

## Naïve Bayes Model

- For simplicity, we only consider binary features

$$x_i \in \{0,1\}, \text{ i.e., } \mathbf{x} \in \{0,1\}^d$$

- The generation model is

$$t \sim \text{Categorical}(\pi_1, \dots, \pi_K)$$

$$\mathbf{x}_i | t = k \sim \text{Bernoulli}(p_{k,i})$$

Here: A Bernoulli distribution parametrized by  $\pi$  means that

$$\Pr[X = 1] = \pi \text{ and } \Pr[X = 0] = 1 - \pi.$$

It is a special case of categorical distributions in that only two cases are considered.

- Such a model can be used to represent a document in text classification. For example, the target indicates Spam or NotSpam. The feature indicates if a word in the vocabulary occurs in the document.

**Problem 1.** Please show that the parameters of naïve Bayes decompose, i.e., the probability factorizes (for the same reason as Gaussian mixture models).

**Problem 2.** Write out the MLE for naïve Bayes (which is simply counting).

Hint: No proof is needed for the second part, because the MLE for categorical distribution has been clear in the Gaussian mixture models.

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