

Home work

M/M/1:2

$$\lambda = 8/hk$$

$$\mu = 9/hk$$

$$N = 2$$

$$P_0 = \frac{1-P}{1-P^{N+1}}$$

$$P = \lambda/\mu$$

$$= \frac{1-8/9}{1-(8/9)^3} = \frac{1-0.888}{1-(0.888)^3}$$

$$= \frac{0.1112}{0.297} = \underline{\underline{0.3732}}$$

$$P_1 = P P_0 = 8/9 \times 0.3732 = \underline{\underline{0.3317}}$$

$$\begin{aligned} P_2 &= P^2 P_0 = (0.888)^2 \times 0.3732 \\ &= 0.7899 \times 0.3732 \\ &= 0.2948 \end{aligned}$$

Probability of joining the system
 $= 1 - 0.2948 = 0.7052$

effective arrival rate

$$\begin{aligned}\lambda_e &= \lambda \times 0.7052 \\ &= 8 \times 0.7052 \\ &= 5.646\end{aligned}$$

Load of system

$$L_s = \frac{\rho [1 + N\rho^{(N+1)} - (N+1)\rho^N]}{(1-\rho)(1-\rho^{N+1})}$$

$$= \frac{0.8888(1 + 2 \times (0.8888)^3 - 3 \times (0.8888)^2)}{(1-0.8888)(1-0.8888^3)}$$

$$= \frac{0.8888(1 + 1.404 - 2.3656)}{0.112 \times 0.2978}$$

$$= \frac{0.8888 \times 0.0384}{0.0331}$$

$$= 1.019 //$$

$$W_s = \frac{L_s}{\lambda_e}$$

$$= \frac{1.019}{5.641} = \underline{\underline{0.1806}}$$