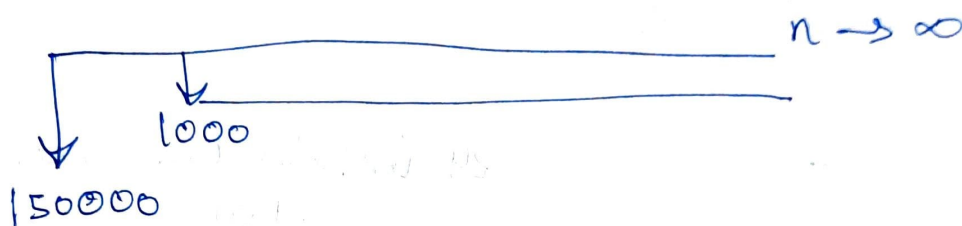
$$\begin{aligned} \text{PW of Tool C} &= -80000 - 3200(P/A, 8\%, 7) + \\ & 20200(P/A, 8\%, 7) + 22000(P/F, 8\%, 7) \\ &= \$21,345.07 \end{aligned}$$

$$\begin{aligned} \text{AW of Tool C} &= 8\% * \$21,345.07 / (1 - (1 + 8\%)^{-7}) \\ &= \$4099.80 \end{aligned}$$

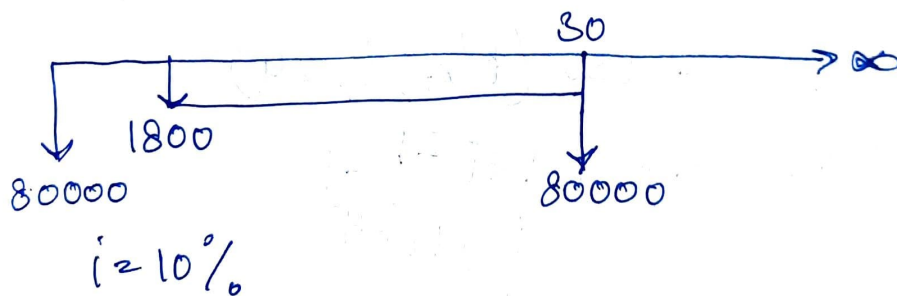
Since PW and AW of Tool C is the highest, therefore Tool C should be chosen.

~~# Present value~~

5) A:



B:



A:

Recurring

1000

Non Recurring

150000

$$\begin{aligned} \text{Capitalized cost} &= \frac{1000}{i} + \underline{150000} \\ &= \frac{1000}{0.1} + 150000 \\ &= 160000 \end{aligned}$$

B: -

$$80000 + \frac{80000(A/F, 10\%, 30)}{i} + \frac{1800}{i}$$
$$= 80000 + \frac{80000(0.00608)}{0.1} + \frac{1800}{0.1}$$
$$= 102864 = CC$$

$$CC = \frac{A}{i}$$

∴ - this is cost dominated

Ans: - Canal B will be built as it has the capitalized cost of B is lower than that of A.

2) $P = \$3000$ 24 installments monthly
 $= \$150$
 $\Rightarrow 24 \times 150 = 3600$

$$3000 = 150 (P/A, i, 24)$$

$$\Rightarrow \cancel{3000}^{20} = \cancel{150} \frac{(1+i)^{24} - 1}{i(1+i)^{24}}$$

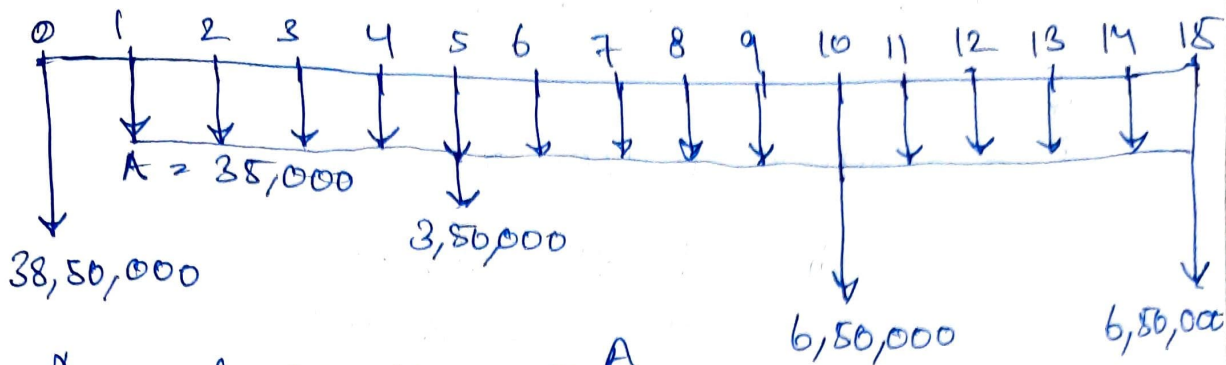
$$\Rightarrow 20 = \frac{(1+i)^{24} - 1}{i(1+i)^{24}}$$

$$\Rightarrow i = 0.0151308$$
$$= 1.51308\% \text{ per month}$$

$$\text{ieff per quarter} = (1+i)^3 - 1$$
$$= (1.0151308)^3 - 1$$
$$= 0.04608$$
$$= 4.608\%$$

7) $n = 15 \text{ years}$, $i = 10\%$

Alternative 1:



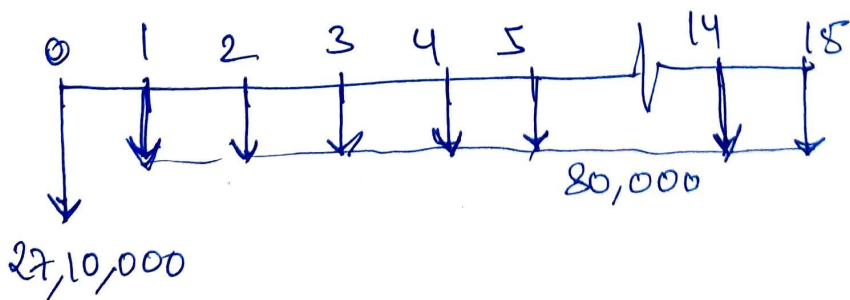
$$\text{Annual Worth} = \frac{A}{35000} + CR$$

$$\begin{aligned} CR &= \left[38,50,000 + 350000 \times (P/F, 10\%, 5) + \right. \\ &\quad \left. 6,50,000 \times (P/F, 10\%, 10) \right] \times (A/P, 10\%, 15) + \\ &\quad 6,50,000 \times (A/F, 10\%, 15) \\ &= \left[38,50,000 + 3,50,000 \times 0.6209 + \right. \\ &\quad \left. 6,50,000 \times 0.3855 \right] \times (0.1315) + \\ &\quad 6,50,000 (0.0315) \end{aligned}$$

$$= ₹ 5,88,277.53$$

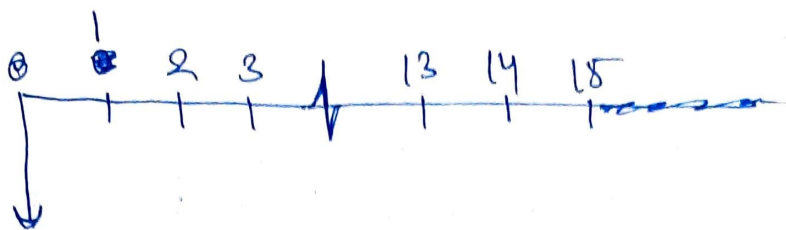
$$\therefore \text{Annual worth} = ₹ 62,3277.53$$

Alternative 2:



$$\begin{aligned} \text{Annual worth} &= 80,000 + 2710000 \underbrace{(A/P, 10\%, 15)}_{0.1315} \\ &= ₹ 4,36,365 \end{aligned}$$

Alternative 3:-



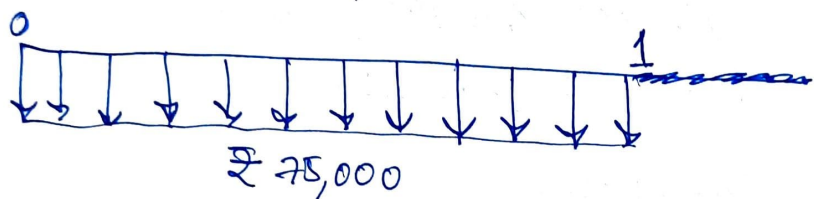
$$P = 3800,000 + 430,000$$

$$\begin{aligned}\text{Annual worth} &= P(A/P, 10\%, 15) \\ &= 4230000 \times 0.1315 \\ &= ₹ 5,56,245\end{aligned}$$

Ans.:- Alternative 2 is the best alternative.

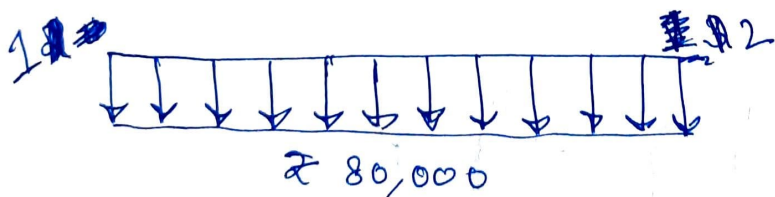
8) $i = 18\%$ compounded monthly.

Year 1:-



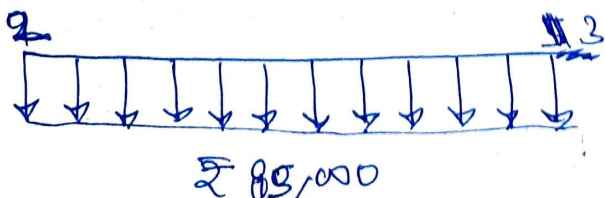
$$PW_1 = 75000 + 75000(P/A, i_1, 11)$$

Year 2:-



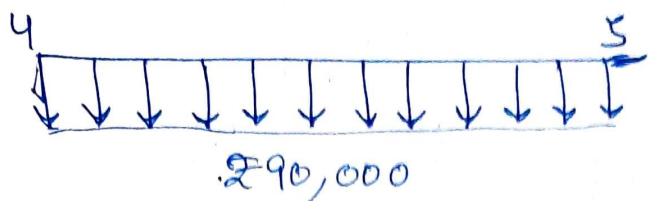
$$PW_2 = (80,000 + 80,000(P/A, i_1, 11))(P/F, i_2, 1)$$

Year 3:-



$$PW_3 = (85000 + 85000(P/A, i_1, 11))(P/F, i_2, 2)$$

Year 4:



₹90,000

$$PW_4 = [90,000 + 90,000(P/A, i_1, 11)](P/F, i_2, 3)$$

$$i_1 = \left(1 + \frac{r}{n}\right)^n - 1 = \left(1 + \frac{.18}{12}\right)^1 - 1 = 1.5\%$$

$$i_2 = \left(1 + \frac{.18}{12}\right)^{12} - 1 = 19.56\%$$

$$\therefore P/A, i_1, 11) = 10.071$$

$$\Rightarrow PW_1 = 75000 + 755,333.83 = 830,333.83$$

$$\begin{aligned} \Rightarrow PW_2 &= 885680(P/F, 19.56, 1) \\ &= 740,782.87 \end{aligned}$$

$$\begin{aligned} \Rightarrow PW_3 &= 941,035(P/F, 19.56, 2) \\ &= 658,315.32 \end{aligned}$$

$$\begin{aligned} \Rightarrow PW_4 &= 996,390(P/F, 19.56, 3) \\ &= 583,004.14 \end{aligned}$$

$$\begin{aligned} PW &= PW_1 + PW_2 + PW_3 + PW_4 \\ &= 2,812,436.16 \end{aligned}$$

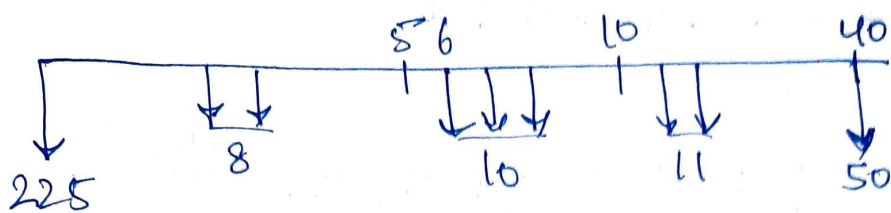
$$\Rightarrow 2812436.16 = 3200000 - S(P/F, i_2, 4)$$

$$\frac{S}{(1.1956)^4} = 387563.84$$

$$\boxed{S = 791,930.14}$$

Minimum salvage value required for making warehouse.

b) $i = 10\%$ Infinite lives
 (All costs in million \$)



a)

Non-recurring cost = 225

Recurring cost = $\frac{A}{i}$

$$\Rightarrow \frac{8}{i} + \frac{2}{i} \left(\frac{1}{1+i} \right)^5 + \frac{1}{i} \left(\frac{1}{1+i} \right)^{10} + \frac{50 \left(\frac{1}{(1+i)^{40}} - 1 \right)}{i}$$

$$\Rightarrow 80 + 12.42 + 3.86 + 1.13$$

$$\Rightarrow 97.41$$

$$C.C = 225 + 97.41 = 322.41 \text{ (million \$)}$$

b) Non-recurring cost = 350

Recurring cost = $\frac{A}{i}$

$$\frac{0.8}{i} + \frac{0.1}{i} \left(\frac{1}{(1+i)^9} \right) = 8 + 0.92 = 8.92$$

$$C.C = 350 + 8.92 = 358.92 \text{ (million \$)}$$

\therefore - A cost is less

Ans:- Steel Conduit (a) is better

10) 1500 hours / yr.

study period of useful life = 5 yrs

MARR = 20%

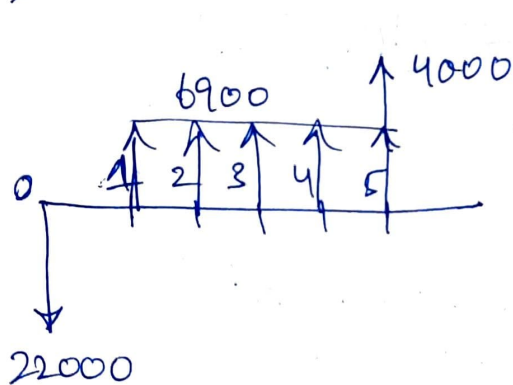
• Arranging in ascending order of investment:

D1, D4, D2, D3

Company D1 & D4

	D1	D4	D4 - D1
Invest	100000	122000	22,000
Annual exp.	29000	22100	-6900
Market val.	10000	14000	4000

⇒ CFD — Cost dominated



$$\therefore PW = -22000 + 6900(P/A, i, 5) + 4000(P/F, i, 5)$$

$$NPW = 0$$

$$PW(5\%) = +11004.1$$

$$PW(30\%) = -4114.4$$

$$PW(20\%) = 245.5$$

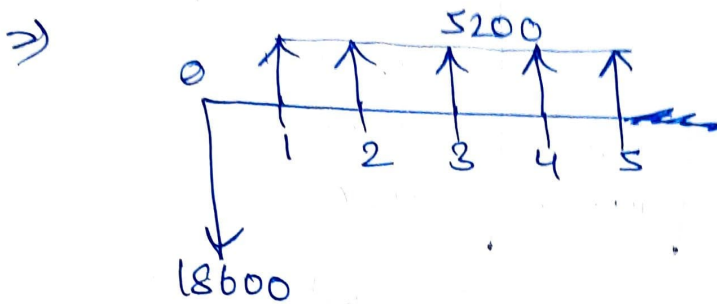
$$\text{Req } i = 20\% + \frac{245.5 + 0}{245.5 - (-4114.4)} \times (10\%)$$

$$\Rightarrow i = 20.56\% > \text{MARR}$$

∴ D4 accepted

Comparing D4 & ~~D1~~ D2

	D4	D2	D2 - D4
invest	122000	140600	18600
exp.	22100	16900	-5200
market val.	14000	14000	0



$$\therefore - PW = -18600 + 5200 (P/A, i, 5)$$

$$PW(10\%) = 1113.2$$

$$PW(15\%) = -1169.6$$

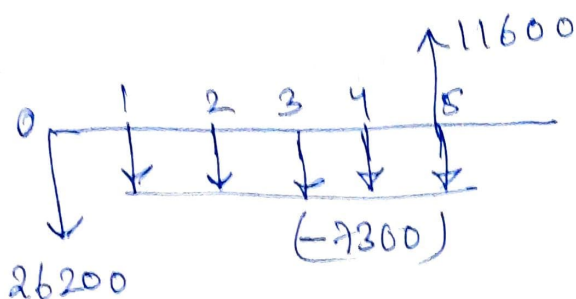
$$\therefore - \text{reqd } i = 10\% + \frac{1113.2 + 0 \times (5\%)}{1113.2 + 1169.6}$$

$$\Rightarrow i = 12.43\% < \text{MARR}$$

∴ D2 not chosen, D4 chosen

Comparing D4 & D3

	D3 - D4
invest	26200
exp.	-7300
market val.	11600



$$\therefore PW = -26200 + 7300(P/A, i, 5) + 11600(P/F, i, 5)$$

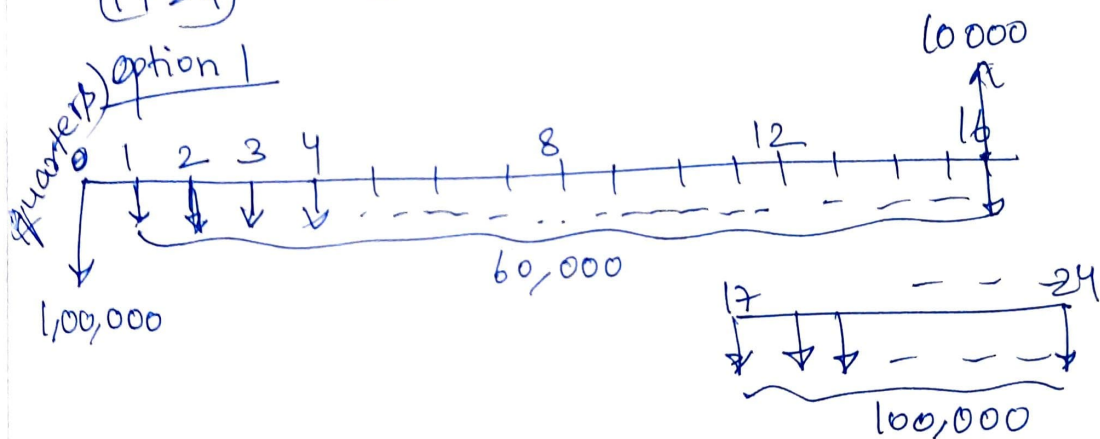
$$PW(20\%) = 296.34$$

$$PW(25\%) = -2768.98$$

By interpolation, we get $i = 20.4\% > MARR$

\therefore D3 chosen \Rightarrow D3 is best choice

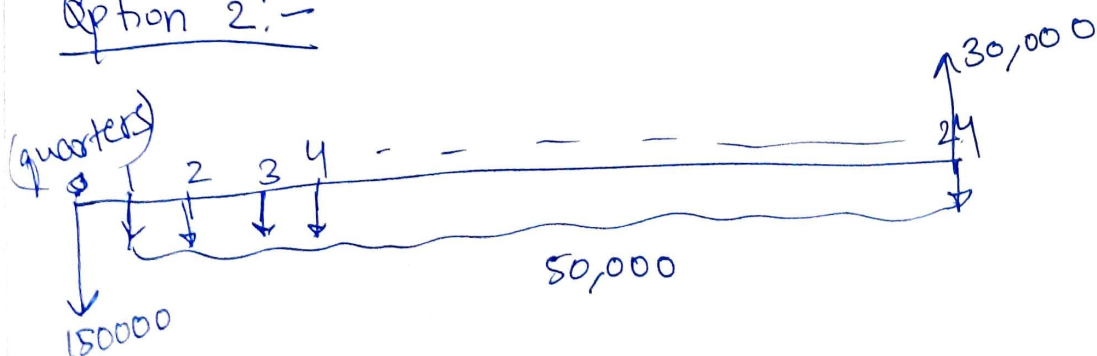
9) $i_{eff} = \left(1 + \frac{0.12}{4}\right)^{4/4} - 1 = 12\%$
(PP=4)



$$PW = 100000 + 60000(P/A, 3, 16) - 10000(P/F, 3, 16) + 100000(P/A, 3, 8)(P/F, 3, 16)$$

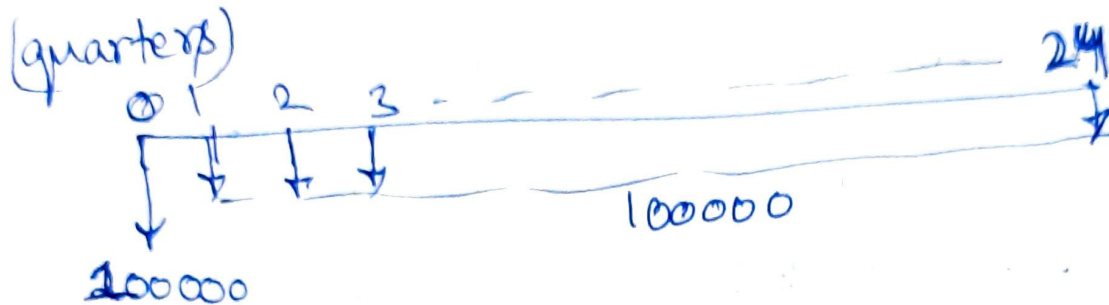
$$= 1284901.704$$

Option 2:-



$$\begin{aligned}
 PW &= 150000 + 30000 (P/A, 3, 24) - 30000 (P/F, 3, 24) \\
 &= \$98,20,18
 \end{aligned}$$

Option 3



$$\begin{aligned}
 PW &= 100000 (P/A, 3, 24) + 100000 \\
 &= \$1793550
 \end{aligned}$$

Conclusion:- Based on cost dominated CFD approach:- Option 2 has min value of PW and hence must be chosen.