

## RSA Public-Key Encryption and Signature Lab

### Task 1: Deriving the Private Key

Let  $p$ ,  $q$ , and  $e$  be three prime numbers. Let  $n = p \cdot q$ . We will use  $(e, n)$  as the public key. Please calculate the private key  $d$ . The hexadecimal values of  $p$ ,  $q$ , and  $e$  are listed in the following. It should be noted that although  $p$  and  $q$  used in this task are quite large numbers, they are not large enough to be secure. We intentionally make them small for the sake of simplicity. In practice, these numbers should be at least 512 bits long (the one used here are only 128 bits).

```
p = F7E75FDC469067FFDC4E847C51F452DF
q = E85CED54AF57E53E092113E62F436F4F
e = 0D88C3
```

```
[10/14/23]seed@VM:~/.../lab8-RSA$ gedit task1.c
^Z
[1]+  Stopped                  gedit task1.c
[10/14/23]seed@VM:~/.../lab8-RSA$ gcc task1.c -o task1 -l crypto
[10/14/23]seed@VM:~/.../lab8-RSA$ ./task1
d= 3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB
[10/14/23]seed@VM:~/.../lab8-RSA$ █
```

**d= 3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB**

#### working Code explanation :

- We have three prime numbers:  $p$ ,  $q$ , and  $e$ .
- We want to calculate the private key 'd' using these primes.
- The public key is represented as  $(e, n)$ , where  $n$  is the product of  $p$  and  $q$  ( $n = p \cdot q$ ).

In the main method:

- Create a `BN_CTX` structure to hold temporary `BIGNUM` variables used by library functions.
- Initialize `BIGNUM` variables:  $p$ ,  $q$ ,  $e$ ,  $d$ ,  $res1$ ,  $res2$ ,  $res3$ , and one.

For example:

- Create a `BIGNUM` structure for  $p$ ,  $q$ ,  $e$ ,  $d$ ,  $res1$ ,  $res2$ ,  $res3$ , and one.

Compute the following values:

- $\text{res1} = p - 1$
- $\text{res2} = q - 1$
- $\text{res3} = \text{res1} * \text{res2}$

Finally:

Calculate 'd' by finding the modular inverse of 'e' with respect to 'res3', ensuring that  $d * e \bmod \text{res3} = 1$ .

$\text{res3} = 1$ .

This code will provide the value of 'd', which is the private key.

**d= 3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB**

Above mentioned is the D value which we need

### Task - 1 Code :

```
Open [icon] *task1.c
~/Desktop/Seedlab/lab8-RSA

1#include <stdio.h>
2#include <openssl/bn.h>
3#define NBITS 256
4void printBN(char *msg, BIGNUM *a){
5// Convert the BIGNUM to number string lol #Arvind's
6char * number_str = BN_bn2hex(a);
7// Print out the number string
8printf("%s %s\n", msg, number_str);
9// Free the dynamically allocated memory
10OPENSSL_free(number_str);
11}
12int main(){
13BN_CTX *ctx = BN_CTX_new();
14BIGNUM *p = BN_new();
15BIGNUM *q = BN_new();
16BIGNUM *e = BN_new();
17BIGNUM *d = BN_new();
18BIGNUM *res1 = BN_new();
19BIGNUM *res2 = BN_new();
20BIGNUM *res3 = BN_new();
21BIGNUM *one = BN_new();
22// here we are goint to initialize p q e lol other wise we will not get output
23BN_hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF"); // Assign the first large prime
24BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F"); // Assign the second large prime
25BN_hex2bn(&e, "0D88C3"); // Assign the Modulus
26BN_dec2bn(&one, "1");
27//res1 = p-1
28BN_sub(res1, p, one); //res2 = q-1
29BN_sub(res2, q, one); //res3=res1*res2
30BN_mul(res3, res1, res2, ctx); //res=a*b mod n
31BN_mod_inverse(d, e, res3, ctx);
32//print BN
33printBN("d= ",d);
34return 0;
35}
36// completed task 1 code
```

## Task 2: Encrypting a Message

The public keys are listed in the followings (hexadecimal). We also provide the private key  $d$  to help you verify your encryption result.

```
n = DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5
e = 010001 (this hex value equals to decimal 65537)
M = A top secret!
d = 74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D
```

### Code explanation :

We are importing libraries

```
1 #include <stdio.h>
2 #include <openssl/bn.h>
3 #define NBITS 256
```

To print the result

```
4 //To print a big number
5 void printBN(char *msg, BIGNUM *a){
6 // Convert the BIGNUM to number string
7 char * number_str = BN_bn2hex(a);
8 // Print out the number string
9 printf("%s %s\n", msg, number_str);
10 // Free the dynamically allocated memory
11 OPENSSL_free(number_str);
12 }
```

To initialize values and encrypt the message

```
13 int main(){
14     BN_CTX *ctx = BN_CTX_new();
15     BIGNUM *m = BN_new();
16     BIGNUM *e = BN_new();
17     BIGNUM *n = BN_new();
18     BIGNUM *d = BN_new();
19     BIGNUM *enc = BN_new();
20     BIGNUM *dec = BN_new();
21     //Initialize
22     BN_hex2bn(&e,"010001"); //values given in the pdf description
23     BN_hex2bn(&n,"DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
24     BN_hex2bn(&m,"4120746f702073656372657421"); //A top secret! code
25     BN_hex2bn(&d,"74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
26     //decry = e^d mod n
27     BN_mod_exp(enc,m,e,n,ctx);
28     printBN("encrypt message = ", enc);
```

To decrypt the message.

```
29 //decry = enc^d mod n
30 BN_mod_exp(dec,enc,d,n,ctx);
31 printBN("The decrypt message = ",dec);
32 return 0;
33 }
34 //boom! task2 completed successfully.
35
```

Full code :

```
Open [icon] *Task2.c
~/Desktop/Seedlab/lab8-RSA
1#include <stdio.h>
2#include <openssl/bn.h>
3#define NBITS 256
4//To print a big number
5void printBN(char *msg, BIGNUM *a){
6// Convert the BIGNUM to number string
7char * number_str = BN_bn2hex(a);
8// Print out the number string
9printf("%s %s\n", msg, number_str);
10// Free the dynamically allocated memory
11OPENSSL_free(number_str);
12}
13int main(){
14    BN_CTX *ctx = BN_CTX_new();
15    BIGNUM *m = BN_new();
16    BIGNUM *e = BN_new();
17    BIGNUM *n = BN_new();
18    BIGNUM *d = BN_new();
19    BIGNUM *enc = BN_new();
20    BIGNUM *dec = BN_new();
21    //Initialize
22    BN_hex2bn(&e,"010001"); //values given in the pdf description
23    BN_hex2bn(&n,"DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
24    BN_hex2bn(&m,"4120746f702073656372657421");//A top secret! code
25    BN_hex2bn(&d,"74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
26    //encry = m^e mod n
27    BN_mod_exp(enc,m,e,n,ctx);
28    printBN("encrypt message = ", enc);
29    //decry = enc^d mod n
30    BN_mod_exp(dec,enc,d,n,ctx);
31    printBN("The decrypt message = ",dec);
32    return 0;
33}
34//boom! task2 completed successfully.
35
```

```
[10/14/23]seed@VM:~/.../lab8-RSA$ gedit Task2.c
^Z
[1]+  Stopped                  gedit Task2.c
[10/14/23]seed@VM:~/.../lab8-RSA$ gcc Task2.c -o Task2 -l crypto
[10/14/23]seed@VM:~/.../lab8-RSA$ ./Task2
encrypt message = 6FB078DA550B2650832661E14F4F8D2CFAEF475A0DF3A75CACDC5DE5CFC5FADC
The decrypt message = 4120746f702073656372657421
[10/14/23]seed@VM:~/.../lab8-RSA$ █
```

In the above snippet we can see the encrypt and decrypt message

----- Task 2 done -----

## Task 3: Decrypting a Message

The public/private keys used in this task are the same as the ones used in Task 2. Please decrypt the following ciphertext C, and convert it back to a plain ASCII string.

```
C = 8C0F971DF2F3672B28811407E2DABBE1DA0FEBBBBDFC7DCB67396567EA1E2493F
```

You can use the following python command to convert a hex string back to a plain ASCII string.

```
$ python -c 'print("4120746f702073656372657421".decode("hex"))'
A top secret!
```

The public and private keys employed in this task are identical to those utilized in Task 2. Our objective is to decrypt the provided ciphertext, C, and subsequently convert it back into a plain ASCII string. We achieve this decryption by applying the formula  $c^d \bmod n$ .

```
[10/14/23]seed@VM:~/.../Lab8-RSA$ echo "Task3"
Task3
[10/14/23]seed@VM:~/.../Lab8-RSA$ gcc task3.c -o task3 -l crypto
[10/14/23]seed@VM:~/.../Lab8-RSA$ ./task3
The encrypt message = 50617373776F72642069732064656573
[10/14/23]seed@VM:~/.../Lab8-RSA$ python -c 'print("A top secret!".decode("hex"))'
bash: syntax error near unexpected token `('
[10/14/23]seed@VM:~/.../Lab8-RSA$ python -c 'print("A top secret!".decode("hex"))'
bash: syntax error near unexpected token `('
[10/14/23]seed@VM:~/.../Lab8-RSA$ python -c ' print("A top secret!".decode("hex"))'
bash: syntax error near unexpected token `('
[10/14/23]seed@VM:~/.../Lab8-RSA$ python -c 'print("4120746f702073656372657421".decode("hex"))'
Command 'python' not found, did you mean:
  command 'python3' from deb python3
  command 'python' from deb python-is-python3
[10/14/23]seed@VM:~/.../Lab8-RSA$ python3 -c 'print("4120746f702073656372657421".decode("hex"))'
Traceback (most recent call last):
  File "<string>", line 1, in <module>
AttributeError: 'str' object has no attribute 'decode'
[10/14/23]seed@VM:~/.../Lab8-RSA$ python3 -c 'print(bytes.fromhex("4120746f702073656372657421").decode("utf-8"))'
A top secret!
[10/14/23]seed@VM:~/.../Lab8-RSA$
```

Initially, we named the file as **"task-3."** We proceeded to compile the C code, which is explained below. **Following the compilation process, we successfully obtained the desired values without encountering any errors**

Encrypted message also decrypted and below i have attached the screenshot

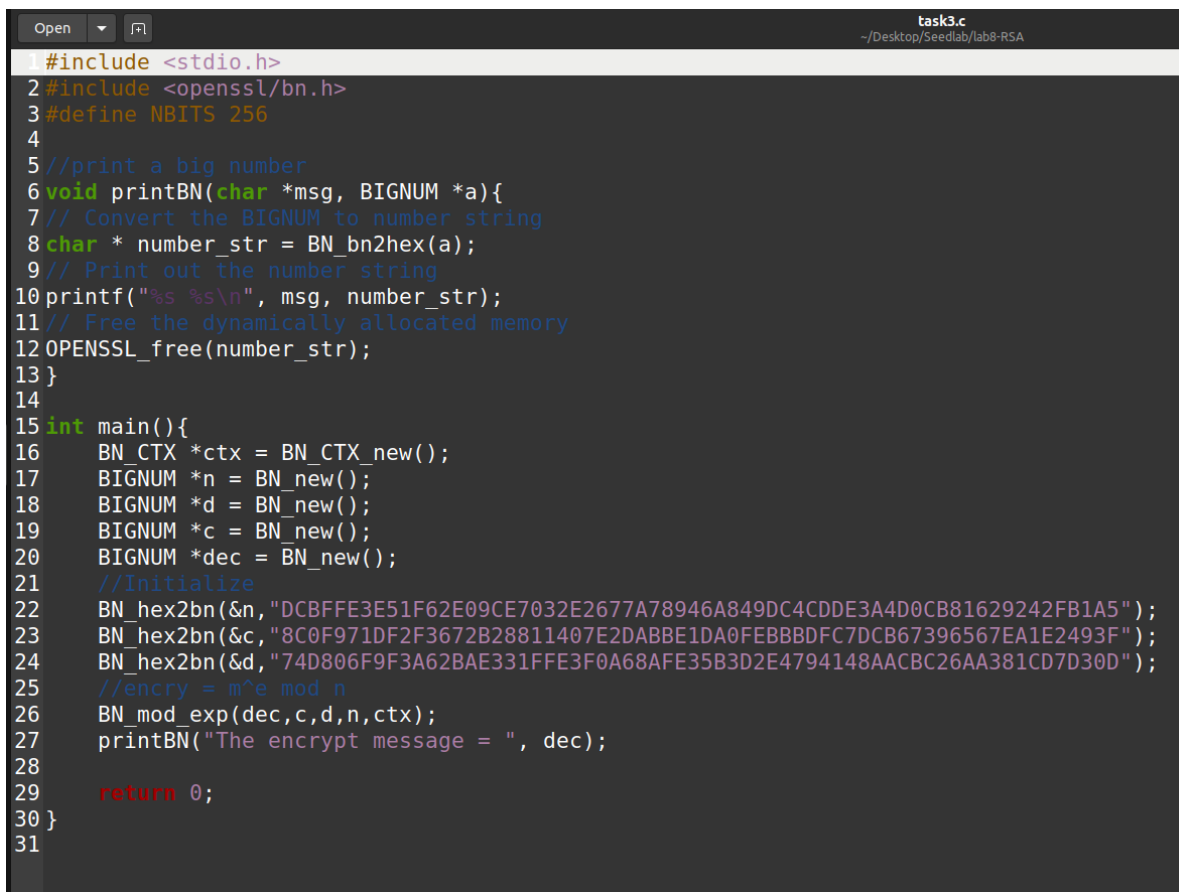
```
[10/14/23]seed@VM:~/.../Lab8-RSA$ python3 -c 'print(bytes.fromhex("50617373776F72642069732064656573").decode("utf-8"))'
Password is dees
```

You can use the following python command to convert a hex string back to a plain ASCII string.

```
$ python -c 'print("4120746f702073656372657421".decode("hex"))'
A top secret!
```

The next step involves using a Python command to convert a hex string back into a plain ASCII string. **However, it's important to note that the initial command provided may work only on older Linux versions**, and there were some issues encountered as shown in the previous screenshots. To resolve this, we made some modifications to the Python command, which you can observe in the error messages displayed in the above screenshots. After compiling the code that was written, it became evident that we can successfully obtain the plain ASCII string.

### Task 3 - Code :



```
1 #include <stdio.h>
2 #include <openssl/bn.h>
3 #define NBITS 256
4
5 //print a big number
6 void printBN(char *msg, BIGNUM *a){
7 // Convert the BIGNUM to number string
8 char * number_str = BN_bn2hex(a);
9 // Print out the number string
10 printf("%s %s\n", msg, number_str);
11 // Free the dynamically allocated memory
12 OPENSSL_free(number_str);
13 }
14
15 int main(){
16 BN_CTX *ctx = BN_CTX_new();
17 BIGNUM *n = BN_new();
18 BIGNUM *d = BN_new();
19 BIGNUM *c = BN_new();
20 BIGNUM *dec = BN_new();
21 //Initialize
22 BN_hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
23 BN_hex2bn(&c, "8C0F971DF2F3672B28811407E2DABBE1DA0FEBBBD7C7DCB67396567EA1E2493F");
24 BN_hex2bn(&d, "74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
25 //encry = m^e mod n
26 BN_mod_exp(dec, c, d, n, ctx);
27 printBN("The encrypt message = ", dec);
28
29 return 0;
30 }
31
```

Upon decryption, we obtain the hexadecimal representation of the message. **Subsequently, we utilize Python to decode this hex value, thereby restoring the original plain ASCII string.**

----- Task 3 completed -----

## Task 4: Signing a Message

The public/private keys used in this task are the same as the ones used in Task 2. Please generate a signature for the following message (please directly sign this message, instead of signing its hash value):

```
M = I owe you $2000.
```

Please make a slight change to the message M, such as changing \$2000 to \$3000, and sign the modified message. Compare both signatures and describe what you observe.

First, we should get the hex value of “I owe you \$2000.”

```
[10/14/23]seed@VM:~/.../lab8-RSA$ gedit task4.c
^Z
[1]+  Stopped                  gedit task4.c
[10/14/23]seed@VM:~/.../lab8-RSA$ python3 -c 'print(("I OWE YOU $2000").encode("hex"))'
Traceback (most recent call last):
  File "<string>", line 1, in <module>
LookupError: 'hex' is not a text encoding: use codecs.encode() to handle arbitrary codecs
[10/14/23]seed@VM:~/.../lab8-RSA$ python3 -c 'print(("I OWE YOU $2000").encode("utf-8").hex())'
49204f574520594f55202432303030
```

We can watch the value of i owe you in the above snap snippet .

The given python command **was not working in this version** so I modified and ran the new command as marked in the above screenshot.

We run our code to produce the **signature for the message for \$2000**

```
[10/14/23]seed@VM:~/.../lab8-RSA$ gedit task4.c
[10/14/23]seed@VM:~/.../lab8-RSA$ gcc task4.c -o task4 -l crypto
[10/14/23]seed@VM:~/.../lab8-RSA$ ./task4
encrypt message = 55A4E7F17F04CCFE2766E1EB32ADDBA890BBE92A6FBE2D785ED6E73CCB35E4CB
[10/14/23]seed@VM:~/.../lab8-RSA$
```

Second step is that we should get the hex value of “I owe you \$3000.” since mentioned in description.

```
[10/14/23]seed@VM:~/.../lab8-RSA$ echo "tsk4 after changing hexvalue"
tsk4 after changing hexvalue
[10/14/23]seed@VM:~/.../lab8-RSA$ python3 -c 'print(("I OWE YOU $3000").encode("utf-8").hex())'
49204f574520594f55202433303030
```

We run our code to produce the **signature for the message for \$3000:**

```
[10/14/23]seed@VM:~/.../lab8-RSA$ gcc task4.c -o task4 -l crypto
[10/14/23]seed@VM:~/.../lab8-RSA$ ./task4
encrypt message = 7E3AE53979186F5CDB08BD2DD0385F5069AD564580C3F31C8165F916DF441F4B2
[10/14/23]seed@VM:~/.../lab8-RSA$ █
```

## Code :

```
Open [v] [f] *task4.c
~/Desktop/Seedlab/lab8-RSA
1 #include <stdio.h>
2 #include <openssl/bn.h>
3 #define NBITS 256
4
5 //print a big number
6 void printBN(char *msg, BIGNUM *a){
7 // Convert the BIGNUM to number string
8 char * number_str = BN_bn2hex(a);
9 // Print out the number string
10 printf("%s %s\n", msg, number_str);
11 // Free the dynamically allocated memory
12 OPENSSL_free(number_str);
13 }
14
15 int main(){
16     BN_CTX *ctx = BN_CTX_new();
17     BIGNUM *n = BN_new();
18     BIGNUM *d = BN_new();
19     BIGNUM *c = BN_new();
20     BIGNUM *dec = BN_new();
21     //Initialize
22     BN_hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
23     BN_hex2bn(&c, "49204f574520594f55202432303030"); // HEX value of "I owe you $2000."
24     BN_hex2bn(&d, "49204f574520594f55202433303030"); // HEX value of "I owe you $3000."
25     BN_hex2bn(&d, "74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
26     //encry = m^e mod n
27     BN_mod_exp(dec, c, d, n, ctx);
28     printBN("encrypt message = ", dec);
29
30     return 0;
31 }
```

The above is for both \$2000 and \$3000 when we run for \$2000 we will comment \$3000 and while running \$3000 we comment \$2000.

**Observation :** It is noticeable that despite a minimal one-byte difference in the messages, their respective signatures are entirely distinct.

----- Task 4 completed -----



## Task 5: Verifying a Signature

Bob receives a message  $M = \text{"Launch a missile."}$  from Alice, with her signature  $S$ . We know that Alice's public key is  $(e, n)$ . Please verify whether the signature is indeed Alice's or not. The public key and signature (hexadecimal) are listed in the following:

```
M = Launch a missile.
S = 643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6802F
e = 010001 (this hex value equals to decimal 65537)
n = AE1CD4DC432798D933779FBD46C6E1247F0CF1233595113AA51B450F18116115
```

Suppose that the signature above is corrupted, such that the last byte of the signature changes from 2F to 3F, i.e, there is only one bit of change. Please repeat this task, and describe what will happen to the verification process.

To begin, **we obtain the hexadecimal representation of the message "Launch a missile."** using Python.

```
[10/14/23]seed@VM:~/.../lab8-RSA$ echo "task5"
task5
[10/14/23]seed@VM:~/.../lab8-RSA$ python3 -c 'print(("Launch a missile").encode("utf-8").hex())'
4c61756e63682061206d697373696c65
[10/14/23]seed@VM:~/.../lab8-RSA$
```

We utilize the signature to calculate the value of the **message C**. Subsequently, we employ the BN\_cmp API to compare the two messages and determine if the signature belongs to Alice.

```
[10/14/23]seed@VM:~/.../lab8-RSA$ gcc task5.c -o task5 -l crypto
task5.c: In function 'main':
task5.c:25:13: error: expected ')' before string constant
   25 | BN_hex2bn(&s "643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6802F");
      |             ^
task5.c:25:1: error: too few arguments to function 'BN_hex2bn'
   25 | BN_hex2bn(&s "643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6802F");
      | ^~~~~~
In file included from task5.c:2:
/usr/local/include/openssl/bn.h:311:5: note: declared here
   311 | int BN_hex2bn(BIGNUM **a, const char *str);
      | ^~~~~~
task5.c:29:12: error: 'M' undeclared (first use in this function)
   29 | BN_mod_exp(M,S,e,n, ctx);
      |             ^
task5.c:29:12: note: each undeclared identifier is reported only once for each function it appears in
task5.c:29:14: error: 'S' undeclared (first use in this function)
   29 | BN_mod_exp(M,S,e,n, ctx);
      |             ^
task5.c:31:42: error: expected ';' before 'BN_free'
   31 | printBN("Verification message (M) = ", M)
      |                                          ^
      |                                          ;
.....
   34 | BN_free(n);

[10/14/23]seed@VM:~/.../lab8-RSA$ gcc task5.c -o task5 -l crypto
[10/14/23]seed@VM:~/.../lab8-RSA$ ./task5
Verification message (M) = 4C61756E63682061206D697373696C652E
```

After compiling the code we get the verification message.

Code of both 2F and 3F :

```
Open [icon] *task5.c
~/Desktop/Seedlab/lab8-RSA

1#include <stdio.h>
2#include <openssl/bn.h>
3void printBN(char *msg, BIGNUM *a){
4    // Convert the BIGNUM to a number string
5    char *number_str = BN_bn2hex(a);
6    // Print out the number string
7    printf("%s %s\n", msg, number_str);
8    // Free the dynamically allocated memory
9    OPENSSL_free(number_str);
10}
11int main(){
12    BN_CTX *ctx = BN_CTX_new();
13
14    BIGNUM *n = BN_new();
15    BIGNUM *s = BN_new();
16    BIGNUM *m = BN_new();
17    BIGNUM *e = BN_new();
18    // Initialize n, s, and e
19    BN_hex2bn(&n, "AE1CD4DC432798D933779FBD46C6E1247F0CF1233595113AA51B450F18116115");
20    BN_hex2bn(&s, "643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6803F");
21    BN_hex2bn(&e, "010001");
22    // Perform the modular exponentiation
23    BN_mod_exp(m, s, e, n, ctx);
24    // Print the result
25    printBN("Verification message (M) = ", m);
26    // Free allocated memory
27    BN_free(n);
28    BN_free(s);
29    BN_free(e);
30    BN_free(m);
31    BN_CTX_free(ctx);
32    return 0;
}
```

At last after in the green after we changed into 3F

## Changed 2F TO 3F

```
[10/14/23]seed@VM:~/.../lab8-RSA$ echo"changed 2F to 3F"
echochanged 2F to 3F: command not found
[10/14/23]seed@VM:~/.../lab8-RSA$ gcc task5.c -o task5 -l crypto
[10/14/23]seed@VM:~/.../lab8-RSA$ ./task5
Verification message (M) = 91471927C80DF1E42C154FB4638CE8BC726D3D66C83A4EB6B7BE0203B41AC294
[10/14/23]seed@VM:~/.../lab8-RSA$ █
```

We can see it was successfully running and we see the verification message.  
If we alter the last byte of the signature from 2F to 3F, the signature becomes:  
S = 91471927C80DF \_\_\_\_\_ so on in the screen shot above. Hehe.

**Observation :** When we compute the value of the message C using this modified signature and then compare it with the original message, we find that the computed message is entirely different from the original message. This minor change in the signature causes the verification to fail.

----- task 5 completed -----

## Task 6: Manually Verifying an X.509 Certificate

In this task, we will manually verify an X.509 certificate using our program. An X.509 contains data about a public key and an issuer's signature on the data. We will download a real X.509 certificate from a web server, get its issuer's public key, and then use this public key to verify the signature on the certificate.

### Step 1: Download a certificate from a real web server.

```

10/14/23]seed[VM:/.../Lab8-RSA$ openssl s_client -connect www.iiit.edu.org:443 -showcerts
CONNECTED(00000003)
depth=2 C = US, ST = Arizona, L = Scottsdale, O = "GoDaddy.com, Inc.", CN = Go Daddy Root Certificate Authority - G2
verify error:num=19:self signed certificate in certificate chain
verify return:1
depth=2 C = US, ST = Arizona, L = Scottsdale, O = "GoDaddy.com, Inc.", CN = Go Daddy Root Certificate Authority - G2
verify return:1
depth=1 C = US, ST = Arizona, O = "GoDaddy.com, Inc.", OU = http://certs.godaddy.com/repository/, CN = Go Daddy Secure Certificate Authority - G2
verify return:1
depth=0 CN = dan.com
verify return:1
---
Certificate chain
 0 s:CN = dan.com
   i:C = US, ST = Arizona, L = Scottsdale, O = "GoDaddy.com, Inc.", OU = http://certs.godaddy.com/repository/, CN = Go Daddy Secure Certificate Authority - G2
  -----BEGIN CERTIFICATE-----
MIHSzCCBjOgAwIBAgIIDWd03F2pqZm0QYjK0ZiHvcNAQELBQAwgBQxZCAJBgVw
BAYTALVTMRQAwDgYDVOQIEwDcm16b25hMRMwEQYDVOQHEwTpy290dHNkYXNlMRow
GAYDVOQKExFhbR8RZGR5LmNvbSwSgwSj1JEtMCCsGA1UECmKAAHR0cDovLzN1cmRz
LmdvdZGFKZHUyZ9tL3JlcG9zaXRvcnkvdG90dGV0QDEpYyBhYBMwSBTZWm1
cmUgO2YydgUmlnNhdGUGQXV0A9G9yaXRSICBGRzIwIWhhcnMjIjMxIjA0MDIwWhcN
MjQwMTIyMjA0MDIwIjwSMRQAwDgYDVOQDEwDkYm4uY29tMIBIIBjANBgkqhkiG9w0B
AQEFAAOCAQAMIBICGCAQEAwmNgEs50de7YDRW0Mpz8FSYyA4ftsv4dzxXHR9
QJ10YjKFTMu08VHLvSYjg67De307ze8qoyfT61jJD4Cz5x0kRh7EKmdp3zNbG/w
WCMHP+PkH6TBa3MnUiu/d4tXNB6hGkw+PJC5iGdw+z0eZsvhhx/Icrh3KzhMI
mAY85Fe7deYCh/cih48MBI6K1JkP56Ja/bka0hZQ5htLKBz8Y3KNZ26u3q/h+Xa
04V5dpTPI7L3JP51CjSp809dh0u80PJCtT7Q1fbkhGjuxgzVt7RyxLob5FS5G
ZuqLL8c7TyIaak0jRbcQtBt0fJRXA10A38c+th32AF70uDAQAB04IEADCCA/w
DAYDVR0TAQH/BAIwADAgBgNVHSUEFjAUBggrBgEFBQcDAQIKwYBBQUHwAwIwDgYD
VR0PAQH/BAQDAgAdBgGGA1UdHwQMCBwLAARoCMGJ2h0dHA6Ly9jcmVudZ29kYWRk
eS5jb29vZ2RrZ2JzZm900TUyLmNyb0Bd8BgNVHSAEYjBUMEgGCCG2CSAGG/W0BBxB
MDkKwYIKwYBBQUHAgEWMK2h0dHA6Ly9jXJ3BaWZpY2F0ZDZ0MjZ9kYWRkeS5jb29v
cmVud3NpdG9yeS8wCAYGZMAQEMIBMHGCCsGAQUFBwEBBG0wAOKBggrBgEFBQcw
AYYyAHRRcDovL29jc3AuZ29kYWRkeS5jb29vMEAGCCsGAQUFBzAChjRodHRw018v
Y2VydGUAmlnNhdG9vLmdvdZGFKZHUyZ9tL3JlcG9zaXRvcnkvdG90dGV0QDEpYyBh
A1UdIYQMAwFEDCvSe0z0SDMK1z1/1t3/CBLIDOMIHqBgNVHREGEIwgd+CD3YU
ZGVZ2MxvcGVLmNvbV9t0dW5kZXZlbG9wZWQwX20KODNlUyZGVZ2MxvcGVLmNugg51
bmRldmVsb3BlZC51a0I0dW5kZXZlbG9wZWQwX2MCDNlUyZGVZ2MxvcGVLmNvgg51
bmRldmVsb3BlZC5ubI0dW5kZXZlbG9wZWQwYmCEXV9tZGVZ2MxvcGVLmNlNlVr
gNlBmRldmVsb3BlZC5kZk1ha5ZeggdYm4uY29tqg343czG6LmNlNlVt0dW5k
ZGVZ2MxvcGVLmNlNlVrZGVZ2MxvcGVLm5IMB9GA1UdGwQgBgBQ1Pj3+LwMLMP
gXGZC5sVhhzqjCCAX0GcisGAQ0G1nkCBAtEgpfBTIIB0QnAHYAs3Q2NXb657F
XLedTMO7ojKHn9y87N7DUJhZrNEftZsAAAGfMnpnoQAABAMARzBFA1BCPr/UZ7fo
py0tMY0wb+UXK1DejuknyLx/d/YtXk1dpSAIhAL+sADW0eYzh2VtJ1N29rMf60BI
e191aFR63ztjF9SAHJASLDja9qmRz0P5Wc+pw6vxxSActk35y82bu/qznYHMA
AAGFNmpokQAABAMARzBEA1BzBTHrMY8koKw5cAwPE6iUaF4vjazneLcadk58AxN
EA1g9K2cVnnnRqQ0L5AL10FKULVypf13ZGgRq6aZtFdi8EAdgDatr9rP7W2Itp+
wrtca+hwk0Fsu1GEHt59p09w5Nf7qAAAYU2amkVAAEXAgGzPusuc7YnRe8XrY1Jp
H93AetSucymj+BYu0QYJK0ZiHvcNAQELBQAdggEBAC+jR6VrWbdgJ3b3aB91Nrd
4cB1+7ZA00E1lycx70eDp4rJ8KKT0AszelpndJYLJs4X/sGeTbPwb67BTQLXHD
KKUnCbvuwmSTFU051kfnCG6fPIuf7J0J60ceSob03HIP1WjBVXUjQK+bX0KCMmGA
Rlv9sFwgbtSq3IMP0B87HFHBCSIYKz/wm+T7xayA30s3M1Gy+nd3r17Xl7FN8G5
DPC6te8bA33+H1GG/JNfA4J7VUuGq90UzgsVkcNNEs828n9EkUCUszWRMH0R93
2r7IPedHel1G35m1q1L0BYDrXB3dtLEob5YhYf1swI2dKg3p0U+L9UR7rYato=
-----END CERTIFICATE-----
1 s: C = US, ST = Arizona, L = Scottsdale, O = "GoDaddy.com, Inc.", OU = http://certs.godaddy.com/repository/, CN = Go Daddy Secure Certificate Authority - G2

```

Here I took the website [www.iit.edu](http://www.iit.edu) and downloaded the certificate as explained in the description.

[illegible]

Copy and paste each of the certificates (the text between the line containing "Begin CERTIFICATE" and the line containing "END CERTIFICATE", including these two lines) to a file. Saved it as first one c0.pem and the second one c1.pem.

**Step 2: Extract the public key (e, n) from the issuer's certificate.**

**Step 2: Extract the public key ( $e$ ,  $n$ ) from the issuer's certificate.** Openssl provides commands to extract certain attributes from the x509 certificates. We can extract the value of  $n$  using `-modulus`. There is no specific command to extract  $e$ , but we can print out all the fields and can easily find the value of  $e$ .

```
For modulus (n):
$ openssl x509 -in cl.pem -noout -modulus

Print out all the fields, find the exponent (e):
$ openssl x509 -in cl.pem -text -noout
```

In the screenshot provided below, I've attached the results of two commands. These commands are essential for obtaining the value of 'e,' which will be used later in the process.

[illegible]

### Step 3: Extract the signature from the server's certificate.

**Step 3: Extract the signature from the server's certificate.** There is no specific `openssl` command to extract the signature field. However, we can print out all the fields and then copy and paste the signature block into a file (note: if the signature algorithm used in the certificate is not based on RSA, you can find another certificate).

```
$ openssl x509 -in c0.pem -text -noout
...
Signature Algorithm: sha256WithRSAEncryption
 84:a8:9a:11:a7:d8:bd:0b:26:7e:52:24:7b:b2:55:9d:ea:30:
 89:51:08:87:6f:a9:ed:10:ea:5b:3e:0b:c7:2d:47:04:4e:dd:
 .....
 5c:04:55:64:ce:9d:b3:65:fd:f6:8f:5e:99:39:21:15:e2:71:
 aa:6a:88:82
```

```
40:11:17:04
[10/14/23]seed@VM:~/.../Lab8-RSA$ openssl x509 -in c0.pem -text -noout
Certificate:
  Data:
    Version: 3 (0x2)
    Serial Number:
      07:2c:f5:0a:82:b6:25:c8:f6:73:91:93:8d:c2:eb:5a
    Signature Algorithm: sha256WithRSAEncryption
    Issuer: C = US, O = DigiCert Inc, CN = DigiCert TLS RSA SHA256 2020 CA1
    Validity
      Not Before: Jan  5 00:00:00 2023 GMT
      Not After : Jan 24 23:59:59 2024 GMT
    Subject: C = US, ST = Illinois, L = Chicago, O = Illinois Institute of Technology, CN = *.iit.edu
    Subject Public Key Info:
      Public Key Algorithm: rsaEncryption
      RSA Public-Key: (2048 bit)
      Modulus:
        00:98:80:47:34:55:e1:b4:92:9c:2b:55:09:06:25:
        d2:69:96:37:82:18:5d:e4:61:25:3c:40:a2:b0:e5:
        dd:0a:39:d0:c3:1b:6a:53:ef:b9:77:1f:d9:f4:87:
        b3:fd:cd:d1:d7:02:25:73:78:7d:07:04:c4:b9:63:
        2e:f1:5f:04:ad:97:a5:0d:f1:2b:6a:c6:bd:55:c5:
        3c:20:5b:20:e1:b3:98:00:a5:bd:e8:0a:53:d7:e7:
        05:e4:d3:40:08:22:a7:d8:d0:71:f1:f6:6b:b5:6e:
        8c:a8:7a:e9:ff:47:ab:cb:1c:59:4a:dc:b8:ac:27:
        2c:58:88:ca:6b:ae:a4:78:47:72:bb:ba:16:d6:6b:
        fa:2f:87:bc:50:30:34:e6:6c:76:9a:00:e3:94:e8:
        8a:5d:c8:9c:3e:4f:55:5a:74:d9:9e:ac:01:b4:1d:
        53:e2:cc:18:8c:bb:37:0e:7e:20:e4:c3:fb:e1:33:
        2b:71:df:68:62:8d:52:33:44:06:aa:c0:93:af:21:
        9c:c3:c0:31:f0:15:2e:ae:e6:8d:4b:85:c6:df:03:
        65:28:c1:cb:4b:97:54:c3:65:82:e7:94:b9:53:13:
        09:27:46:c6:3f:e9:22:52:6f:71:b2:b6:06:57:2a:
        33:04:e2:bb:fa:07:f9:81:fb:37:53:60:5d:be:34:
        f5:bd
      Exponent: 65537 (0x10001)

      B7:C4:82:6F:0C:3A:4B
    Signature Algorithm: sha256WithRSAEncryption
    11:39:f4:0b:3b:91:b8:25:81:66:7c:ee:b9:da:33:fc:cf:c3:
    24:e1:e2:09:4d:12:66:66:ce:8b:93:c6:eb:42:3e:ab:7e:0d:
    96:eb:0a:a6:46:2c:c9:85:81:e7:f5:02:dc:2b:60:72:b8:f7:
    2d:5c:08:71:12:43:f0:f9:8d:9d:52:d0:67:95:4d:cd:a2:20:
    53:29:c7:95:4b:4d:5c:5e:9f:ec:1f:65:b7:06:c5:1c:5b:ff:
    9a:69:3f:0e:d1:6a:9b:c9:99:dd:7b:fb:2d:df:42:75:35:c2:
    1c:69:4a:97:84:40:a1:c6:4d:a6:d5:ac:c5:e3:a7:75:8c:44:
    12:0e:45:2a:e8:ac:3f:2b:4d:3e:76:39:10:4b:1f:47:90:5f:
    ba:f4:ea:44:b6:c4:60:53:7e:48:4a:20:9e:b8:38:70:14:5d:
    4d:87:07:02:cd:d8:21:6d:09:18:00:16:d1:a9:e0:e0:61:66:
    d8:7e:da:0a:33:e0:9e:56:f1:a3:f2:14:5d:37:22:87:05:38:
    4b:f7:8a:47:75:c3:9c:05:8a:7c:79:77:b4:a9:ca:a5:1c:d2:
    5b:10:03:3c:1a:68:8a:2c:8e:39:c8:56:a5:51:f3:89:80:51:
    fa:db:dc:08:50:65:dc:e9:25:e6:45:e3:5c:a5:26:a3:0a:e2:
    70:de:1a:22
```

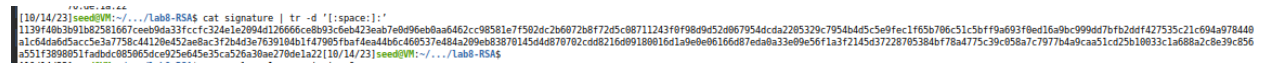
From the step 3 we took the values and variables of signature block into the file



We need to remove the spaces and colons from the data, so we can get a hex-string that we can feed into our program. The following command can achieve this goal. The `tr` command is a Linux utility tool for string operations. In this case, the `-d` option is used to delete ":" and "space" from the data.

```
$ cat signature | tr -d '[:space:]'
84a89a11a7d8bd0b267e52247bb2559dea30895108876fa9ed10ea5b3e0bc7
.....
5c045564ce9db365fdf68f5e99392115e271aa6a8882
```

Below is the screenshot of the above executed command.



```
[10/14/23]seed@VM:~/.../Lab8-RSA$ cat signature | tr -d '[:space:]'
1139f40b3b91b82581667ceeb9da33fccf324e1e2094d126666ce893c6eb423eab7e0d96eb0aa6462cc98581e7f502dc2b6072b8f72d5c08711243f8f98d9d52d067954dca285329c7954b4d5c5e9fec1f65b706c51c5bf9a693f6ed16a9bc999dd7bfb2ddf427535c21c694a978440
a1c64d8d6dacc5e3a7758c44120e452a8ba3f2b4d3e7639104b1f47965fba74ea44b6c468537e484a289eb83878145d4087072cdd8216d9918001d1a9e0e0166d7eda8a33e99e50f1a3f72145d37228705384bf78a4775c39c858a7c7977b4a9caa51cd25b10633c1a688a2c8e39c856
551f308051fadbc085965dc0f25e4f43e35ca526a308e2780e1a22110/14/23]seed@VM:~/.../Lab8-RSA$
```

## Step 4: Extract the body of the server's certificate

```
$ openssl asn1parse -i -in c0.pem
0:d=0 hl=4 l=1522 cons: SEQUENCE
4:d=1 hl=4 l=1242 cons: SEQUENCE
8:d=2 hl=2 l= 3 cons: cont [ 0 ]
10:d=3 hl=2 l= 1 prim: INTEGER :02
13:d=2 hl=2 l= 16 prim: INTEGER :0E64C5FBC236ADE14B172AEB41C78CB0
...
1236:d=4 hl=2 l= 12 cons: SEQUENCE
1238:d=5 hl=2 l= 3 prim: OBJECT :X509v3 Basic Constraints
1243:d=5 hl=2 l= 1 prim: BOOLEAN :255
1246:d=5 hl=2 l= 2 prim: OCTET STRING [HEX DUMP]:3000
1250:d=1 hl=2 l= 13 cons: SEQUENCE
1252:d=2 hl=2 l= 9 prim: OBJECT :sha256WithRSAEncryption
1263:d=2 hl=2 l= 0 prim: NULL
1265:d=1 hl=4 l= 257 prim: BIT STRING
```

The field starting from ❶ is the body of the certificate that is used to generate the hash; the field starting

```
[10/14/23]seed@VM:~/.../Lab8-RSA$ openssl asn1parse -i -in c0.pem
0:d=0 hl=4 l=1762 cons: SEQUENCE
4:d=1 hl=4 l=1482 cons: SEQUENCE
8:d=2 hl=2 l= 3 cons: cont [ 0 ]
10:d=3 hl=2 l= 1 prim: INTEGER :02
13:d=2 hl=2 l= 16 prim: INTEGER :072CF50A82B625C8F67391938DC2EB5A
31:d=2 hl=2 l= 13 cons: SEQUENCE
33:d=3 hl=2 l= 9 prim: OBJECT :sha256WithRSAEncryption
44:d=3 hl=2 l= 0 prim: NULL
46:d=2 hl=2 l= 79 cons: SEQUENCE
48:d=3 hl=2 l= 11 cons: SET
50:d=4 hl=2 l= 9 cons: SEQUENCE
52:d=5 hl=2 l= 3 prim: OBJECT :countryName
57:d=5 hl=2 l= 2 prim: PRINTABLESTRING :US
61:d=3 hl=2 l= 21 cons: SET
63:d=4 hl=2 l= 19 cons: SEQUENCE
65:d=5 hl=2 l= 3 prim: OBJECT :organizationName
70:d=5 hl=2 l= 12 prim: PRINTABLESTRING :DigiCert Inc
84:d=3 hl=2 l= 41 cons: SET
86:d=4 hl=2 l= 39 cons: SEQUENCE
88:d=5 hl=2 l= 3 prim: OBJECT :commonName
93:d=5 hl=2 l= 32 prim: PRINTABLESTRING :DigiCert TLS RSA SHA256 2020 CA1
127:d=2 hl=2 l= 30 cons: SEQUENCE
129:d=3 hl=2 l= 13 prim: UTCTIME :230105000000Z
144:d=3 hl=2 l= 13 prim: UTCTIME :240124235959Z
159:d=2 hl=2 l= 113 cons: SEQUENCE
161:d=3 hl=2 l= 11 cons: SET
163:d=4 hl=2 l= 9 cons: SEQUENCE
165:d=5 hl=2 l= 3 prim: OBJECT :countryName
170:d=5 hl=2 l= 2 prim: PRINTABLESTRING :US
```

```
$ openssl asn1parse -i -in c0.pem -strparse 4 -out c0_body.bin -noout
```

Once we get the body of the certificate, we can calculate its hash using the following command:

```
$ sha256sum c0_body.bin
```

```
[10/14/23] seed@VM:/.../Lab8-RSA$ openssl asnparse -in c0.pem -strparse 4 -out c0_body.bin -noot  
[10/14/23] seed@VM:/.../Lab8-RSA$ sha256sum c0 body bin  
8bd2dfbb37481a5c59241d4cf2f37f7608bf9cd8192ae68f10a10cb2ba8 c0 body bin  
[10/14/23] seed@VM:/.../Lab8-RSA$ gcc task5.c -o task5 -L crypto  
[10/14/23] seed@VM:/.../Lab8-RSA$ ./task5  
Verification message : 01FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF  
FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF  
FFFFFFFFFFFFFFFFF0B3E138D066906A48016503040201050004208002DFBB37481A5C59241CF2F37F7608BF9CD8192AE68F10A10CB2BA8
```

In the above screen shot after using the command we can see the sha256 sum

## Step 5 : Signature verification

```
[10/14/23]seed@WH:/.../.Lab8-RSAs openssl asnparse -i in.cem.pem -strparse 4 -out c0_body.bin -noout  
[10/14/23]seed@WH:/.../.Lab8-RSAs sha256sum c0_body.bin  
8dd7dfbb32481a5e29414f2f237f76d86bfec08192ae68f10cbb7a8a *c0_body.bin  
[10/14/23]seed@WH:/.../.Lab8-RSAs gcc task5.c -o task5 -l crypto  
[10/14/23]seed@WH:/.../.Lab8-RSAs ./task5  
Verification message [M] = 01ffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffffff  
FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF  
FFFFFFFFFFFFFFFFFF0803B138D0E069066A4801E563B4020105008420002DFBB32481A5E29414CF2F237F76D86BFEC08192AE68F10CBB7A8A
```

We can verify the correctness of our Task 5 code (modified code ) by comparing the verification message marked in **green with the final message marked in dark**. If these messages match, it indicates that we have successfully completed the lab.

It's worth noting that the original message and the hash value of the computed message are identical.

**Signature verification done .**

**Below I have attached the code snippet of the task ....**

## Task 6 Code :

```
task6.c  cp.pem  ct.pem  n  exp  signature  s signature
1 #include <stdio.h>
2 #include <openssl/bn.h>
3 void printBN(char *msg, BIGNUM *a){
4     // Convert the BIGNUM to a number string
5     char *number_str = BN_bn2hex(a);
6     // Print out the number string
7     printf("%s %s\n", msg, number_str);
8     // Free the dynamically allocated memory
9     OPENSSL_free(number_str);
10 }
11 int main(){
12     BN_CTX *ctx = BN_CTX_new();
13
14     BIGNUM *n = BN_new();
15     BIGNUM *s = BN_new();
16     BIGNUM *m = BN_new();
17     BIGNUM *e = BN_new();
18     // Initialize n, s, and e
19
20     BN_hex2bn(&n, "C148B3654770BCDD4F58DBEC9CEDC366E51F311354AD4A66461F2C0AEC6407E52EDDCB90A20E0DFE3C4D09E9AA97A1D8288E511560B1E9F58C251E72C3460");
21     BN_hex2bn(&s, "1139f40b3b91b82581667cceb9da33fcfc324e1e20944176666c08b93c6eb423eb7e0d96eb0aa6462cc98581e7f502dc2b6072b8f77d5c68711243f0f98d");
22     BN_hex2bn(&e, "010001");
23     // Perform the modular exponentiation
24     BN_mod_exp(m, s, e, n, ctx);
25     // Print the result
26     printBN("Verification message (M) = ", m);
27     // Free allocated memory
28     BN_free(n);
29     BN_free(s);
30     BN_free(e);
31     BN_free(m);
32     BN_CTX_free(ctx);
33     return 0;
34 }
```

In this step, we have incorporated the values of n, s, and e, which were extracted from the preceding steps explained in the description.

----- Task 6 done successfully and verified done hehe -----