

Problem: Find value of x that maximizes function $f(x) = x^2$ for integer values of $0 \leq x \leq 255$.
Concentrate only on representation, initialization, and selection

1. **Representation** – numbers up to 255 can be represented by 8 bits ($2^8 = 256$) – use 8-bit binary code
2. **Initialization** – randomly generate e.g. 5 elements/individuals of the population

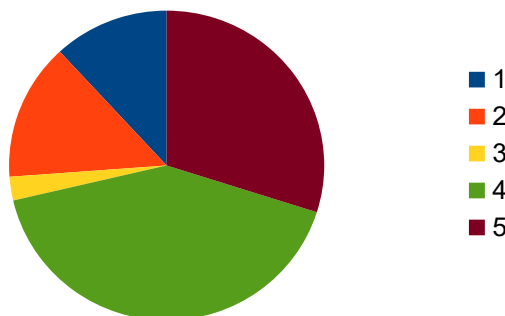
| # | Code |
|---|----------|
| 1 | 01011100 |
| 2 | 01100101 |
| 3 | 00101010 |
| 4 | 10101100 |
| 5 | 10010010 |

3. Selection

a) fitness proportional: evaluate fitness of each individual, and assign it a probability of selection proportional to its relative fitness within the population

| # | Code | x | Fitness | Percentage | Probability | Cumulative |
|---|----------|-----|----------------|------------|-------------|------------|
| 1 | 01011100 | 92 | 8464 | 11.87% | 0.12 | 0.12 |
| 2 | 01100101 | 101 | 10201 | 14.30% | 0.14 | 0.26 |
| 3 | 00101010 | 42 | 1764 | 2.47% | 0.02 | 0.29 |
| 4 | 10101100 | 172 | 29584 | 41.48% | 0.41 | 0.70 |
| 5 | 10010010 | 146 | 21316 | 29.88% | 0.30 | 1.00 |
| | | | $\Sigma=71329$ | 100.00% | 1.00 | |

This corresponds to selection using a biased roulette wheel – each sector has area corresponding to the relative (percentage) fitness of the individual:



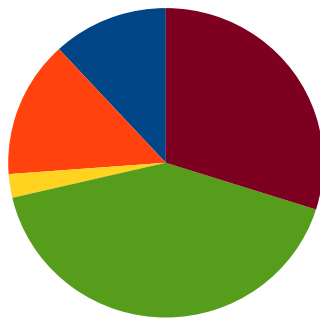
Individuals are then selected by generating a random number, and selecting an individual based on the interval (roulette sector) the number falls in.

b) rank: assign rank to each individual based on its fitness, and then distribute the probability of individual selection based on the ranks (not fitness)

| # | Code | x | Fitness | Rank | Percentage | Probability | Cumulative |
|---|----------|-----|----------------|-------------|------------|-------------|------------|
| 1 | 01011100 | 92 | 8464 | 2 | 13.33% | 0.13 | 0.13 |
| 2 | 01100101 | 101 | 10201 | 3 | 20.0% | 0.20 | 0.33 |
| 3 | 00101010 | 42 | 1764 | 1 | 6.67% | 0.07 | 0.40 |
| 4 | 10101100 | 172 | 29584 | 5 | 33.33% | 0.33 | 0.73 |
| 5 | 10010010 | 146 | 21316 | 4 | 26.67% | 0.27 | 1.00 |
| | | | $\Sigma=71329$ | $\Sigma=15$ | 100.00% | 1.00 | |

This corresponds to selection using a biased roulette wheel – each sector has area corresponding to the relative (inverse) rank of the individual:

Fitness proportional



vs.

Rank

