

Q5)

a)  $\lceil \log_{100} 10,000,000 \rceil = \lceil 3.5 \rceil = 4$  max depth

$\lceil \log_{200} 10,000,000 \rceil = \lceil 3.04 \rceil = 4$  min depth

b. & c) In the worst case, we assume all nodes are half full.

records	reads	writes	total (b)	total (c)
1-100	1	1	$2 * 100$	0
101-10,000	2	2	$4 * (10,000 - 100)$	0
10,001 - 1,000,000	3	3	$6 * (1 \text{ million} - 10k)$	$2 * (1 \text{ million} - 10k)$
1,000,001 - 10,000,000	4	4	$8 * (9 \text{ million})$	$4 * 9 \text{ million}$
Total			77,979,800	37,980,000

In Part (c), we also need to write the first two layers of the index on disk at the end. That will add additional 101 I/Os.

d) Assuming the data is sorted, the index can be constructed in a way that we fill the nodes fully from left to right, keeping the index frontier in memory, and when a node is written, we won't touch it again. The # of I/Os will be the size of the index.

Index size =  $\lceil 10,000,000 / 200 \rceil + \lceil 50,000 / 200 \rceil + \lceil 250 / 200 \rceil + 1$