ECE 449 - Intelligent Systems Engineering Python Supplement

1 Jupyter Notebook

All labs will be completed in a **Jupyter notebook**, which is a document that allows you to create and run Python code, while including visualizations and explanatory texts in the same document. Consequently, the lab reports will also be completed in these documents. The Jupyter notebook templates for each lab can be found on eClass.

To begin, go to https://cybera.syzygy.ca and log-in with your ualberta e-mail address. We strongly recommend using Google Chrome to complete these labs. Microsoft Edge and Firefox do not print the results correctly. Start your server, upload a Jupyter notebook file, and open it. In order to run a cell, select it, and press SHIFT+ENTER. Each cell has access to variables and functions in cells that were already run. The In [] to the left of a code cell indicates its current state:

```
In [] - the cell has not yet been runIn [*] - the cell is currently being runIn [#] - the cell has been run and in the order indicated by the number
```

A cell has access to all of the variables and functions in previously run cells. Therefore, make sure that you run the cells with code that are initially provided in the template before proceeding with your own coding. Keyboard shortcuts can be found under HELP \rightarrow KEYBOARD SHORTCUTS.

When you have completed your notebook and are ready to submit it, download the document as HTML. This is accomplished by going to FILE \rightarrow DOWNLOAD AS \rightarrow HTML. However, your local server must be configured correctly for the results to display properly. Run the cell below, and then reboot your server by going to CONTROL PANEL \rightarrow STOP MY SERVER for the changes to be set. Make sure that all of the necessary plots are displayed in the final document that you submit. Document submission will be done through eClass, and the due date can be found at the top of each lab manual.

Configure notebooks to save results as well for HTML printing:

```
!mkdir -p ~/.jupyter
!echo "c.FileContentsManager.pre_save_hook = None" > ~/.jupyter/jupyter_notebook_config.py
Various libraries are required for these labs. Run the cell below to install these libraries.
```

NOTE: If you are installing the library for the first time, you will need to restart the kernel in order to use it in the rest of the document.

```
%%bash
# "--user" is essential to install in local environment
pip install --user -U scikit-fuzzy
pip install --user -U minisom
pip install --user -U pyeasyga
```

2 Python

All Jupyter notebooks will be completed in Python 3. This section will comprise of various code cells to introduce you to the syntax and some common statements. A more in-depth tutorial can be found at

https://docs.python.org/3/tutorial/.

Different ways that one can import libraries that you will likely encounter: (import as is; import and assign a pseudonym; and/or import a sub-library)

```
import math
import numpy as np
from numpy import random
```

To print data, stings can be concatenated or comma separated. Numerical data can be comma separated or one of the string format methods.

```
### VARIABLE ASSIGNMENT AND PRINTING ###
# Note that there is no need for terminating semicolons
name = "John"
age = 19
print("Hello " + name + ",")
print("My name is also", name)
# the comma separated method adds spaces with each separation
print("You are", age, "years old?")
# 0:d means the integer in the first argument in "format()"
print("What a coincidence I am also 0:d years old".format(age))
# the older method of inserting a number into a string
print("I would guess that the odds of meeting someone with the same name and age is only
%.4f%" % (random.rand()/100))
```

If-else statements don't change much but there will be some changes in usable syntax.

```
### CONTROL FLOW (IF) ###
# Note that tabs and colons are used instead of curly braces to group sets of statements
x = 10
if x > 11:
  print("x is greater than 11.")
elif x == 10:
  print("x is equal to 10.")
  print("x is less than 9.")
if x is not 11:
  print("x is not 11.")
elif x != 11:
  print("x is not 11.")
if x in [1,2,3,4]:
  print("x is in the set.")
if math.isnan(x):
  print("x is NaN.")
if isinstance(x, int):
  print("x is an integer")
```

For loops automatically iterate through a list and break at the end. While loops require an exit condition and any iterations must be explicitly incremented. FYI: it is very important to keep track of the actual variable scope otherwise you might get some strange behavior (e.g. starting half way though a list instead of at the beginning).

```
### CONTROL FLOW (FOR) ###
for i in range(5):
    print(i)
while i in range(5):
    print(i)
    i -= 1
```

There are different ways of initializing and storing sets of data (lists [], dictionaries, tuples (), and np.ndarrays np.array() are the most common), but keep in mind that they can behave VERY differently for the same piece of code.

```
### ARRAY CREATION ###
grades = np.array([85, 70, 90, 100])
print(grades)
x = [3]
y = (3,)
z = np.array([3])
# x*x and y*y give an error
print(x*3, y*3, z*z, z*3)
```

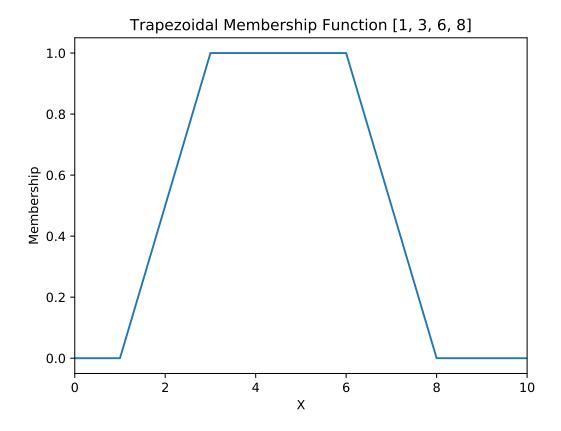
3 Fuzzy Logic

Assume that the following import statements are used:

3.1 Defining a membership function

A membership function can be defined in several ways. A trapezoidal membership function requires four parameters: a, b, c, and d. a and d specify the ends of the base, and b and c specify the ends of the top.

```
X = np.linspace(0, 10, num = 11) # 0 to 10 with 11 elements
Y = fuzz.trapmf(X, [1, 3, 6, 8])
plt.plot(X, Y)
plt.xlabel('X')
plt.ylabel('Membership')
plt.title('Trapezoidal Membership Function [1, 3, 6, 8]')
plt.show()
```



3.2 Concentration and dilatation

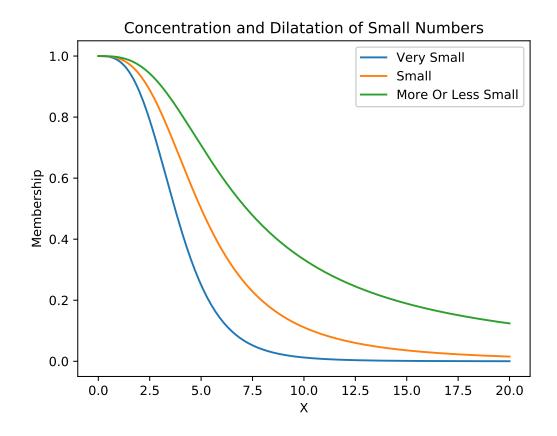
Concentration emphasizes points with higher membership values. For example, concentration of "small numbers" turns into "**very** small numbers". This is quantitatively represented by squaring the membership values:

$$Con(A) = A^2(x)$$

Dilatation of "small numbers" turns into "more or less small numbers", and can be quantitatively represented by taking the square root of the membership values:

$$Dil(A) = \sqrt{A(x)}$$

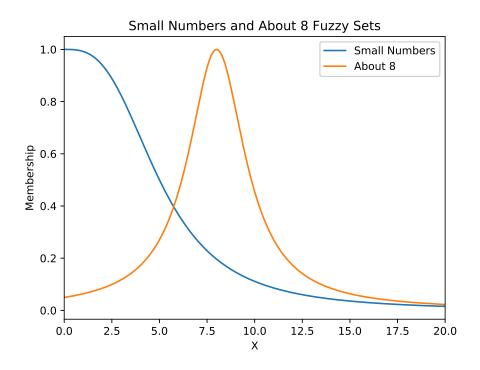
```
X = np.linspace(0, 20, num = 201)
A = 1 / (1 + (X / 5 )** 3) # "small numbers"
verySmall = A ** 2
moreOrLessSmall = A ** (0.5)
verySmallHandle ,= plt.plot(X, verySmall, label = 'Very Small')
smallHandle ,= plt.plot(X, A, label = 'Small')
moreOrLessSmallHandle ,= plt.plot(X, moreOrLessSmall, label = 'More Or Less Small')
plt.xlabel('X')
plt.ylabel('Membership')
plt.title('Concentration and Dilatation of Small Numbers')
plt.legend(handles = [verySmallHandle, smallHandle, moreOrLessSmallHandle])
plt.show()
```

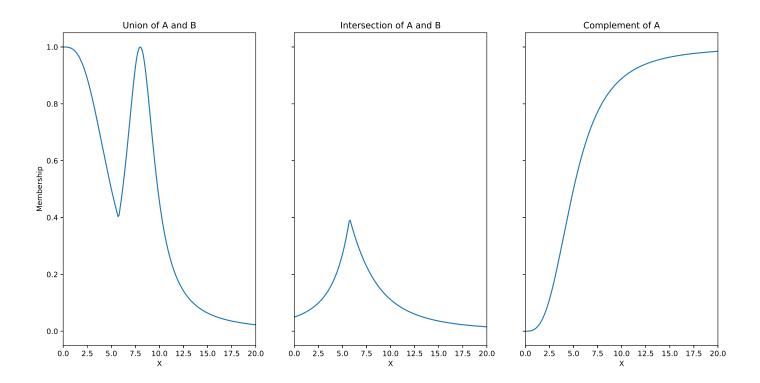


3.3 Union, intersection, and complement

The union $(A \cup B)$, intersection $(A \cap B)$, and complement (A^C) are common operations performed on fuzzy sets. There are various realizations of the union and intersection operations, but the most common forms are maximum and minimum, respectively. The complement operation is always defined as 1 - A(x)

```
X = np.linspace(0, 20, num = 201)
A = 1 / (1 + (X / 5 ) ** 3) # "small numbers"
B = 1 / (1 + 0.3 * (X - 8) ** 2) # "about 8"
[Y, union] = fuzz.fuzzy_or(X, A, X, B) # Y, new universe of discourse; union, new MF
[Z, intersection] = fuzz.fuzzy_and(X, A, X, B)
complement = fuzz.fuzzy_not(A)
```





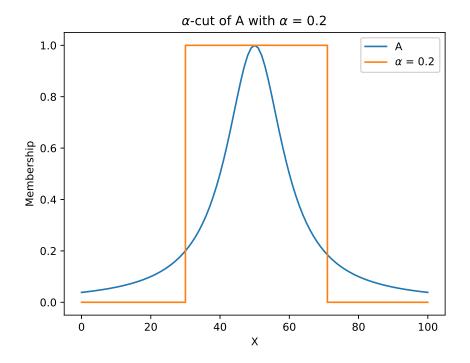
3.4 α -cuts

An α -cut is a crisp set that contains the elements that have membership greater than or equal to a certain value, α . Consider a fuzzy set with membership function:

$$A(x) = \frac{1}{1 + 0.01(x - 50)^2}$$

Example:

```
X = np.linspace(0, 100, num = 101)
A = 1 / (1 + 0.01 * (X - 50) ** 2)
alphaCut = (A >= 0.2) # alpha-cut with alpha = 0.2
AHandle ,= plt.plot(X, A, label = 'A')
aCutHandle ,= plt.step(X, alphaCut, where = 'post', label = r'$\alpha$ = 0.2')
plt.xlabel('X')
plt.ylabel('Membership')
plt.title(r'$\alpha$-cut of A with $\alpha$ = 0.2')
plt.legend(handles = [AHandle, aCutHandle])
plt.show()
```



3.5 Relations

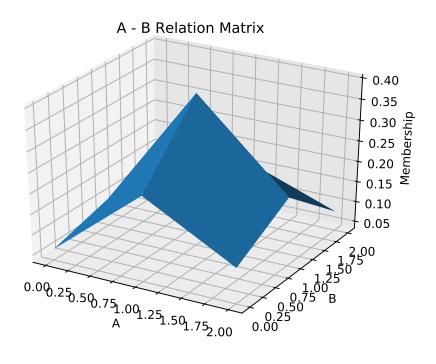
Fuzzy relations between two fuzzy sets are performed using implication operators. Common operators include Larsen implication (product) and Mamdani implication (minimum). The relation can be expressed as:

$$R_{A\to B}(x,y) = [A(x)B(y)]$$

```
uniA = np.array([0, 1, 2])
uniB = np.array([0, 1, 2])
A = np.array([0.3, 0.5, 0.2])
B = np.array([0.2, 0.8, 0.4])
larsen = fuzz.relation_product(A, B) # Larsen implication
fig = plt.figure()
```

```
[gX, gY]= np.meshgrid(uniA, uniB, indexing = 'ij')
ax = fig.gca(projection = '3d')
ax.plot_surface(gX, gY, larsen)
ax.set_xlabel('A')
ax.set_ylabel('B')
ax.set_zlabel('Membership')
ax.set_title('A - B Relation Matrix')
plt.show()
```

$$larsen = \begin{bmatrix} 0.06 & 0.24 & 0.12 \\ 0.10 & 0.40 & 0.20 \\ 0.04 & 0.16 & 0.08 \end{bmatrix}$$



3.6 Projections

The x and y projections of R(x, y) can be respectively expressed as:

$$ProjR_x(x) = sup_{y \in Y}R(x, y)$$

 $ProjR_y(y) = sup_{x \in X}R(x, y)$

The supremum (sup) operator often employed is the maximum operation. Take note that the projection operation is done according to matrix indexing, not Cartesian.

$$xProj = \begin{bmatrix} 0.24\\0.40\\0.16 \end{bmatrix}$$
$$yProj = \begin{bmatrix} 0.10 & 0.40 & 0.20 \end{bmatrix}$$

3.7 Reconstruction

The reconstruction of a fuzzy relation is expressed as the Cartesian product of its projections.

Example:

```
reconstruction = yProj * xProj
print("reconstruction:\n", reconstruction)
```

$$reconstruction = \begin{bmatrix} 0.024 & 0.096 & 0.048 \\ 0.040 & 0.160 & 0.080 \\ 0.016 & 0.064 & 0.032 \end{bmatrix}$$

3.8 Cylindrical extension

Cylindrical extension is defined as:

$$Cyl(A)(x,y) = A(x) \ \forall \ y \in Y$$

Example:

$$cyl = \begin{bmatrix} 0.24 & 0.24 & 0.24 \\ 0.40 & 0.40 & 0.40 \\ 0.16 & 0.16 & 0.16 \end{bmatrix}$$

3.9 Sup-t composition

Using relations R_1 and R_2 , the sup-t composition can be performed with various **t** operations. Some common combinations are max-min and max-product.

$$R = \begin{bmatrix} 0.5 & 0.5 \\ 0.4 & 0.7 \end{bmatrix}$$

3.10 Compositional rule of inference

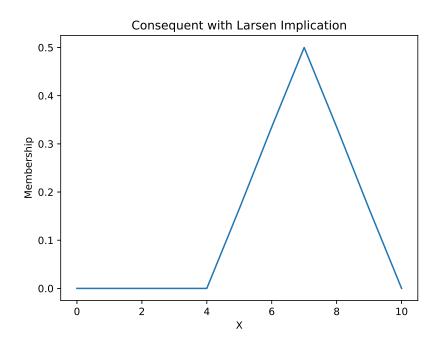
Generalized modus ponens states that when a rule's antecedent is satisfied to some degree, its consequent can be inferred to the same degree.

This can be written using the implication relation (R(x,y)) as in the max-min composition:

$$B' = A' \circ R(x, y)$$

Consider the rule "**IF** x **IS** ABOUT 3 **THEN** y **IS** ABOUT 7" with fuzzy sets FN3 = ABOUT 3 and FN7 = ABOUT 7 defined on the universe of discourse, X. Applying a compositional rule of inference to a fuzzy singleton A = 4, using Larsen implication, yields the following results.

```
X = np.linspace(0, 10, num = 11)
FN3 = np.array([0, 0, 0.5, 1.0, 0.5, 0, 0, 0, 0, 0, 0])
FN7 = np.array([0, 0, 0, 0, 0.33, 0.67, 1.0, 0.67, 0.33, 0])
larsen = fuzz.relation_product(FN3, FN7)
A = np.zeros(11) # Define fuzzy singleton
A[4] = 1
fuzzySet = fuzz.maxprod_composition(A, larsen)
plt.plot(X, fuzzySet.T)
plt.xlabel('X')
plt.ylabel('Membership')
plt.title('Consequent with Larsen Implication')
plt.show()
```



3.11 Defuzzification

There are various methods of determining the crisp value from a fuzzy set. The most frequently used are the centroid and mean of maxima (MOM) methods.

Example:

```
X = np.linspace(0, 1, num = 6)
fuzzySet = np.array([0, 0.165, 0.335, 0.5, 0.335, 0.165])
crispValue = fuzz.defuzz(X, fuzzySet, 'mom') # Mean Of Maximum defuzzification method
```

$$crispValue = 0.6$$

4 Neural Networks

Assume that the following import statements are used:

```
import numpy as np
import matplotlib.pyplot as plt
from sklearn import preprocessing
from sklearn.linear_model import Perceptron
from sklearn.neural_network import MLPRegressor, MLPClassifier
from minisom import MiniSom
```

4.1 Preprocessing

The Python library, sklearn, contains some common methods of data preprocessing. This includes normalization, standard scaling, and minimum-maximum scaling.

4.1.1 Normalization

Using this function on an array of data normalizes each input vector in the array (along the x-axis) to unit length.

Example:

```
X = np.array([[0, 1], [3, 4], [0.5, 0.5]])
normX = preprocessing.normalize(X)
```

$$normX = \begin{bmatrix} 0 & 1\\ 0.6 & 0.8\\ 0.707 & 0.707 \end{bmatrix}$$

4.1.2 Standard scaling

This function standardizes features in the input data by removing the mean and scaling to unit variance. When the input data is transformed, the scaler allows for the user to perform an inverse transform to revert the data back to its original form.

```
X = np.array([[0, 1], [3, 4], [0.5, 0.5]])
scaler = preprocessing.StandardScaler()
stdX = scaler.fit_transform(X)
invX = scaler.inverse_transform(stdX) # X = invX
```

$$stdX = \begin{bmatrix} -0.889 & -0.539 \\ 1.40 & 1.40 \\ -0.508 & -0.863 \end{bmatrix}$$

4.1.3 Minimum-maximum scaling

Minimum-maximum scaling transforms the input data by scaling each feature to a given range, typically [0, 1]. Each column of the input array is scaled to this range, independently of the other columns. Similar to standard scaling, an inverse transform function is provided.

Example:

$$minmaxX = \begin{bmatrix} 0 & 0.143 \\ 1 & 1 \\ 0.167 & 0 \end{bmatrix}$$

4.2 Perceptron

sklearn provides a way of building a simple perceptron, with the ability to set how many iterations of training it completes, and appropriate methods to employ the neural unit.

Example:

```
# Logical "OR" data
X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]]) # Inputs
Y = np.array([0, 1, 1, 1]) # Targets
percep = Perceptron(n_iter = 50)
percep.fit(X, Y) # Train the perceptron
Z = percep.predict(X)
```

$$Z = \begin{bmatrix} 0 & 1 & 1 & 1 \end{bmatrix}$$

4.3 Multi-layer perceptron

MLPRegressor and MLPClassifier in sklearn build a multi-layer perceptron, with the ability to customize various parameters, such as the number of units in each hidden layer, the activation function, and the initial learning rate. It has similar training and prediction methods to the perceptron class. Additionally, if the output values after each iteration are required, a partial_fit method is provided that trains the MLP for one iteration.

```
# Logical "XOR" data
X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]]) # Inputs
Y = np.array([0, 1, 1, 0]) # Targets
mlp = MLPClassifier(
    hidden_layer_sizes = (100,), # One hidden layer of 100 units
    activation = 'relu',
    max_iter = 1000
    )
mlp.fit(X, Y) # Train the MLP
Z = mlp.predict(X)
```

$$Z = \begin{bmatrix} 0 & 1 & 1 & 0 \end{bmatrix}$$

4.4 Self-organizing map (Kohonen network)

MiniSom is a Python library that implements self-organizing maps. The constructor permits for customization of size, neighborhood function, and learning rate.

```
inputData = np.random.rand(100,2)
noIter = 100

som = MiniSom(
    x, # X dimension of SOM
    y, # Y dimension of SOM
    input_len, # Number of elements in an input vector
    sigma = 1.0, # Spread of neighborhood function
    learning_rate = 0.5, # Initial learning rate
    neighborhood_function = 'gaussian' # Neighborhood function type
)
```

Next, the weights must be randomly initialized, and then the SOM needs to be trained. The network can be trained using either a random method (train_random) or a batch method (train_batch).

```
som.random_weights_init(inputData) # Initialize weights randomly
som.train_random(inputData, noIter) # Train randomly noIter times
```

Finally, the SOM results can be visualized using various methods, such as distance_map, which displays how close each neuron is to its neighboring neurons, and activation_response, which displays how many times each neuron was activated to an input array of data.

```
plt.pcolor(som.distance_map().T)
plt.pcolor(som.activation_response(inputData).T)
```

5 Genetic Algorithms

Assume that the following import statements are used:

```
import numpy as np
from pyeasyga import pyeasyga
```

pyeasyga is a Python library that allows for the creation and customization of genetic algorithms. Only the input data needs to be specified when creating an algorithm, but numerous other parameters can be specified.

```
inputData = np.random.rand(10,10)

ga = pyeasyga.GeneticAlgorithm(
    inputData,
    population_size = 50,
    generations = 100,
    crossover_probability = 0.8,
    mutation_probability = 0.2,
    maximise_fitness = True # Minimizes fitness if False
)
```

Additionally, functions to implement the individual creation, crossover, mutation, selection, and fitness functions need to be assigned to the GA.

```
def create_individual(data):
    individual = ...
    return individual
def crossover(parent_1, parent_2):
    child_1 = ...
    child_2 = ...
    return child_1, child_2
def mutate(individual):
    individual = ...
def fitness(individual, data):
    fitness = ...
    return fitness
ga.create_individual = create_individual
ga.crossover_function = crossover
ga.mutate_function = mutate
ga.selection_function = ga.tournament_selection # pyeasyga's implemented selection function
ga.fitness_function = fitness
```

Finally, the GA can be run, and the best solution can be obtained.

```
ga.run()
bestSoln = ga.best_individual()
print("Fitness = ", bestSoln[0])
print("Solution = ", bestSoln[1])
```

6 Useful Links

6.1 Library documentation

• NumPy

- Matplotlib
- \bullet skfuzzy
- ullet sklearn preprocessing
- ullet sklearn perceptron
- $\bullet\,$ sklearn MLP
- \bullet MiniSom
- pyeasyga

6.2 Plotting

- 2-D plots
- Figure labels
- Legend
- \bullet Subplots
- Surface plots