

# Computing Science (CMPUT) 325

## Nonprocedural Programming

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# Introduction to Prolog

- Prolog syntax is based on predicate calculus
- Examples of predicates:
  - `likes(mary, john)`
  - `greater(3, 2)`
  - `isPrime(19)`

# Atoms in Predicate Calculus

- Atom, or atomic formula:
- $p(t_1, \dots, t_n)$
- $p$  is a **predicate symbol** (e.g. `likes`, `isPrime`)
- $t_i$  are called **terms** (a bit similar to symbolic expressions in Lisp)
- Terms can **only** be used as arguments in predicates

# Terms

- A constant is a term (in Prolog: starts with lowercase letter)
  - Numbers are represented in Prolog as usual
- A variable is a term (in Prolog: starts with uppercase letter)
- Functions are terms, defined recursively:
- if  $s_1, \dots, s_k$  are terms, and  $f$  is an  $k$ -ary function symbol, then  $f(s_1, \dots, s_k)$  is a term

## More Details

- Functions and predicates in Prolog also start with lowercase letter
- Only variables start with uppercase
- Examples of predicates with variables:
  - `append(X, Y, Z)`
  - `p(X, f(Y), g(Z))`
- Note that in Prolog, the role of functions is **very** different
- Function symbols are mostly used to structure data, not used for computation
- We compute by doing inference with predicates

# Binding Variables

- As in Lisp, variables can be *bound* to values
- The mechanisms for doing the binding are different
- The simplest one uses `=`, as in `x = 2`
- There are other ways to bind variables using unification, see later

# Prolog Program

- A Prolog program is a collection of **clauses**
- A clause is either a **fact** or a **rule**
- Example of a fact:
  - `father(ken, mary) .`
- Example of a rule:
  - `parent(X, Y) :- father(X, Y) .`
- A Prolog program usually contains both rules and facts.
- Both rules and facts always end with a dot.
- If you forget it, Prolog will sit and wait for it (or give a syntax error).

## More About Facts

- A fact is also called an unconditional clause.
- A fact like `father(ken, mary) .` means that this predicate is unconditionally true within the current program.
- Facts and rules can also contain variables. Those are always **universally quantified**.
- Example: `awesome(X) .` in Prolog means:
  - In logic:  $\forall X \text{ awesome}(X)$
  - In words: “everything is awesome”



## More About Rules

- `parent(X,Y) :- father(X,Y) .`
- The `:-` symbol can be read as “if”
- Rules are **conditional** clauses
- The **head** of the clause is `parent(X,Y)`
- It is true under the condition that the **body** `father(X,Y)` is true
- It may be true in other cases as well,  
if there are more clauses with `parent` as head

## Rules with Multiple Predicates in the Body; Multiple Rules

- The body can have a list of atoms
- All of them must be true to imply that the head is true
- `banana(X) :- yellow(X), fruit(X), bendy(X) .`
- This rule means that all yellow bendy fruits are bananas.
- It does **NOT** mean that all bananas must be yellow bendy fruits.
- We can add more rules such as
- `banana(X) :- green(X), vegetable(X), notBent(X) .`

## Rules and Logical Consequence

- `parent(X,Y) :- father(X,Y) .`
- X is a parent of Y **if** X is a father of Y
- `parent(X,Y)` is true whenever `father(X,Y)` is true
- `father(X,Y)` implies `parent(X,Y)`
- In logic:  $\forall X \forall Y \text{ father}(X,Y) \rightarrow \text{parent}(X,Y)$
- In words: for all X and all Y: if X is a father of Y, then X is a parent of Y

# General Form of Prolog Rules

- $A :- B_1, B_2, \dots, B_n.$
- $A$  and all  $B_i$  are atoms
- $A$  is the head of the clause
- The list of  $B_i$ 's is the body
- In logic:  $(B_1 \wedge B_2 \wedge \dots \wedge B_n) \rightarrow A$
- In words: whenever all  $B_i$  are true,  $A$  is also true
- As before, universally quantified over all variables in the clause (see next slide)

# Universal Quantifiers for Prolog Rules

- Given a rule  $A :- B_1, B_2, \dots, B_n.$
- Assume  $x_1, \dots, x_m$  are all the variables appearing anywhere within the rule
- In logic, this is same as having universal quantifiers for all the  $x_i$ :
- $\forall x_1 \forall x_2 \dots \forall x_m$   
 $(B_1 \wedge B_2 \wedge \dots \wedge B_n) \rightarrow A$

# Facts as Special Cases of Rules

- Fact  $A$ .
- Rule  $A \text{ :- } B_1, B_2, \dots, B_n$ .
- We can view a fact as a special case of a rule with zero atoms in the body
- We could also write the fact as  $A \text{ :- true}$ . but it just adds clutter.
- “If true then  $A$ ” is just a cluttered way of saying “ $A$ ”.

## Example Prolog Program - Family Tree

```
grandparent(X,Z) :- parent(X,Y), parent(Y,Z).  
parent(X,Y) :- father(X,Y).  
parent(X,Y) :- mother(X,Y).
```

```
father(ken, mary).  
mother(lily, mary).  
mother(mary, john).
```

- Some facts about father and mother relations
- General rules about parents and grandparents
- First we load this program called `family.pl` into Prolog with `[family], or consult(family).`

## Example Prolog Program - Family Tree continued

- After loading, we can ask Prolog about which family relations follow from the facts and rules above
- `?- grandparent (ken, john) .`
- Prolog will say **yes**
- `?- grandparent (mary, ken) .`
- Prolog will say **no**
- We can also consult user, as in `[user]`, to read Prolog code from the terminal. Stop with Ctrl-D to get back to the usual prompt.



## General Form of Prolog Queries

- A query is also called a goal
- General form  $?- C_1, C_2, \dots, C_k.$
- $?-$  is the Prolog prompt, waiting for your queries
- $C_i$  are atoms, called subgoals
- Don't. forget. the. dot. at. the. end. Or. nothing. will. happen.
- Prolog will try to prove all of  $C_1, C_2, \dots, C_k$ , using the facts and rules in your program
- Does  $C_1$  and  $C_2$  and ... and  $C_k$  follow logically from your program?
- Equivalently: if all the statements in your program are true, then is the conjunction  $C_1$  and  $C_2$  and ... and  $C_k$  also true?

# Prolog Execution

- Rough outline of algorithm:
- to solve a goal  $?- C_1, C_2, \dots, C_k.$
- Try to solve each subgoal  $C_i$  from left to right
- To solve a subgoal, find a clause in the program whose head can be “matched” with the subgoal
- Replace the subgoal by the body of the clause
- Apply the variable bindings, if any
- This step is a little bit like function application in Lisp
- If all subgoals are eventually solved, then the original goal is solved.

## Sample of Execution

- Query: `grandparent (ken, john) .`
- Try to match with head of clause  
`grandparent (X, Z) :- parent (X, Y) ,  
parent (Y, Z) .`
- The match works if we bind the variables as follows:
- `X = ken` and `Z = john`
- Now we replace the original query with the body, after substituting the variables:
- New query: `parent (ken, Y) , parent (Y, john) .`
- Note that `Y` is still an unbound variable.

## Sample of Execution - Continued

- New query: `parent(ken, Y), parent(Y, john) .`
- Important: in queries, free variables are **existentially quantified**
- We do **not** need to show that the query is true **for all Y**
- We only need to find at least one solution:  
There exists some Y such that `parent(ken, Y)` and `parent(Y, john)` are both true (for the same choice of Y)

## Sample of Execution - Continued

- New query: `parent(ken, Y), parent(Y, john) .`
- To show `parent(ken, Y)`,  
we can use `parent(X, Y) :- father(X, Y) .`
- This gives subgoal `father(ken, Y) .`
- The overall goal at this step is  
`father(ken, Y), parent(Y, john) .`
- `father(ken, Y)` matches the fact  
`father(ken, mary) .`
- So `father(ken, Y)` can be solved  
by setting `Y = mary`.

## Sample of Execution - Continued

- Query: `parent(ken, Y), parent(Y, john) .`
- `father(ken, Y)` solved by setting `Y = mary`.
- Remaining goal now: `parent(mary, john) .`
- To solve `parent(mary, john) .` we can use `parent(X, Y) :- mother(X, Y) .`
- So, must solve `mother(mary, john) .`
- Easy! This is a fact in our program. Finally, all subgoals solved!
- The original query `?- grandparent(ken, john) .` is answered with `yes`. Prolog found a proof for it!
- How exactly did it find this proof? More next time.

# Summary of Prolog Intro

- Discussed basics of Prolog syntax and its foundation in logic
- Sample program for family tree
- Sample execution steps - how queries can be resolved by matching with head of rule, then replacing it by body
- The matching may involve binding variables
- How to select the rule to match, and what if the matching fails? More next time.