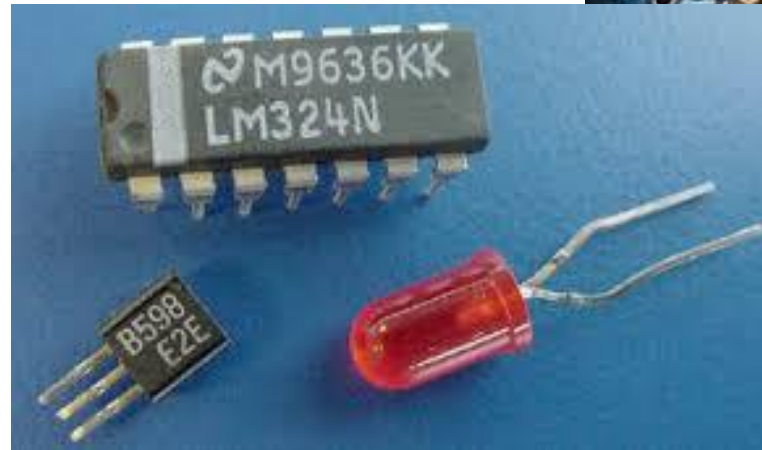


Electronic Materials

What are they?

Materials that conduct electricity

Used in electrical industries, electronics and microelectronics, and the substances for the building up of integrated circuits, circuit boards, packaging materials, communication cables, optical fibres, displays, and various controlling and monitoring devices.



Ohm's Law

$$V = IR$$

Where V is the voltage (volts, V), I is the current (amperes or amps, A), and R is the resistance (ohms).

$$R = \rho \frac{l}{A} = \frac{l}{\sigma A}$$

where l is the length (cm) of the resistor, A is the cross-sectional area (cm²) of the resistor, ρ is the electrical resistivity (ohm.cm), and σ , which is the reciprocal of ρ , is the electrical conductivity (ohm⁻¹ cm⁻¹).

Metals: High conductivity

Insulators: Low Conductivity

Semiconductors: Conductivity can be varied by several orders of magnitude.

Using Ohm's law

$$P = IV = I^2R$$

The electrical power **P** (in watts, W) lost when a current flows through a resistance.

$$J = \frac{I}{A} = \sigma \frac{V}{l} = \sigma E = nq\upsilon$$

$$\mu = \frac{\upsilon}{E} = \frac{\sigma}{nq}$$

J: Current density(A/cm²)

E: Electric field (V/cm)

n: number of charge carriers (carriers/cm³)

q: charge on each carrier (1.6×10⁻¹⁹ C)

υ:the average drift velocity (cm/s) at which the charge carriers move

μ: Mobility (cm² /V s)

Example

A voltage of 1700 V is applied to a gold wire 25 m in length. Calculate the diameter of wire and current density if the resistance is 3 ohm

Example

Design an electrical transmission line 1500 m long that will carry a current of 50 A with no more than 5×10^5 W loss in power.

Material	Conductivity ($\Omega^{-1} \text{m}^{-1}$)
Aluminum	3.5×10^7
Copper	6.0×10^7
Gold	4.1×10^7
Iron	1.0×10^7
Silver	6.2×10^7
Tungsten	1.8×10^7
Nichrome ^a	6.7×10^5
Carbon	2.9×10^4

Example

A current density of 5000 A/cm^2 is applied to a Aluminum wire. If half of the valence electrons serve as charge carriers, calculate the average drift velocity of the electrons

How does conductivity work?

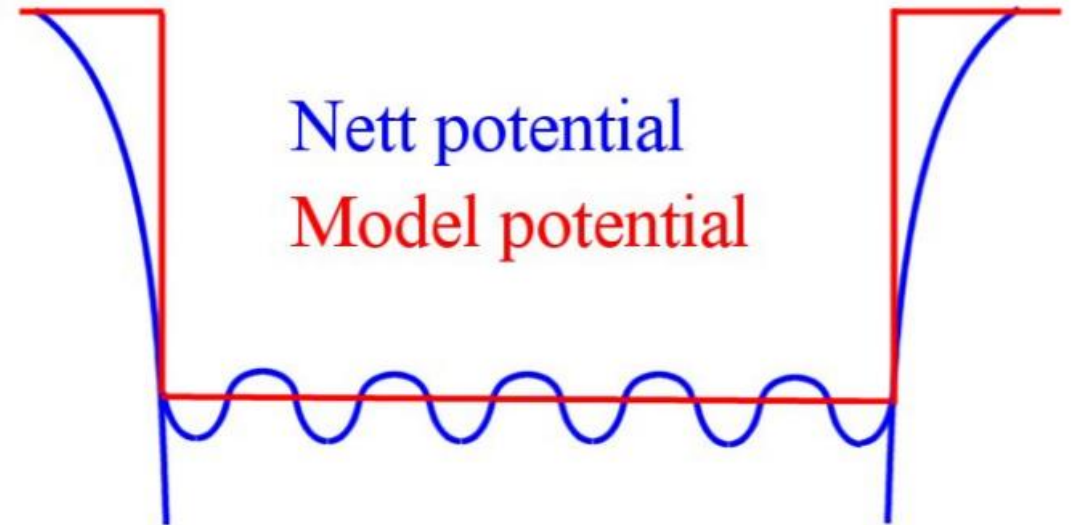
1. FREE ELECTRON MODEL

Assumptions: e⁻ are not interacting with each other

e⁻ respond equally to an external field

inner e⁻ are localized

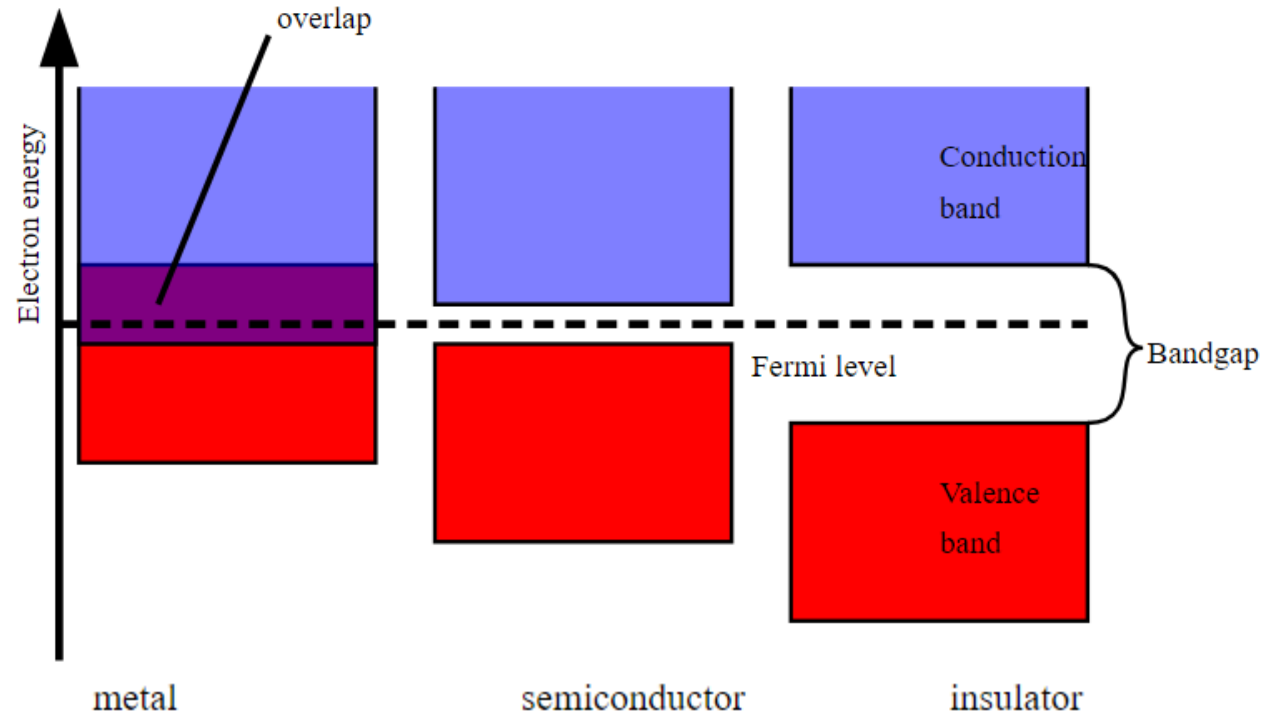
Constant potential



How does conductivity work?

2. BAND THEORY

Describes the conduction in terms of the energy to excite an e-



BAND THEORY

In order for e⁻ to jump from one band to another, the energy must accelerate the e⁻ enough to promote it to energy empty states.

Fermi Energy (E_f): Energy level at which only half of the energy levels in the band are filled at ABSOLUTE ZERO

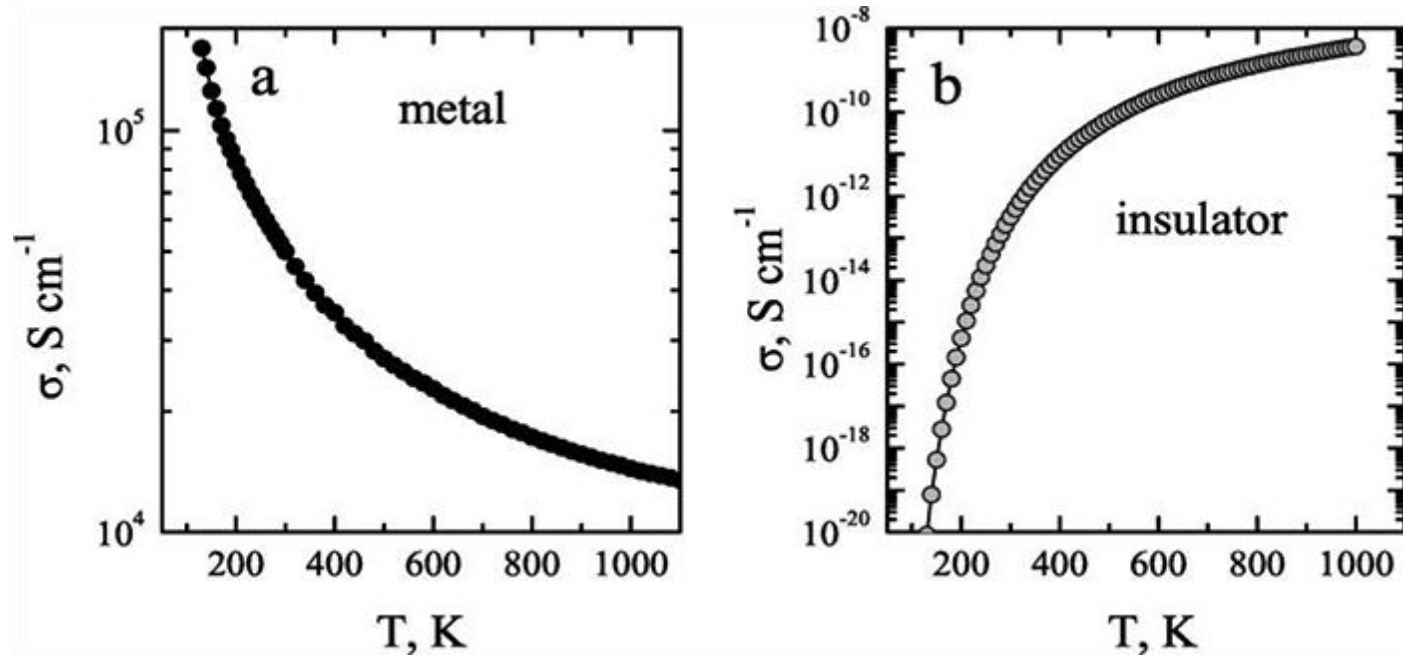
What happens with Non-metals? Due to covalent bonding the energy needed to excite an e⁻ will form a hybrid band between s and p levels.

Response to temperature

By the way

Siemens is a resistivity unit

$$S = \Omega^{-1}$$



Example

If all valence e- contribute to the current flow in Cu, calculate:

a) Mobility of e- and, b) average drift velocity of e- in 100cm long wire when 10V are applied

$$a_0 = 3.51 \times 10^{-8} \text{ cm}$$

FCC structure

$$\sigma = 5.98 \times 10^5 \text{ } \Omega^{-1} \text{ cm}^{-1}$$

Conductivity of Metals and Alloys

Conductivity is defined by the electronic structure of the material, if and only, the material is pure and defect-free.

$$\sigma = nq\mu$$

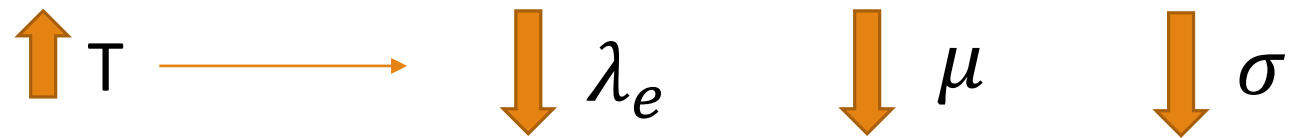
The paths of electrons are influenced internal fields due to the atoms present in the solid and imperfections present in the lattice.

$$\lambda_e = \tau v$$

λ_e : Mean free path

τ : Average time between collisions

Conductivity of Metals and Alloys: Temperature effect

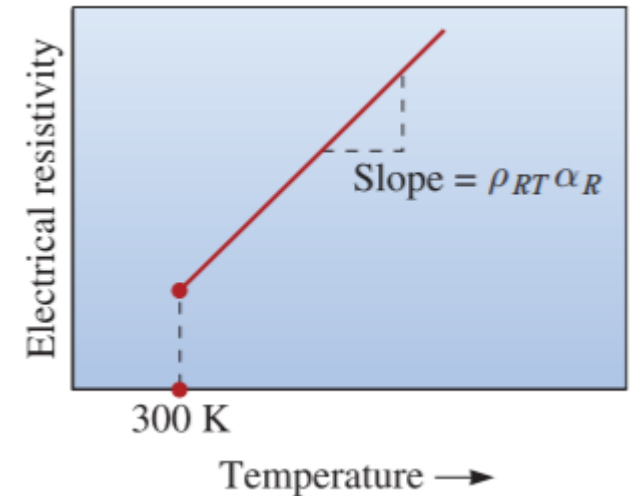


$$\frac{1}{\sigma} = \rho = \rho_{RT}(1 + \alpha_R(T - 25^\circ\text{C}))$$

ρ_{RT} : Resistivity at room temperature ($\Omega \cdot \text{cm}$)

α_R : Temperature resistivity coefficient ($\Omega / \Omega ^\circ\text{C}$)

T : New temperature ($^\circ\text{C}$)



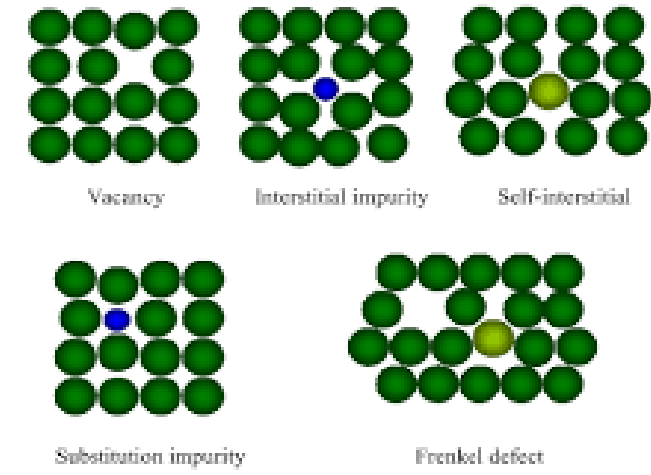
Example

After finding the electric conductivity of cobalt at 0 °C, we decide to double de conductivity. To what temperature must we cool the metal?

TABLE 19-3 ■ *The temperature resistivity coefficient α_R for selected metals*

Metal	Room Temperature Resistivity (ohm · cm)	Temperature Resistivity Coefficient (α_R) [ohm/(ohm · °C)]
Be	4.0×10^{-6}	0.0250
Mg	4.45×10^{-6}	0.0037
Ca	3.91×10^{-6}	0.0042
Al	2.65×10^{-6}	0.0043
Cr	12.90×10^{-6} (0°C)	0.0030
Fe	9.71×10^{-6}	0.0065
Co	6.24×10^{-6}	0.0053
Ni	6.84×10^{-6}	0.0069
Cu	1.67×10^{-6}	0.0043
Ag	1.59×10^{-6}	0.0041
Au	2.35×10^{-6}	0.0035
Pd	10.8×10^{-6}	0.0037
W	5.3×10^{-6} (27°C)	0.0045
Pt	9.85×10^{-6}	0.0039

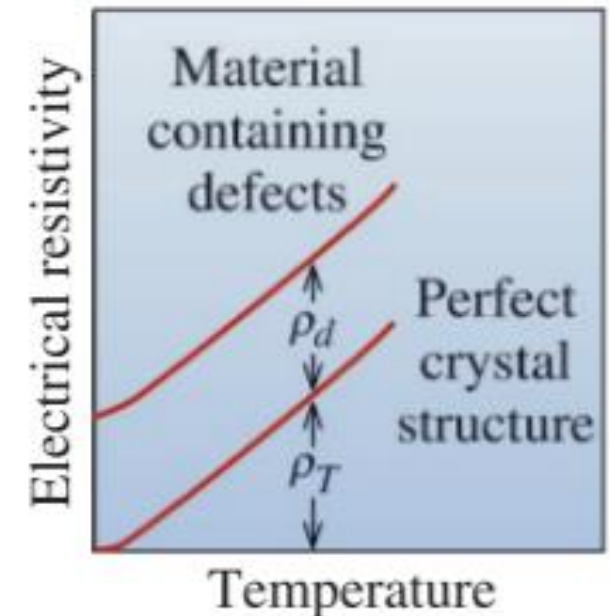
Conductivity of Metals and Alloys: Defects effect



$$\rho_d = bx(1 - x)$$

ρ_d : Resistivity due to defects ($\Omega \cdot \text{cm}$)
b: Defect resistivity coefficient ($\Omega \cdot \text{cm}$)
x: fraction of impurity

$$\rho = \rho_t + \rho_d$$



Semiconductors

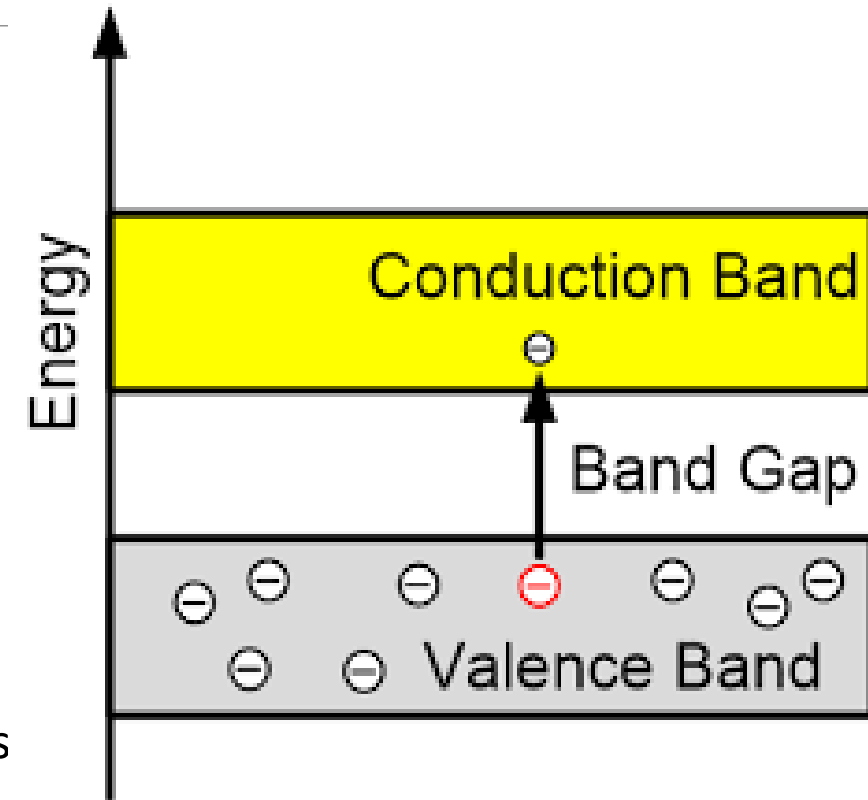
Any of a class of crystalline solids intermediate in electrical conductivity between a conductor and an insulator.

Key elements for the majority of electronic systems, serving communications, signal processing, computing, and control applications in both the consumer and industrial markets.

Energy gap (E_g) between the valence and conduction bands is relatively small.

Intrinsic semiconductors: Properties independent of the impurities.

Extrinsic semiconductors: Temperature stable and can be controlled by ion implantation or diffusion of impurities known as dopants.



Intrinsic semiconductors

For every electron promoted to the conduction band, there is a hole left in the valence band.

$$\sigma = n_i q (\mu_n + \mu_p)$$

n_i : Concentration of e-

μ_n : Mobility of e-

μ_p : Mobility of holes (h+)

$$\mu_n > \mu_p$$

Intrinsic semiconductors: Temperature effect

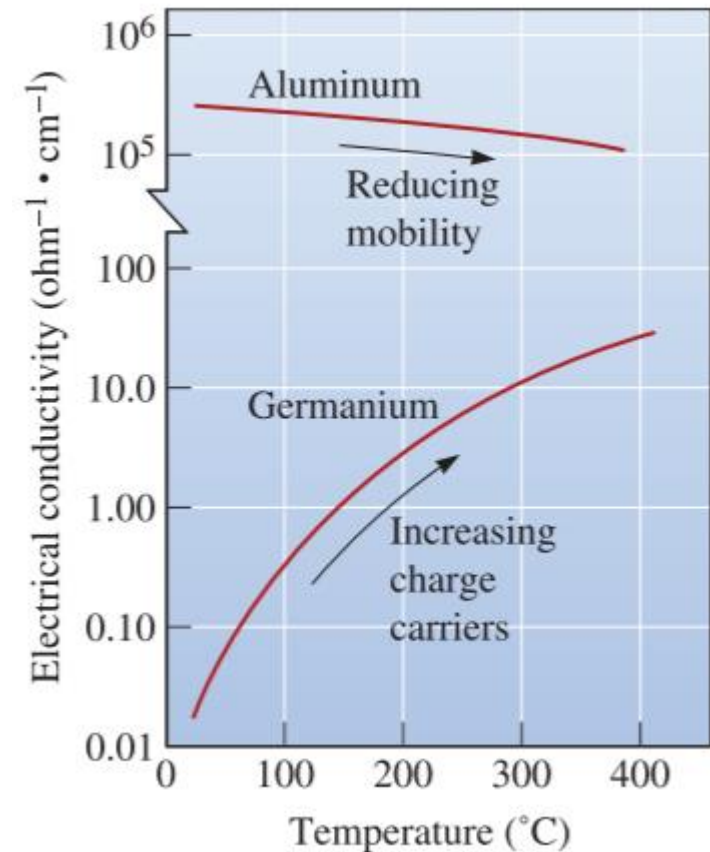
$$n_i = n_0 \exp\left(\frac{-E_g}{2k_B T}\right) \quad n_0 = 2 \left(\frac{2\pi k_B T}{h^2}\right)^{3/2} (m_n^* m_p^*)^{3/4}$$
$$\sigma = n_0 q (\mu_n + \mu_p) \exp\left(\frac{-E_g}{2k_B T}\right)$$

k_B : Boltzmann's constant ($1.38 \times 10^{-23} \text{ m}^2 \text{ kg s}^{-2} \text{ K}^{-1}$ or **$8.63 \times 10^{-5} \text{ eV/K}$**)

h : Planck's constant ($6.63 \times 10^{-34} \text{ m}^2 \text{ kg / s}$)

m_n^* : Effective mass of e-

m_p^* : Effective mass of h+



Example

For germanium and silicon, compare, at 25°C, the number of charge carriers per cubic centimeter, the fraction of the total # electrons in the valence band that are excited into the conduction band, and the constant n_0

TABLE 19-5 ■ *Properties of commonly encountered semiconductors at room temperature*

Semiconductor	Bandgap (eV)	Mobility of Electrons (μ_n) ($\frac{\text{cm}^2}{\text{V}\cdot\text{s}}$)	Mobility of Holes (μ_p) ($\frac{\text{cm}^2}{\text{V}\cdot\text{s}}$)	Dielectric Constant (k)	Resistivity ($\Omega \cdot \text{cm}$)	Density ($\frac{\text{g}}{\text{cm}^3}$)	Melting Temperature ($^\circ\text{C}$)
Silicon (Si)	1.11	1350	480	11.8	2.5×10^5	2.33	1415
Amorphous Silicon (a:Si:H)	1.70	1	10^{-2}	~ 11.8	10^{10}	~ 2.30	—
Germanium (Ge)	0.67	3900	1900	16.0	43	5.32	936
SiC (α)	2.86	500		10.2	10^{10}	3.21	2830
Gallium Arsenide (GaAs)	1.43	8500	400	13.2	4×10^8	5.31	1238
Diamond	~ 5.50	1800	1500	5.7	$> 10^{18}$	3.52	~ 3550

$$a_0(\text{Si}) = 5.43\text{E-}8 \text{ cm}$$

$$a_0(\text{Ge}) = 5.66\text{E-}8 \text{ cm}$$

Example

For germanium and silicon, compare, at 25°C, the number of charge carriers per cubic centimeter, the fraction of the total # electrons in the valence band that are excited into the conduction band, and the constant n_0

	Ge	Si
n (e-/cm ³)	2.51E13	1.37E10
n_t (e-/cm ³)	1.77E23	1.998E23
Fraction	1.42E-10	6.85E-14
n_0 (carriers/cm ³)	1.14E19	3.27E19

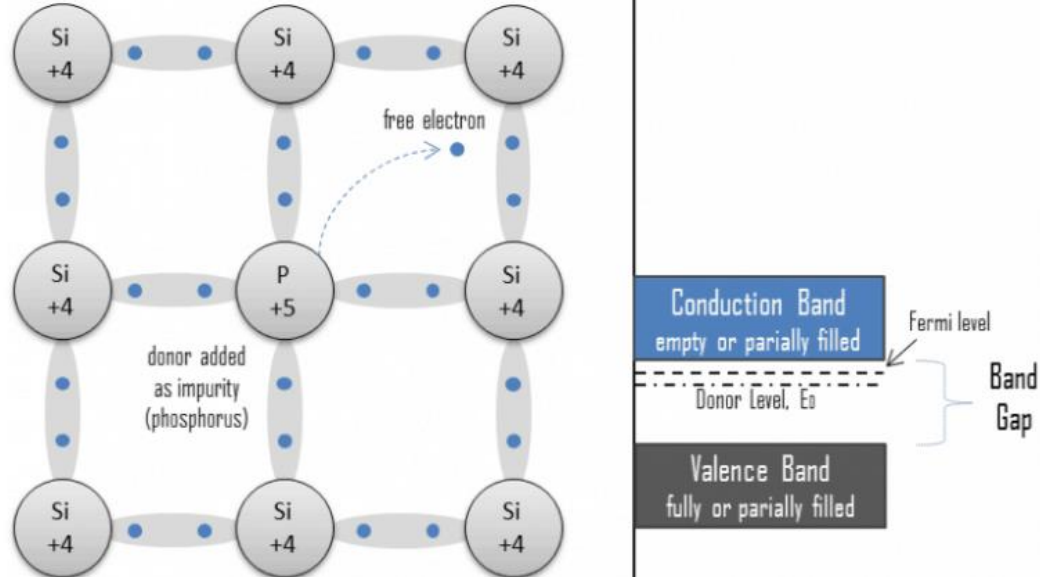
Extrinsic Semiconductors

Conductivity is based on the addition of impurities (Doping)

Conductivity can be independent of temperature

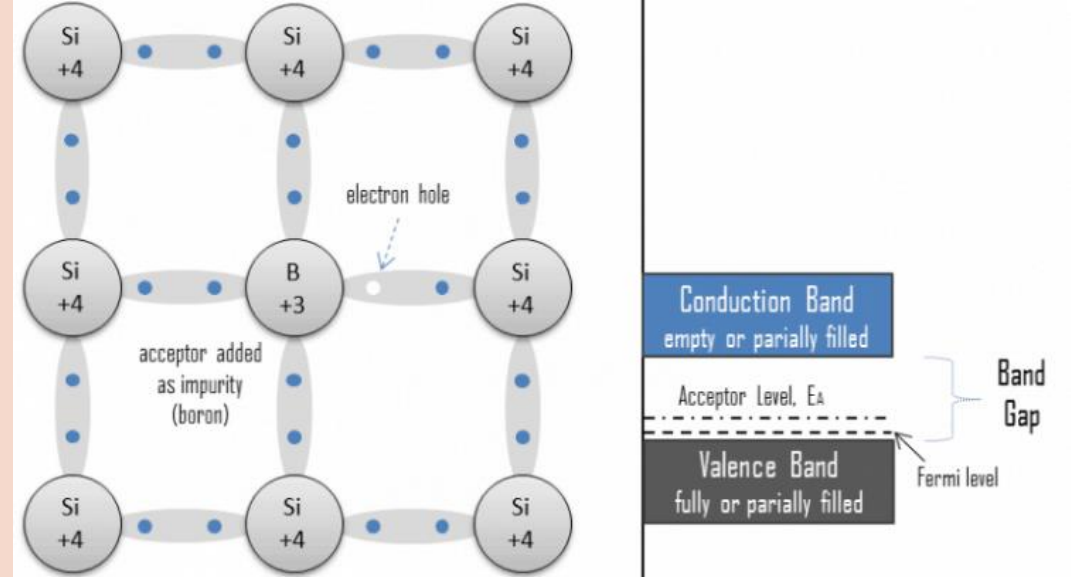
n-Type

Negative: Valence of dopant is greater than 4

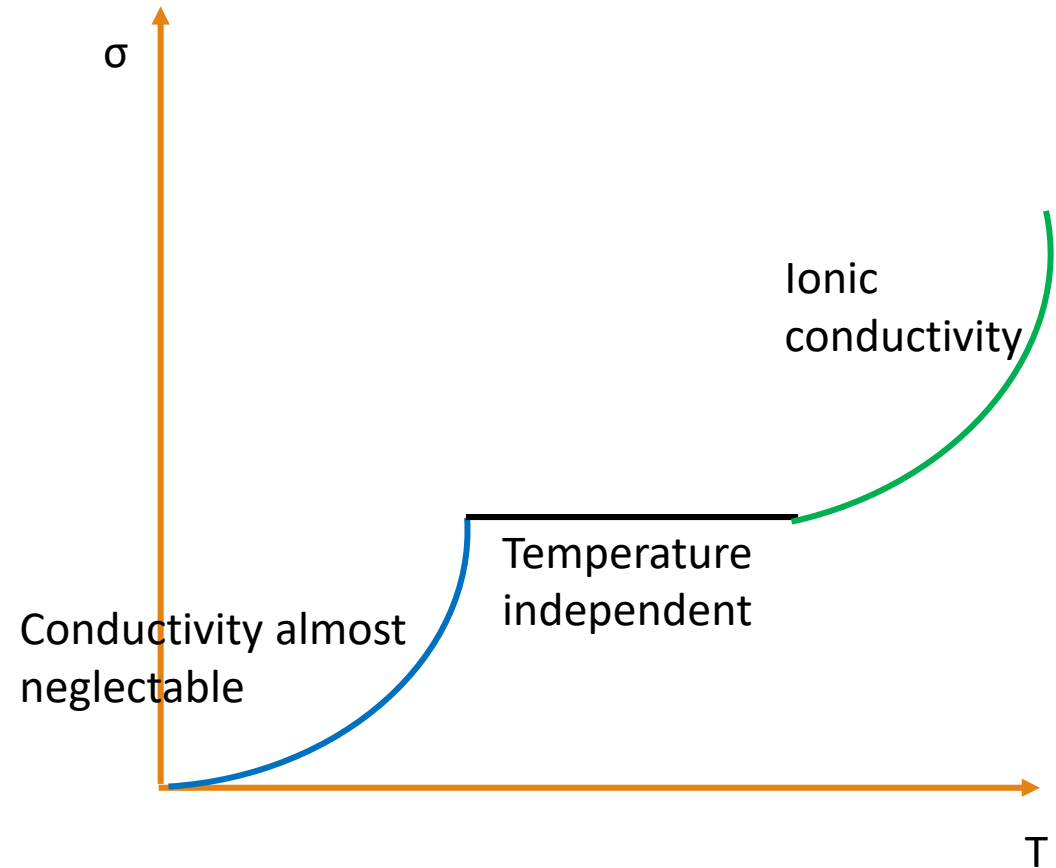
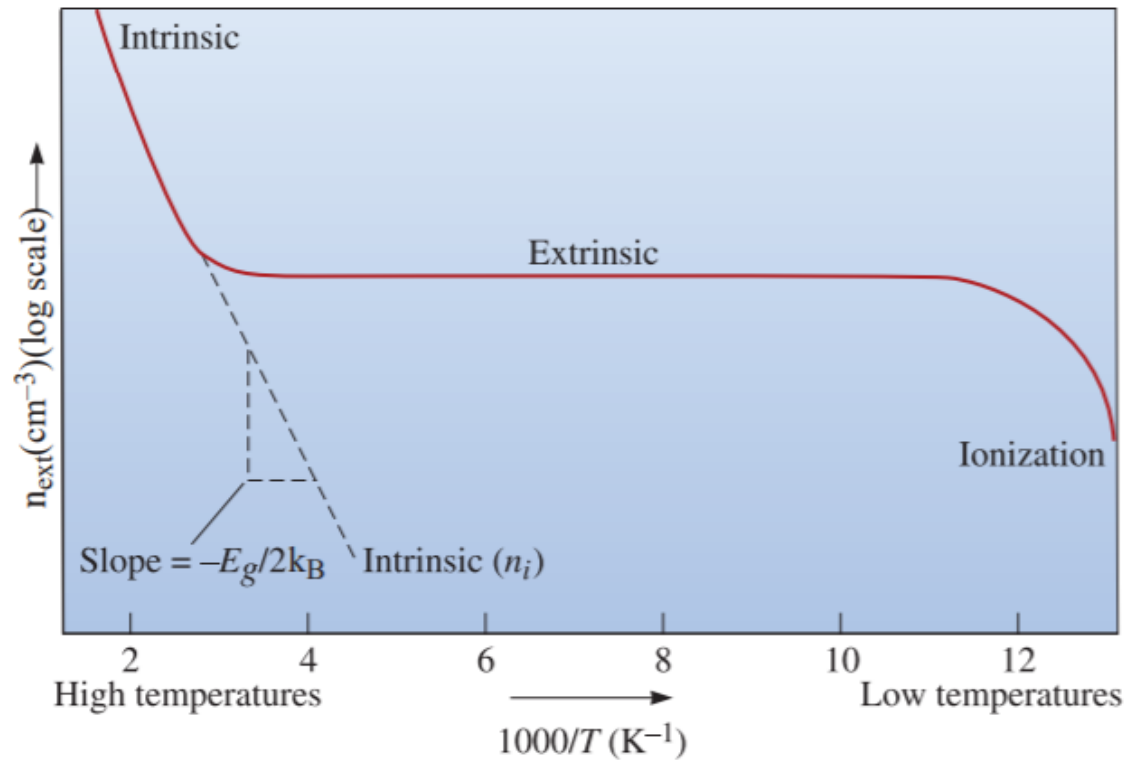


p-Type

Positive: Valence of dopant is less than 4



Extrinsic Semiconductors: Temperature dependence



Example

Determine the electrical conductivity of silicon when 0.0001at% Sb is added as a dopant. Compare it to the electrical conductivity when the same percentage of In is added.

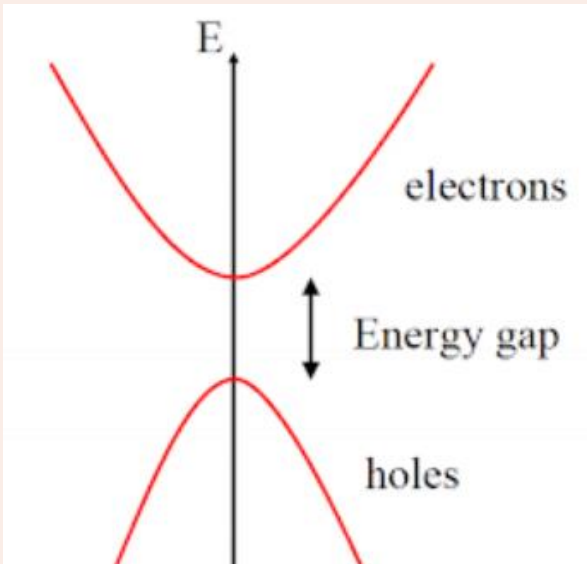
TABLE 19-6 ■ *The donor and acceptor energy levels (in electron volts) when silicon and germanium semiconductors are doped*

Dopant	Silicon		Germanium	
	E_d	E_a	E_d	E_a
P	0.045		0.0120	
As	0.049		0.0127	
Sb	0.039		0.0096	
B		0.045		0.0104
Al		0.057		0.0102
Ga		0.065		0.0108
In		0.160		0.0112

Bandgap Semiconductors

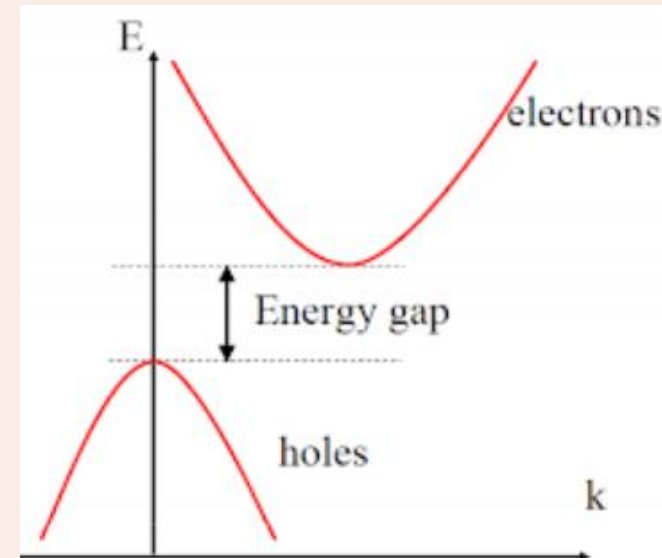
Direct (DBG) semiconductor

- The maximum energy level of the valence band aligns with the minimum energy level of the conduction band.
- The probability of a radiative recombination is high.
- DBG semiconductors are always preferred over IBG for making optical sources.
- Example, Gallium Arsenide (GaAs).

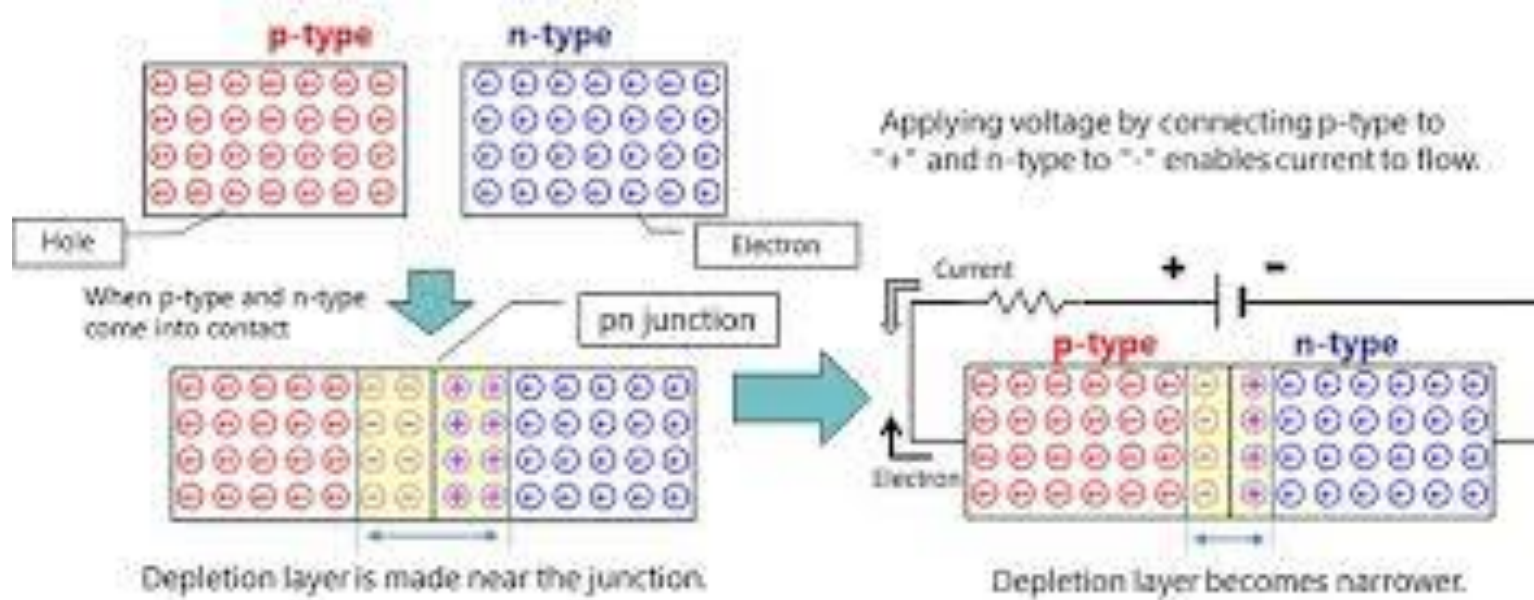


Indirect (IBG) semiconductor

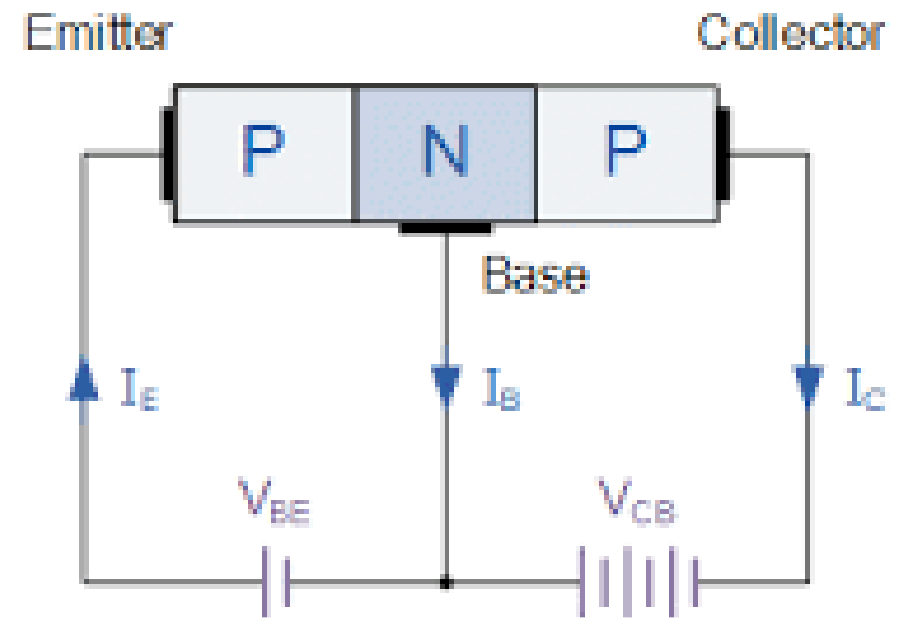
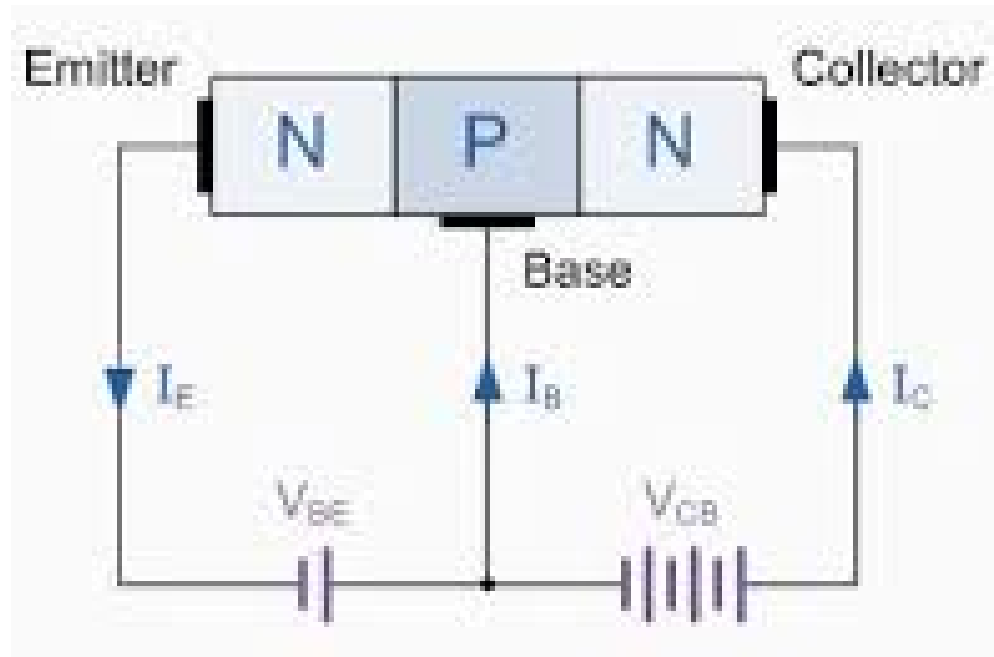
- The maximum energy level of the valence band and the minimum energy level of the conduction band are misaligned.
- Heat
- Example, Silicon and Germanium.



p-n Junction



Transistors



Conductivity in other materials: Polymers

- $10^{-8}, 10^{-12} \Omega^{-1} \text{ cm}^{-1}$

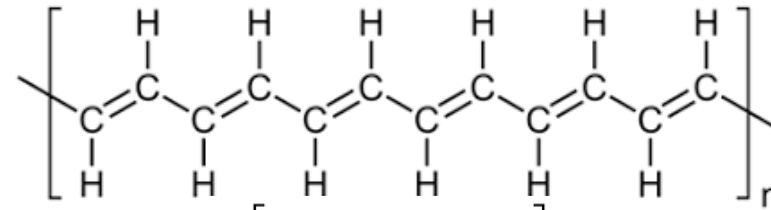
- Covalent bonds

+ **Composite materials:**

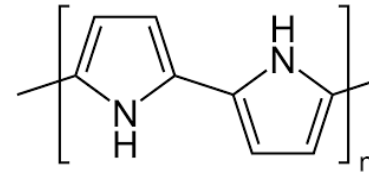
Powders

Coatings

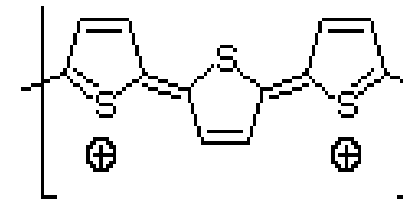
Polyacetylene



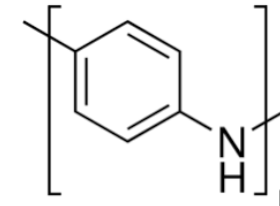
Polypyrrole



Polythiophene



Polyaniline



Dope with:

ClO_4^-

I_3

AsF_5

Conductivity in other materials: Ceramics

- Ionic material
- entire ions move, not just e-

$$\mu = \frac{zqD}{k_B T} \quad \sigma = n_i z q \mu$$

$$D = D_0 \exp\left(\frac{-Q}{RT}\right)$$

Z: valence of the ion

q: charge on each carrier (1.6×10^{-19} C)

D: diffusion coefficient

n_i: concentration of diffusing ions



Example

Suppose that the electrical conductivity of MgO is determined primarily by the diffusion of the Mg²⁺ ions. Estimate the mobility of the Mg²⁺ ions and calculate the electrical conductivity of MgO at 1500°C.

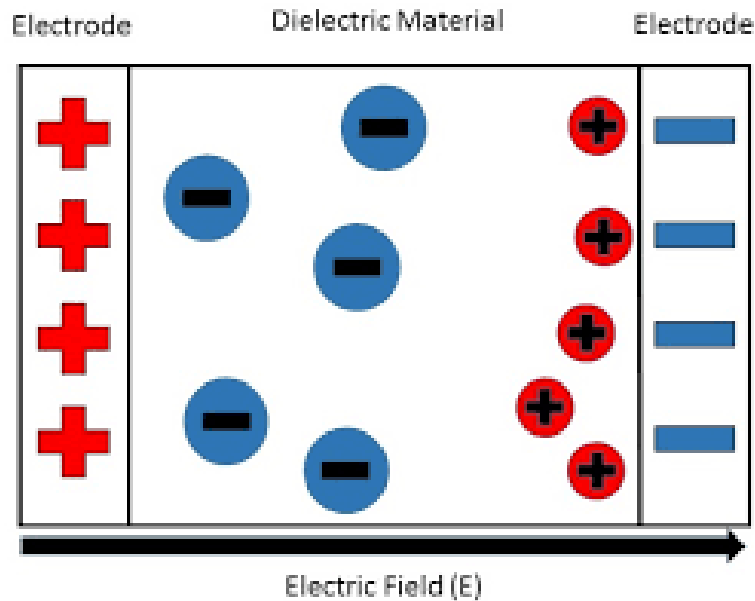
$$D_0 = 0.705 \cdot 10^{-13} \text{ [cm}^2 \text{ s}^{-1}\text{]}$$

$$Q = 1.25 \cdot 10^5 \text{ J}$$

$$a_0 = 3.96 \cdot 10^{-8} \text{ cm}$$

Dielectric and insulating materials: Polarization

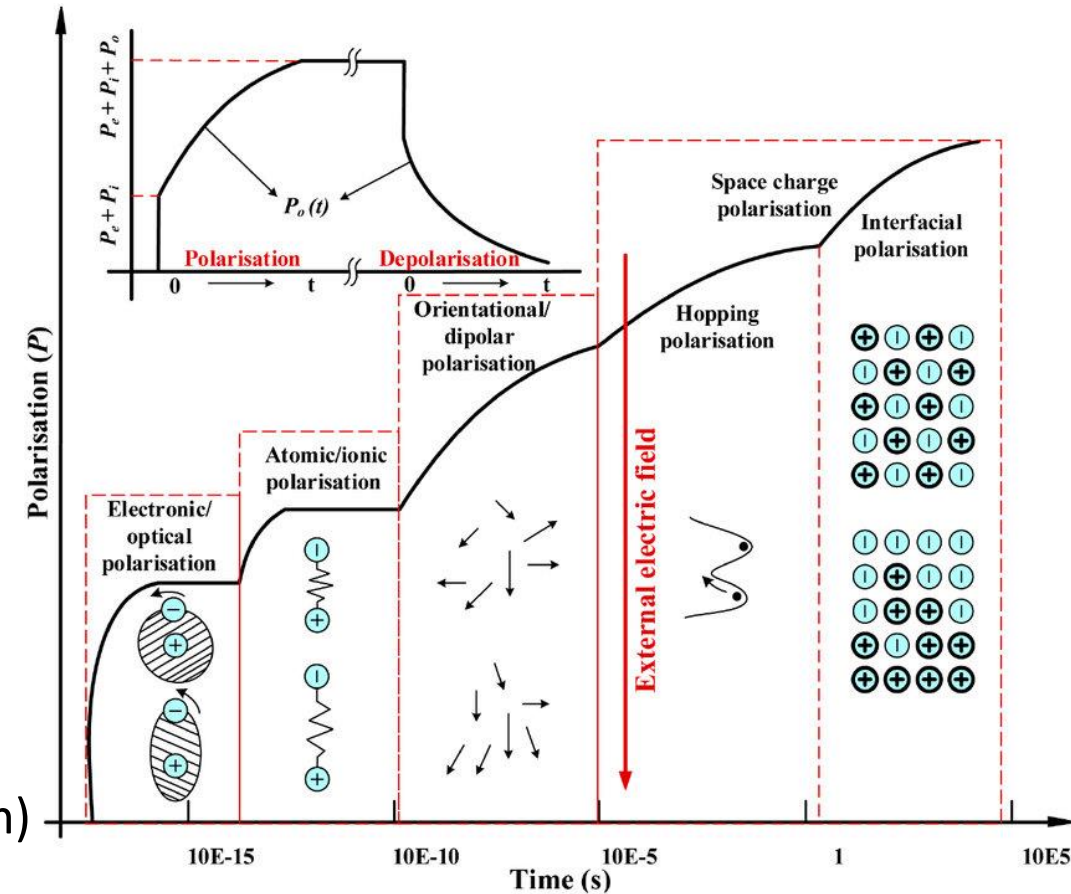
Charge separation!



$$U = qd$$

$$P = zqd$$

P: polarization
z: Number of charges
displaced per unit volume
d: average displacement (m)



Example

Calculate the displacement of e- if the polarization of Al is $2\text{E-}8 \text{ C m}^{-2}$

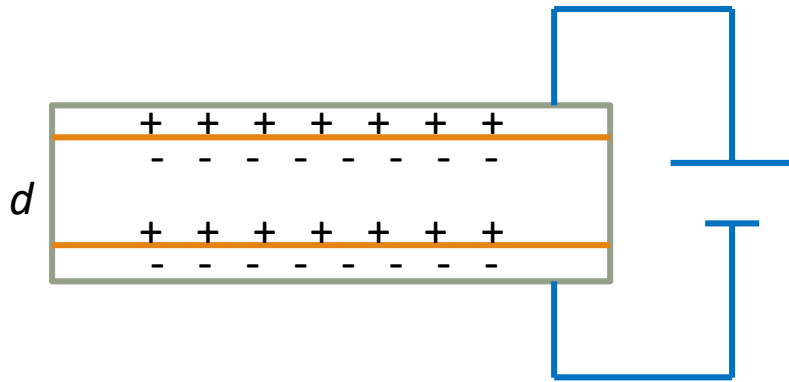
Atomic number: 13

a_0 : $4.04\text{E-}8 \text{ cm}$

FCC structure

Dielectric constant (k)

Also known as Relative permittivity



$$Q = CV \qquad k = \frac{\epsilon}{\epsilon_0}$$

$$C = \epsilon \frac{A}{d} \qquad C = k\epsilon_0 \frac{A}{d}$$

Q: Stored charge (C)

C: capacitance (Farad)

V: voltage (V)

ϵ_0 : Permittivity of vacuum (8.85E-12 F/m)

A: Surface area (m²)

d: average displacement (m)

ϵ : permittivity of material (F/m)

Example

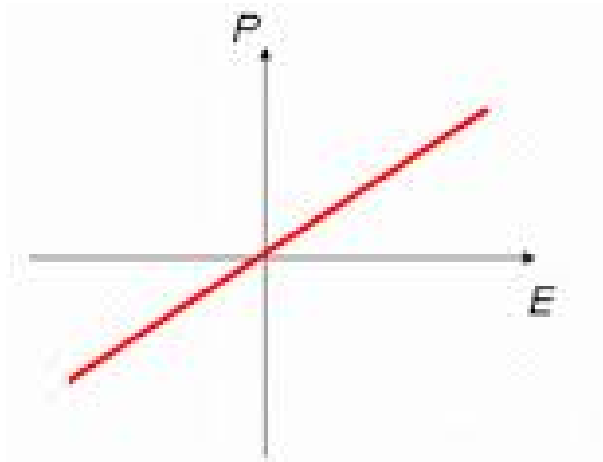
A simple parallel plate capacitor is designed to store 5×10^{-6} C at a potential of 8000 V. The distance between plates is 0.30 mm. Calculate the area of the plates if a) there is vacuum in between and b) alumina is the chosen dielectric material, if the permittivity of this material is 9 times the vacuum permittivity.

Linear and non-Linear dielectrics

Polarization only occurs when an electric field is applied

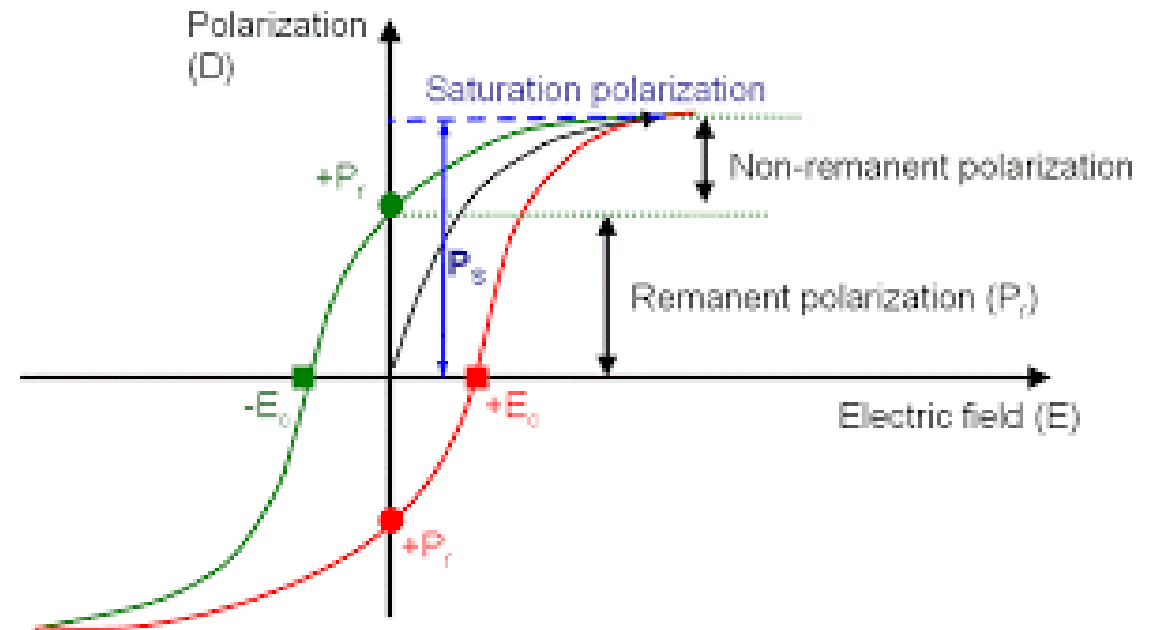
$$P = (k - 1)\epsilon_0 E \quad V = Ed$$

$\chi = (k - 1)$: Dielectric susceptibility



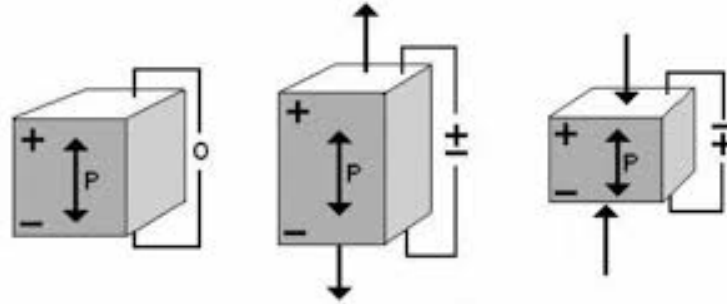
E: Electric field (V/m)

Polarization has a remnant even after the electric field is removed

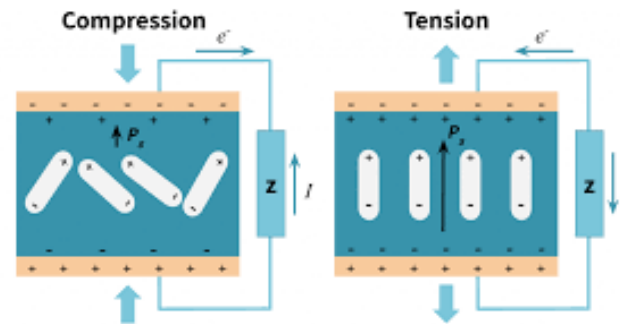


Non-Linear dielectrics

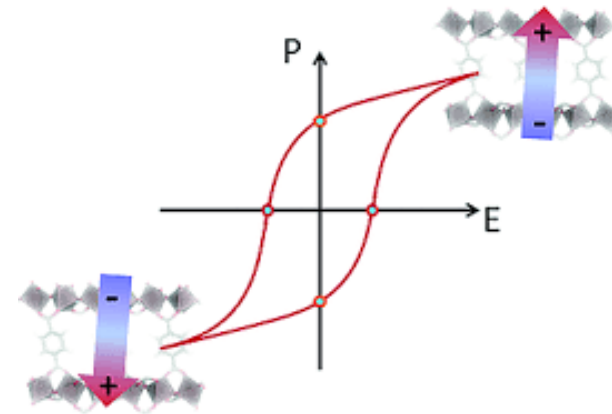
Electrostricticity: Dimensional change in the material when there is E .



Piezoelectricity: Application of stress on some materials can produce polarization



Ferroelectricity: Spontaneous and reversible dielectric polarization (P_s).



Example

A 2-mm-thick alumina dielectric is used in a 60 Hz circuit. Calculate the voltage required to produce a polarization of $5\text{E-}7 \text{ C/m}^2$

TABLE 19-7 ■ Properties of selected dielectric materials

Material	Dielectric Constant		Dielectric Strength (10^6 V/m)	$\tan \delta$ (at 10^6 Hz)	Resistivity (ohm · cm)
	(at 60 Hz)	(at 10^6 Hz)			
Polyethylene	2.3	2.3	20	0.00010	$> 10^{16}$
Teflon	2.1	2.1	20	0.00007	10^{18}
Polystyrene	2.5	2.5	20	0.00020	10^{18}
PVC	3.5	3.2	40	0.05000	10^{12}
Nylon	4.0	3.6	20	0.04000	10^{15}
Rubber	4.0	3.2	24		
Phenolic	7.0	4.9	12	0.05000	10^{12}
Epoxy	4.0	3.6	18		10^{15}
Paraffin wax		2.3	10		$10^{13}\text{--}10^{19}$
Fused silica	3.8	3.8	10	0.00004	$10^{11}\text{--}10^{12}$
Soda-lime glass	7.0	7.0	10	0.00900	10^{15}
Al ₂ O ₃	9.0	6.5	6	0.00100	$10^{11}\text{--}10^{13}$
TiO ₂		14–110	8	0.00020	$10^{13}\text{--}10^{18}$
Mica		7.0	40		10^{13}
BaTiO ₃		2000–5000	12	~0.0001	$10^8\text{--}10^{15}$
Water		78.3			10^{14}

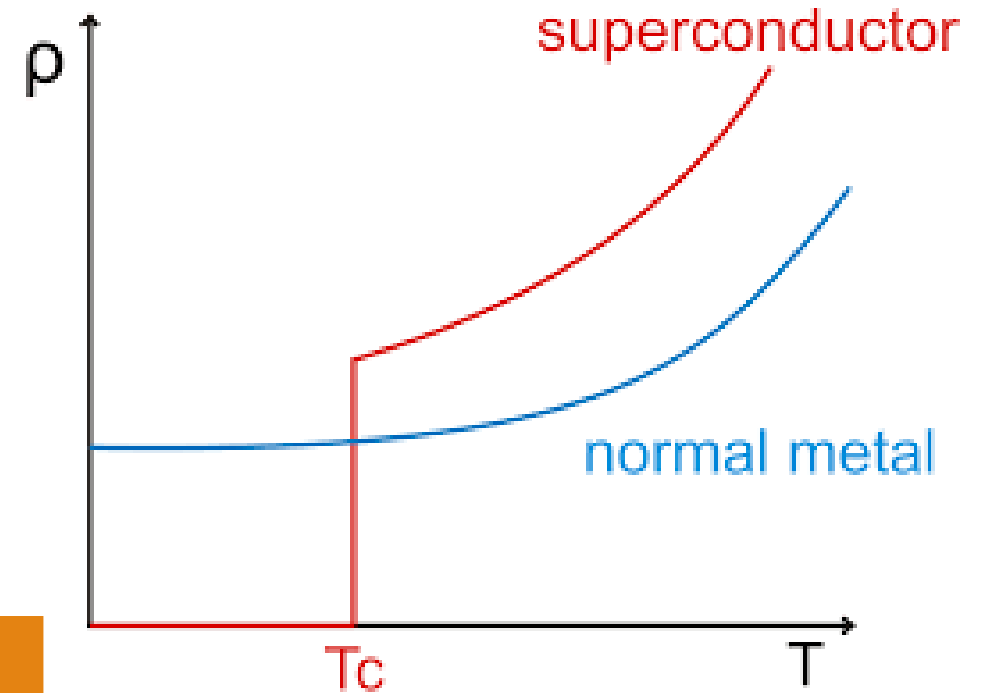
Superconductivity

Zero resistance

Temperature dependent

Meissner effect: Response of the superconductor to a magnetic field. A new opposing field.

Critical magnetic field: Magnitude of field needed to eliminate the superconductivity property of the material.



Type I	Type II
Ideal metals (most of them)	Intermetallic compounds
Completely expel magnetic field	Able to lose superconductivity

Example

The electrical resistivity of beryllium alloy containing 5at% of an alloying element is found to be $50 \times 10^{-6} \Omega \text{ cm}$ at 400°C .

Determine the contributions to resistivity due to temperature and due to impurities by finding the expected resistivity of pure beryllium at 400°C , the resistivity due to impurities, and the defect resistivity coefficient.

What would be the electrical resistivity if beryllium contained 10 at% of the same alloying element at 200°C ?

$$\rho_{\text{RT}}: 4 \times 10^{-6} \Omega \text{ cm}$$

$$\alpha_{\text{R}}: 0.025 \text{ } 1/^\circ\text{C}$$

Example

Design a capacitor that is capable of storing $1\text{ }\mu\text{F}$ when 1000 V is applied, producing an electric field of 250 V/m and the distance between plates is a fifth of the side of a plate.