

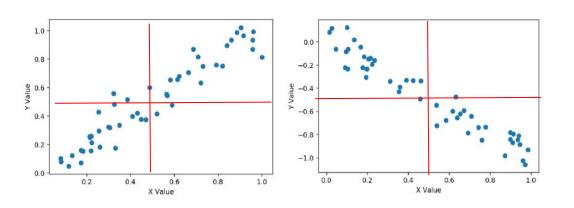
## Covariance

Cov(X,Y)= 
$$\frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{N}$$



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0.15 0.10 0.05 -0.05 -0.10 -0.15 -0.20 0.0 0.2 0.4 0.6 0.8 1.0

**Positive Covariance** 

**Negative Covariance** 

**Zero Covariance** 



$$Correlation = \frac{Cov(x,y)}{\sigma x * \sigma y}$$



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#### **Pearson Correlation:**

Covariance divided by the product of standard deviation of the two variables



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#### **Pearson Correlation:**

- Covariance divided by the product of standard deviation of the two variables
- Value between +1 and -1



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#### **Pearson Correlation:**

- Covariance divided by the product of standard deviation of the two variables
- Value between +1 and -1
- Strength of Linear Relationship



$$r_{xy} = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2 \sum (y_i - \overline{y})^2}}$$

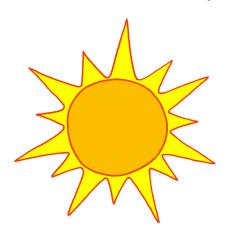
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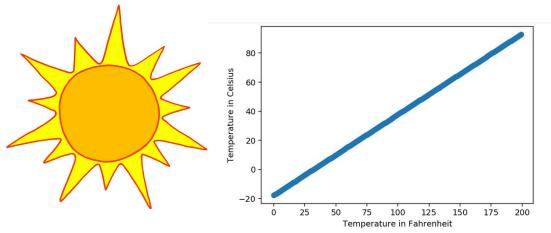
Ex. Relation between Temperature in Celsius and Fahrenheit.





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Ex. Relation between Temperature in Celsius and Fahrenheit.



Pearson Correlation = 1.0



$$r_{xy} = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2 \sum (y_i - \overline{y})^2}}$$

Ex. Relation between Temperature in Celsius and Fahrenheit.

$$F = \frac{9}{5}C + 32$$

$$\int_{\text{Temperature in Fabrenheit}}^{80} C + 32$$

Pearson Correlation = 1.0



$$r_{xy} = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2 \sum (y_i - \bar{y})^2}}$$

Ex. Relation between Distance travelled and Fuel remained?

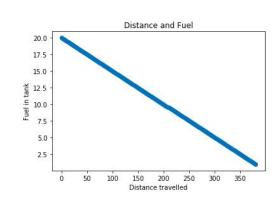




$$r_{xy} = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2 \sum (y_i - \overline{y})^2}}$$

#### Ex. Relation between Distance travelled and Fuel remained?





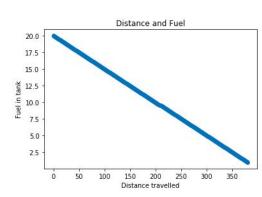
Pearson Correlation = -1.0



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Ex. Relation between Distance travelled and Fuel remained?





Pearson Correlation = -1.0

Fuel\_remained = Fuel\_Initial - Mileage \* Distance



$$r_{xy} = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2 \sum (y_i - \overline{y})^2}}$$

Ex. Relation between Height and IQ Score?

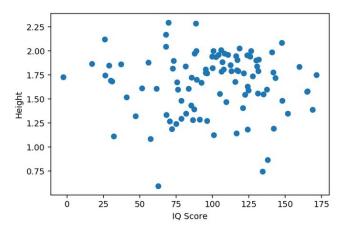




$$r_{xy} = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2 \sum (y_i - \overline{y})^2}}$$

#### Ex. Relation between Height and IQ Score?





Pearson Correlation = 0



Rain and Umbrella Sell



Employee investing hour in work and Paycheck



**Exercise and Muscle Power** 





Age and Hair



More time in mall and account balance



Crime and Tourism





# Thank You!

