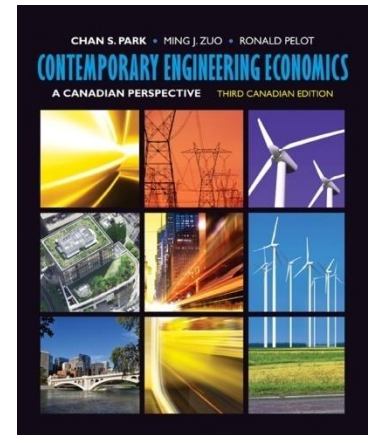


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# Total-Investment Approach & Incremental Investment Analysis

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Lecture No. 17

Chapter 6

Contemporary Engineering Economics Third Canadian  
Edition

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# Lecture 17 Objectives

- How do firms compare alternatives using a total investment approach and incremental analysis?

## Example 6.1: Present-Worth Comparison: Three Alternatives

- Bullard Company (BC) is considering expanding its range of industrial machinery. Several combinations of new equipment and labour could serve to fulfill this new function:
  1. (M1) New machining centre with three operators
  2. (M2) New machining centre with automatic pallet changer and with three operators
  3. (M3) New machining centre with automatic pallet changer and with two task-sharing operators
- BC has a MARR = 12%. The estimated costs and additional revenues are as follows:

## Example 6.1: Present-Worth Comparison: Three Alternatives (continued)

	Machining Centre Methods		
	M1	M2	M3
Investment:			
Machine tool purchase	\$121,000	\$121,000	\$121,000
Automatic pallet changer		\$ 66,600	\$ 66,600
Installation	\$ 30,000 ✓	\$ 42,000	\$ 42,000
Tooling expense	\$ 58,000 ✓	\$ 65,000 ✓	\$ 65,000 ✓
Total investment	\$209,000	\$294,600	\$294,600
Annual benefits: Year 1			
Additional revenues	\$ 55,000	\$ 69,300	\$ 36,000 ✓
Direct labour savings			\$ 17,300
Setup savings		\$ 4,700	\$ 4,700
Year 1: Net revenues	\$ 55,000	\$ 74,000	\$ 58,000
Years 2–5: Net revenues	constant	constant	$r = 13\%/year$
Salvage value in year 5	\$ 80,000	\$120,000	\$120,000

←  
- 1 person

Geometrical series

## Example 6.1: Present-Worth Comparison: Three Alternatives (continued)

$n$	M1	M2	M3
0	-\$209,000	-\$294,600	-\$294,600
1	55,000	74,000	58,000
2	55,000	74,000	64,540
3	55,000	74,000	74,060
4	55,000	74,000	83,688
5	135,000	194,000	214,567

Investments

$g = 13\%$

Salvage  
+ Revenue

# Example 6.1: Solution

## ■ Option M1

$$PW(12\%)_{M1} = -\$209,000 + \$55,000(P/A, 12\%, 5) + \$80,000(P/F, 12\%, 5)$$
$$= \$34,657$$

Equal series

## ✖ Option M2

$$PW(12\%)_{M2} = -\$294,600 + \$74,000(P/A, 12\%, 5) + \$120,000(P/F, 12\%, 5)$$
$$= \$40,245$$

## ■ Option M3

$$PW(12\%)_{M3} = -\$294,600 + \$58,000(P/A, 13\%, 12\%, 5)$$
$$+ \$120,000(P/F, 12\%, 5)$$
$$= \$37,085$$

$g = 13\%$   
geometric series

## Example 6.2: Annual Equivalent Comparison: Three Alternatives

### ■ Option M1

$$\begin{aligned} AE(12\%)_{M1} &= -\$209,000(A/P, 12\%, 5) + \$55,000 + \$80,000(A/F, 12\%, 5) \\ &= \underline{\$9614} \end{aligned}$$

### ~~■~~ Option M2

$$\begin{aligned} AE(12\%)_{M2} &= -\$294,600(A/P, 12\%, 5) + \$74,000 + \$120,000(A/F, 12\%, 5) \\ &= \underline{\$11,164} \end{aligned}$$

### ■ Option M3

$$\begin{aligned} AE(12\%)_{M3} &= -\$294,600(A/P, 12\%, 5) \\ &\quad + \$58,000(P/A_1, 13\%, 12\%, 5)(A/P, 12\%, 5) \\ &\quad + \$120,000(A/F, 12\%, 5) \\ &= \underline{\$10,288} \end{aligned}$$

# Decision Rules Using the Total Investment Approach:

- Select Project A if any one of the following conditions is met:

$$PE_A > PE_B, AE_A > AE_B, FE_A > FE_B$$

That is, select the project with the largest PE, AE or FE value, when there are more than 2 projects.

- Important: Don't make decision based on direct comparison of IRR<sub>A</sub> and IRR<sub>B</sub> ← *check Sign changes in Net Cash flow*



# Flaws in Project Ranking by IRR

- **Issue:** Can we rank the mutually exclusive projects by the magnitude of its IRR?

<i>n</i>	<b>A1</b>	<b>A2</b>
<b>0</b>	-\$1,000 ✓	-\$5,000 ✓
<b>1</b>	\$2,000 ✓	\$7,000 ✓
<b>IRR</b> ✓	100% <i>Is relative to investment amount</i>	40% <i>(less attractive)</i>
<b>PW (10%)</b>	\$818 ✓	\$1,364 ✓

*Tool*

*Decision making*

*{ Absolute returns*

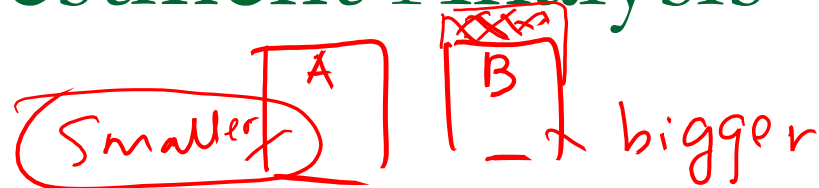
# Incremental Investment Analysis

$n$	Project A1	Project A2	Incremental Investment (A2 – A1)
0	-\$1,000	-\$5,000	-\$4,000
1	\$2,000	\$7,000	\$5,000
IRR	100%	40%	25%
PW(10%)	\$818	\$1,364	\$546

- Assuming a MARR of 10%, you can always earn that rate from other investment source, i.e., \$4,400 at the end of one year for \$4,000 investment.
- By investing the additional \$4,000 in A2, you would make an additional \$5,000, which is equivalent to earning at the rate of 25%. Therefore, the incremental investment in A2 is justified.

> 10% (MARR)

# Incremental Investment Analysis



- For two mutually exclusive projects, rate-of-return analysis is done by computing the internal rate of return on the incremental investment ( $IRR_{\Delta}$ ). Always subtract the lower cost investment from the highest cost one.
- Decision Rule:
  - If  $IRR_{B-A} > MARR$ , select B. ✓
  - If  $IRR_{B-A} = MARR$ , select either project.
  - If  $IRR_{B-A} < MARR$ , select A. ✓
- If a “do-nothing” alternative is allowed, each alternative’s IRR must be greater than MARR.

MARR

$IRR_{(A)} > MARR$

$\left\{ \begin{array}{l} IRR_A > MARR \\ IRR_B > MARR \end{array} \right\}$

Commercial interest only

check →

# Incremental Investment Analysis

- Incremental analysis may also be used for PW, FW, and AE analyses.
- Decision Rules:

	> 0	= 0	< 0
$PW_{B-A}$ (MARR)	select B	select either one	select A
$AW_{B-A}$ (MARR)	select B	select either one	select A
$FW_{B-A}$ (MARR)	select B	select either one	select A

accept bigger option

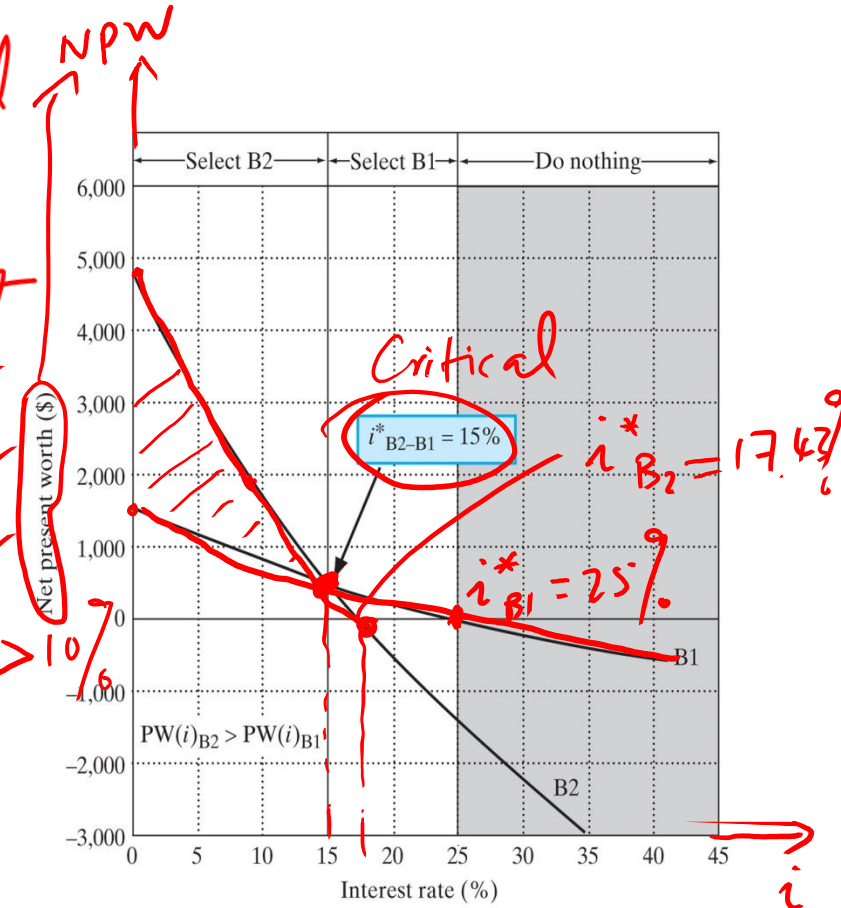
Accept smaller option

No justification

Consistent

## Example 6.3: IRR on Incremental Investment: Two Alternatives

$n$	B1	B2 <i>Bigger</i>	B2 - B1
0	-\$3,000	-\$12,000	-\$9,000
1	1,350	4,200	2,850
2	1,800	6,225	4,425
3	1,500	6,330	4,830
IRR	25.00%	17.43%	15.00%
PW	\$841	\$1718	\$877
AE	\$338	\$691	\$353
FW	\$1120	\$2287	\$1167



Given MARR = 10%, which project is a better choice?

Since  $IRR_{B2-B1} = 15\% > 10\%$ , and also  $IRR_{B2} > 10\%$ , select B2.

## Example 6.4: IRR on Incremental Investment: Three Alternatives

$n$	M1	M2	M3
0	<u>-\$209,000</u>	<u>-\$294,600</u>	<u>-\$294,600</u>
1	55,000	74,000	<u>58,000</u>
2	55,000	74,000	<u>64,540</u>
3	55,000	74,000	<u>74,060</u>
4	55,000	74,000	<u>83,688</u>
5	<u>135,000</u>	<u>194,000</u>	<u>214,567</u>
IRR =	17.62%	16.60%	15.99%

> MARR? > 12% ✓      > 12% ✓      > 12% ✓

Handwritten notes: A red arrow points from the value 135,000 in the M1 row n=5 to the underlined > MARR?. A red bracket on the right side of the table groups the values for M3 from n=1 to n=4, with a red arrow pointing down. A red note 'q=13%' is written next to the bracket.

# Example 6.4: IRR on Incremental Investment: Three Alternatives (continued)

- **Step 1:** Examine the IRR for each alternative. When “do nothing” is an option, we can eliminate any project that fails to meet the MARR. In this example all three alternatives exceed the MARR of 12%.
- **Step 2:** Compare M1 and M2 in pairs.
  - $IRR_{M2-M1} = 14.61\% > 12\%$ , *MARR*
  - so select M2. M2 becomes the current best.
- **Step 3:** Compare M3 and M2.
  - $IRR_{M3-M2} = 6.66\% < 12\%$ , *MARR*
  - so select M2 again.
- Here, we conclude that M2 is the best alternative.

## Example 6.5:

Falk Corporation is considering two types of manufacturing systems to produce its shaft couplings over six years:

(1) a cellular manufacturing system (CMS) and

(2) a flexible manufacturing system (FMS). — Computerization ↑  
— Control Software ↑

The average number of pieces to be produced with either system would be 544,000 per year. The operating cost, initial investment, and salvage value for each alternative are given on the following page.

The firm's MARR is 15%. On the basis of the IRR criterion, which alternative would be a better choice?



## Example 6.5: Incremental Analysis for Cost-Only Projects

Items	CMS Option	FMS Option
Annual O&M costs:		
Annual labour cost	\$1,169,600 <sup>higher</sup>	\$707,200
Annual material cost	832,320	598,400
Annual overhead cost	<u>3,150,000</u>	1,950,000
Annual tooling cost	470,000	300,000
Annual inventory cost	141,000	31,500
Annual income taxes	1,650,000	1,917,000
Total annual costs (AEC)	\$7,412,920	\$5,504,100
Investment (P)	\$4,500,000	\$12,500,000
Net salvage value (S)	\$500,000	\$1,000,000

## Example 6.5: Incremental Cash Flow (FMS – CMS)

Net Cash flows

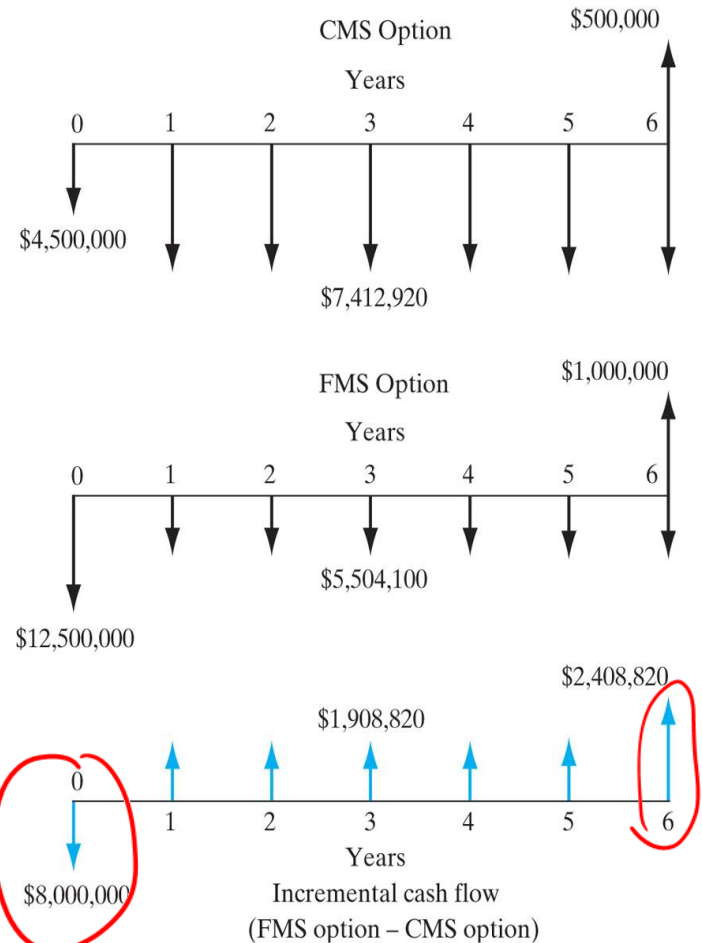
$n$	CMS Option	FMS Option	Incremental (FMS-CMS)
0	<u>-\$4,500,000</u>	<u>-\$12,500,000</u>	-\$8,000,000
1	-7,412,920	-5,504,100	1,908,820
2	-7,412,920	-5,504,100	1,908,820
3	-7,412,920	-5,504,100	1,908,820
4	-7,412,920	-5,504,100	1,908,820
5	-7,412,920	-5,504,100	1,908,820
6	-7,412,920	-5,504,100	
Salvage	+ \$500,000	+ \$1,000,000 ✓	\$2,408,820

There is no "Do Nothing".  $IRR_{CMS}$  or  $IRR_{FMS}$  is not checked

# Example 6.5: Solution

$$\begin{aligned}
 PW(i)_{FMS-CMS} &= -\$8,000,000 \\
 &\quad + \$1,908,820(P/A, i, 5) \\
 &\quad + \$2,408,820(P/F, i, 6) \\
 &= 0
 \end{aligned}$$

$$\begin{aligned}
 IRR_{FMS-CMS} &= \underline{12.43\%} < \underline{15\%}, \\
 &\text{select } \underline{\text{CMS}}.
 \end{aligned}$$



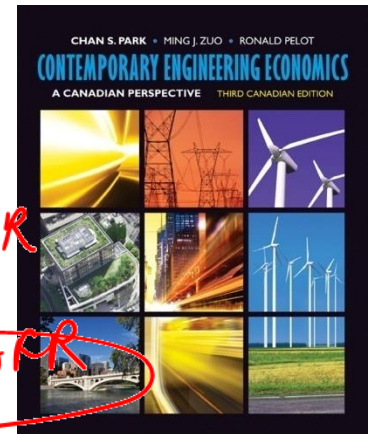
# Summary

Absolute  
Amount

{ PW  
AEW  
FW

IRR — MARR

{ IRRΔ — MARR



In **total investment analysis**, the PW of each mutually exclusive alternative is calculated separately, and the best choice is the one with the highest PW. In **incremental investment analysis**, the differences in cash flows between pairs of mutually exclusive alternatives are used as the basis for analysis.