Text Justification

You are given a sequence of words, and a limit on the number of characters that can be put in one line (i.e., the line width). Put line breaks in the given sequence such that the lines are printed neatly. Assume that the length of each word is smaller than the line width.

Input: Given array of n + 1 words w[0:n].

Measure of badness (ugliness): Suppose we are considering a line ℓ containing the words w[i] through w[j]. Define the badness(ℓ) for the line of words $\ell := w[i:j+1]$ to be:

$$\mathit{badness}(\ell) = \left\{ \begin{array}{ll} (\mathsf{page\text{-}width} - \mathsf{total\text{-}length}(\ell))^3, & \mathsf{if} \; \mathsf{total\text{-}length}(\ell) \leq \mathsf{page\text{-}width} \; ; \\ +\infty, & \mathsf{otherwise} \; . \end{array} \right.$$

Goal: Split words into lines $\ell_1 = w[0:i_1], \ell_2 = w[i_1:i_2],$ etc. to minimize $\sum_{\ell} badness(\ell)$.

Question 1: Write a dynamic programming algorithm to solve this problem. You should first define the subproblems and recursive relation.

