## Computing Science (CMPUT) 325 Nonprocedural Programming

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## Logic Programming vs Other Programming Styles

- Review major types of programming styles
- Imperative use destructive assignments to change state
  - int x = 5;
  - x = 15;
- Functional programming first part of this course
  - Computation as function application
- From now on: logic programming, declarative programming
  - Computation as logical inference
  - From facts and rules, derive answers to a given query

### What is logic programming (LP)?

- Programs are written in the language of some logic
- Execution of a logic program is a theorem proving process
- Prolog, PROgramming in LOGic, is a LP language
- Prolog is based on a subset of first order predicate logic
- There are many other LP languages
- Prolog is (by far) the most popular LP language for general purpose programming

#### Prolog System, Tutorial and Labs

- We use SWI Prolog
- Open source Prolog system, see Resource page on eClass for download
- Installed on the undergrad machines
- Type swipl on the command line to start
- Prolog Tutorial next week in labs

## Why logic programming (LP) and Prolog?

- Declarative style of programming
- Write a specification of a solution to a problem
- The specification is executable -Prolog can use it to find a solution
- The core of Prolog is a search process to find such a solution
- Prolog is further away from classical programming than functional programming

# How is LP different from Imperative or Functional Languages?

- So far: specify all computations step by step
- Prolog: specify what properties a solution should have, then let Prolog search for it
- Understanding this search and using it to your advantage is the key for mastering Prolog
- Several other features of Prolog help with this
  - see next slide

### Some Important Features of Prolog

- Procedure is defined recursively
- Invocation of a procedure is by pattern matching
- Prolog has a single but very powerful logic inference rule called unification
- Combining these features, you can write some amazingly short and powerful programs
- You can also get unexpected behavior and infinite loops very easily... we will learn best practices to stay out of trouble

#### Logic

- · There are many different kinds of logic
  - Predicate logic, first order logic, higher order logic, modal logic, lambda calculus,...
- A logic is a language
- Like any language it has syntax and semantics
- Beyond ordinary language, a logic also has inference rules

### **Syntax**

- Syntax: the rules about what are well-formed formulas in a logic
- Example: predicate logic: a ∨ b
- Example: first-order logic:  $\forall x \, p(x)$
- Syntax is usually the easy part of a logic
- Semantics is the hard part

#### **Semantics**

- Semantics in written or spoken language: the meaning of a text
- Semantics in logic: the meaning of a well-formed formula
- How to express the meaning in a formal way?
- The classic approach is called "model-theoretic" semantics
- We will discuss it a little bit now, in depth later in this course
- Other formal semantics exist see https://en. wikipedia.org/wiki/Formal\_semantics\_(logic)

#### Logical Consequences

- Roughly, a semantics describes all the logical consequences of a formula
- Example: predicate logic formula F: a ∧ b
- \( \) is logical and
- a and b are atoms
- Assume F is true. Then we can infer:
  - a is true
  - b is true
- Whenever F is true, both a and b have to be true as well

# Expressing Logical Consequence In Natural Language

- In English, there are many different but equivalent ways of stating logic consequences. Some examples:
  - b is a logic consequence of F;
  - b follows (logically) from F
  - F implies b
  - F entails b
  - whenever F is true, b is also true
  - b is true because of F
  - ...

#### Inference Rules

- Given a collection of one or more formulas:
- An inference rule can be used to derive new formulas
- Examples:
  - Given the formula a ∧ b, we can derive the new formula a
  - Given the formula a ∧ b,
     we can derive the new formula b

#### Logical Consequence vs Inference

- There is a strong link between consequence and inference
- Semantics: a is a logical consequence of a ∧ b
- Inference: an inference rule allows us to create a new formula a from a given formula a ∧ b
- Ideally, we want inference rules that are:
  - Sound they respect the semantics
  - Complete they allow us to derive everything that is true according to the semantics

### Sidebar: Our University's Motto



- The UofA's motto is Quaecumque Vera.
- It is Latin and means "Whatsoever things are true"
- It asks us to go out and find the truth about the world through research
- Similarly, sound and complete logical inference rules can be used to find the true formulas in a given "world", which is given as a set of formulas

#### Example - Unsound Inference Rule

- Example of a bad inference rule:
- From  $a \lor b$ , derive  $a \land b$
- v means logical or
- In English: if a or b is true, then both a and b are true
- We know this is wrong in predicate logic
- A system that used such a rule would "prove" formulas that do not correspond to our intended semantics
- Example: "the ball is red or green" does not imply "the ball is red and green"

#### Example - Unsound Inference Rule

- We can show by using a counterexample that the implication:
  - if  $a \lor b$ , then  $a \land b$
- ...is invalid in predicate logic.
- Proof: set a to true, b to false
- Then  $a \lor b$  is true, and  $a \land b$  is false
- The implication  $\texttt{true} \to \texttt{false}$  is false according to the rules of logic.

### More on Sound and Complete; Efficiency

- All inference rules must be sound with respect to the semantics
- It is good if they are also complete if any logical consequence can be derived. But that is not a must for a useful system.
- Inference rules should also be efficient to be useful in practice

#### Natural Deduction is Inefficient

- There is a proof system called "natural deduction" which is close to normal logic rules, such as the one above
- From given set of formulas, derive new ones
- Efficiency problems:
  - We need many inference rules
  - Applying them makes the number of formulas we can derive explode
  - It is too hard to figure out which new formulas will be useful later, and which are just junk
  - Example: from a we can derive a ∨ a, a ∧ a, a ∨ (a ∧ a),
     a ∧ a ∧ a ∧ a ∧ a, ...
- Prolog has only a single inference rule called resolution. It is more efficient in general.

### Summary so Far

- Discussed logic in terms of syntax, semantics, and inference rules
- Discussed problems with "human-like" inference rules
- Hinted that Prolog uses a different style of inference based on resolution