

# A STUDY OF RELIGIONS

## CS785A - Multi Agent Systems

---

Aashi Manglik (13006), M Arunothia (13378), Rachita Chhaparia (13525)

April 14, 2017

Indian Institute of Technology Kanpur

- Model inter-religion interaction
- Interaction as co-operation and defect

# ITERATED PRISONER'S DILEMMA

	C	D
C	d,d	c,b
D	b,c	a,a

**Figure:** Prisoner's dilemma payoff matrix

- $b > d > a > c$
- Widely used to model co-operation in society
- Game played repeatedly to capture evolution of co-operation

Religion: My actions will have repercussions

- $q_c$  : probability of being punished for co-operating
- $q_d$ : probability of being punished for defecting

Taken as Gaussian Distributions

- Following the strategic interaction, each individual believes he will receive, in addition to the payoff of the PD game, either a negative utility shock,  $-\epsilon$ , or a positive utility shock,  $\epsilon$ .

- What one religious organization expects from the opponent religious organization
- $b_i$  : probability that the opponent will co-operate
- $b_i$  modified after every iteration of game: increased by  $\alpha$  if opponent co-operated, decreased by  $\alpha$  if opponent defected

	C	D
C	$d + \epsilon(1 - 2q_c), d + \epsilon(1 - 2q_{c'})$	$c + \epsilon(1 - 2q_c), b + \epsilon(1 - 2q_{d'})$
D	$b + \epsilon(1 - 2q_d), c + \epsilon(1 - 2q_{c'})$	$a + \epsilon(1 - 2q_d), a + \epsilon(1 - 2q_{d'})$

- $q_i \leq \frac{c-b}{2\epsilon}$  : always co-operate
- $q_i \geq \frac{d-a}{2\epsilon}$  : always defect

- Payoff expected for co-operating

$$\pi_c = b_i * (d + \epsilon(1 - 2 * q_c)) + (1 - b_i) * (c + \epsilon(1 - 2 * q_c))$$

- Payoff expected for defected

$$\pi_d = b_i * (b + \epsilon(1 - 2 * q_d)) + (1 - b_i) * (a + \epsilon(1 - 2 * q_d))$$

- Agent plays co-operate if  $\pi_c \geq \pi_d$  and defect otherwise



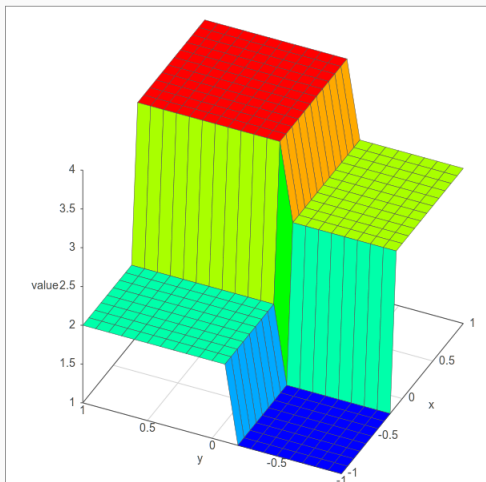
- $b_i$  is initialized keeping in mind the dynamics of the religions involved
- $q_c, q_d$  is set keeping in mind the doctrines of the religion
- $\epsilon$  is set keeping in mind the intensity of reward/punishment aspect of religion

We consider the dynamics between two religions: Hinduism, Islam. Parameter values for these and their justification is as follows:

- $b_H = 0.3$
- $b_I = 0.5$
- $\epsilon_H = 5$
- $\epsilon_I = 7$
- Muslims consider Hindus to be more cooperative than the reverse.
- Utility shock of Islam is higher relative to Hinduism.

## GAME SIMULATIONS: GRAPH

$\alpha$  is set to 0.02



**Figure:** Graph showing the dependence of strategy on  $q_c$  and  $q_d$

$$q_i = q_c - q_d$$

- High negative  $q_i \rightarrow$  tendency to co-operate increases  
Belief that co-operation is highly rewarded and defection is penalized
- High positive  $q_i \rightarrow$  tendency to defect increases  
Belief that co-operation is penalized and defection is rewarded
- On increasing  $\epsilon \rightarrow$  tendency to co-operate increases with lesser negative value of  $q_i$

- Every node is a religious agent.
- Number of nodes correspond to the geographic population of the religion they represent.
- An edge occurs between 2 religious agents if they are neighbours geographically and also if they seem to show interactions in the real world.

- Every agent plays against the nearest  $k$  neighbours of the opposite religion. Hence, pay-off for an agent is the sum of pay-offs received in each of these individual interactions.
- The strategy used by an agent remains same across all the players he plays.
- An agent updates his strategy by looking at how successful his peers have been in adopting an alternative strategy.

# UTTAR PRADESH RELIGION CENSUS 2011

- Considered 9 districts in Uttar Pradesh and the percentage of Hindu and Muslim population in each.

District	Node ratio (Hindu: Muslim)
Baghpat	7:3
Meerut	6:4
Muzzafarnagar	6:4
Ghaziabad	7:3
Aligarh	8:2
Mathura	9:1
Agra	9:1
Rampur	5:5
Bareilly	6:4

- Every region was represented by 10 religious agents with (Hindus : Muslims) ratio accounting for the population of these two religions in that region.
- Interaction between different religious agents is not explicitly available to us via any data. Hence, to complete this information we made logical assumptions.
- We measure the harmony of a region by measuring the inverse count of the number of Defect – Defect links in that region.



The following results were obtained for the data considered.

- Amongst the neighbouring districts - Baghpat, Meerut, Muzzafarnagar and Gaziabad, we detected Muzzafarnagar to be the least harmonious district (with a high frequency). This in some sense models the scenario in the real world.

Thank you!