Reg No.:_______ Name: 02000M A T 206052101

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

Fourth Semester B. Tech Degree Examination July 2021 (2019 Scheme

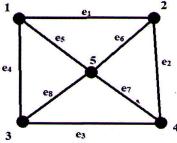
deposit A

Course Code: MAT206 Course Name: GRAPH THEORY

Max. Marks: 100 Duration: 3 Hours

PART A

	(Answer all questions; each question carries 3 marks)	Marks
1	What is the maximum number of edges in a simple graph with n vertices?	3
	Justify your answer.	
2	There are 25 telephones in Metropolis. Is it possible to connect them with wires	3
	so that each telephone is connected with exactly 7 others? Why?	
3	Show that all vertices of an Euler graph G are of even degree	3
4	Explain strongly connected and weakly connected graphs with the help of	3
	examples.	
5	Prove that a connected graph G with n vertices and n-1 edges is a tree.	3
6	How many labelled trees are there with n vertices? Draw all labelled trees with	3
	3 vertices.	
7	Define planar graphs. Is K ₄ , the complete graph with 4 vertices, a planar graph?	3
	Justify.	
8	Define fundamental circuits and fundamental cut-sets.	3
9	Construct the adjacency matrix and incidence matrix of the graph.	3



Define chromatic number. What is the chromatic number of a tree with two or more vertices?

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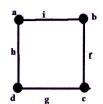
PART B

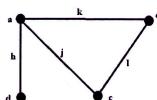
(Answer one full question from each module, each question carries 14 marks) Module -1

- 11 a) Define complete graph and complete bipartite graph. Draw a graph which is a complete graph as well as a complete bipartite graph.
 - b) Explain walks, paths and circuits with the help of examples.
- 12 a) Define isolated vertex, pendant vertex, even vertex and odd vertex. Draw a graph that contains all the above.
 - b) Prove that simple graph with n vertices and k components can have at most 7 (n-k)(n-k+1)/2 edges.

Module -2

13 a)





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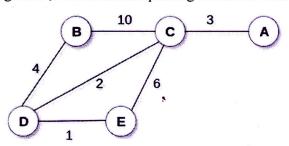
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Find the union, intersection and ring sum of the above graphs.

- b) State travelling salesman problem. How it is related to Hamiltonian circuits?
- 14 a) Prove that in a complete graph with n vertices there are (n-1)/2 edge disjoint 7 Hamiltonian circuits, if n is an odd number and $n \ge 3$.
 - b) For which values of m, n is the complete graph $K_{m,n}$ an Euler graph? Justify your answer.

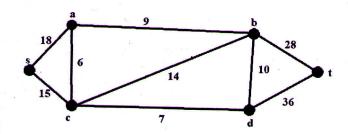
Module -3

- 15 a) Prove that a binary tree with n vertices has (n+1)/2 pendant vertices.
 - b) Using Prims algorithm, find a minimal spanning tree for the following graph.



16 a) Write down Dijkstra's algorithm and use it to find the shortest path from s to t.

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b) Prove that every tree has either one or two centers.

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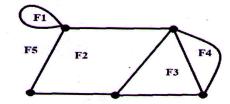
Module -4

- 17 a) Define cut-set. Prove that every circuit in G has an even number of edges in common with any cut-set.
 - b) Construct the geometric dual of the graph below

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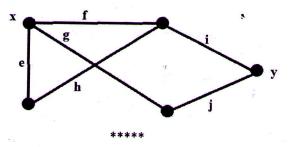
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- 18 a) Prove that a connected planar graph with n vertices and e edges has e-n+2 regions.
 - b) Let G be a connected graph and e an edge of G. Show that e is a cut-edge if and only if e belongs to every spanning tree.

Module -5

- 19 a) Explain four colour problem using the concept of chromatic number.
 - b) Let B and A be the circuit matrix and the incidence matrix of a graph G which is free from loops, whose columns are arranged using the same order of edges. Show that AB^T=BA^T=0 (mod 2).
- 20 a) Show that chromatic polynomial of a tree with n vertices is $P_n(\lambda) = 7$ $\lambda(\lambda 1)^{n-1}$
 - b) Define path matrix of a graph. Find the path matrix P(x, y) for the graph below. 7



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