

Recall the simple insertion method into a binary search tree that inserts the key  $k$  into the tree:

1. If the tree is empty, create the root and set its key to be equal to  $k$
2. Otherwise, find the insertion point by following the path from the root to a leaf where at each node  $n$ , the left child is taken if  $k < n.key$ , otherwise the right child is taken. The insertion point is the last node  $n$  which doesn't have the appropriate child.
3. Insert a new node as a left child of the insertion point  $n$  if  $k < n.key$ , otherwise as a right child.

Recall the simple method to remove key  $k$ :

1. Find the node  $n$  that holds the key  $k$ .
2. If there is no left child of  $n$ , replace  $n$  with its right child (may be nothing).
3. Otherwise, find the node  $m$  with the maximum key in the subtree rooted at  $n.left$ . Move  $m.key$  to  $n.key$ . Then remove  $m$  and replace it with its left child (may be nothing).

### **Problems**

1. Draw the binary search tree resulting from inserting the keys 49, 79, 44, 41, 64, 80, 48 into the empty tree in this order with the simple insertion method. Let  $T$  be the resulting tree.

The items being stored with the keys are not relevant for this exercise, just show the keys.

2. Give the range of numbers that can could insert  $T$  as a left child of the node whose key is 48:
3. Give the range of numbers that can be inserted into  $T$  as a right child of the node whose key is 64:

5. What order could you insert keys 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 to get a BST with the following shape?

