

Binary \rightarrow 2

Decimal \rightarrow 10

Octal \rightarrow 8

Hexadecimal \rightarrow 16

~~(*) (*)~~ (\div)

~~(*) (*)~~ $(\times^* 4 +)$

CONVERSION OF DECIMAL $\frac{4}{10}$ TO DECIMAL.

To convert anything to Decimal $(n, \dots, 2, 1, 0) + \text{powers}$

\rightarrow for eg: we are given 101_2 , now we have to multiply the powers of 2 to each digit of 101 . Add them.

\rightarrow for eg: we are given 64_8 , now we have to multiply the power of 8 to each digit of 64 & add them

\hookrightarrow (descending order)

$$\rightarrow ① 101_2 = 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \\ = 4 + 0 + 1 = \underline{\underline{5}} = 101$$

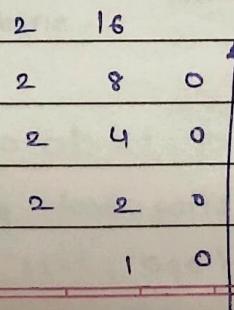
$$\rightarrow ② 63_8 = 6 \times 8^1 + 3 \times 8^0 \\ = 48 + 1 = \underline{\underline{49}} \quad (\text{in octal } 63_8 = \underline{\underline{49}} \text{ in decimal})$$

$$\rightarrow ③ (110)_{16} = 1 \times 16^2 + 1 \times 16^1 + 0 \times 16^0 \quad X \quad 1 \times 16^1 + 10 \times 16^0 \\ (110)_{16} = 256 + 16 = \underline{\underline{272}}_{10} \quad = 16 + 10 = \underline{\underline{26}} = \underline{\underline{1A}}.$$

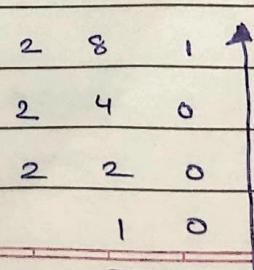
To convert decimal to binary. (\div by 2) \rightarrow (remainder = Binary code)

\rightarrow For going decimal to binary \rightarrow divide the given decimal number by 2 & (remainder is the binary code)

\rightarrow for eg: we are given 16 eg: we are given 17 .



$$= (10000)_2 = 16$$



$$(10001)_2 = 17$$

decimal \rightarrow octal \div by 8
 \rightarrow binary \div by 2
 \rightarrow hexa \div by 16.

} remainder
= ans.

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To convert decimal to octal (\div by 8) (remainder = octal code)

→ For going from decimal to octal, divide the decimal value by 8.
the remainder we get is the octal code.

for eg: we are given $(26)_{10}$.

eg: we are given $(44)_{10}$.

$$\therefore \div 8 \quad 26$$

$$\begin{array}{r} 3 \\ 8 \overline{) 26} \\ -24 \\ \hline 2 \end{array}$$

$$(32)_8 = (26)_{10}$$

$$(44)_8 = (54)_{10}$$

$$\begin{array}{r} 5 \\ 8 \overline{) 44} \\ -40 \\ \hline 4 \end{array}$$

To convert decimal to hexa decimal (\div by 16) (remainder = hexa code)

→ For going from decimal to hexa decimal, divide decimal by 16,
the remainder we get is hexadecimal value.

for eg: we are given $(26)_{10}$.

$$\therefore \div 16 \quad 26$$

$$1 \quad \begin{array}{c} 16 \\ \rightarrow A \end{array} = (1A)_{16}$$

$$= (110)_{16}$$

* now if we get value of in remainder betn. (10-15),
we write them as (A-f)

for eg : $16 \quad 46$

$$2 \quad \begin{array}{c} 16 \\ \rightarrow F \\ 14 \end{array} \quad \begin{array}{c} 16 \\ \rightarrow E \\ 2E \end{array}$$

Binary → octal } Separate binary no. into parts
 → Hexa } of 8 digits & 4 digits
 (Octal) (Hexa)

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Convert Binary to octal: (3 digits)

- ① Take the binary code
- ② Divide the binary code into parts of 3 digits

③ Convert the parts of 3 digits to numbers

④ combine numbers.

For example : 1 101011101001

① Separating binary into part of 3 digits

→ 10, 011, 110, 001

S 4 21.

② convert 3 digit parts to numbers.

→ 2, 3, 6, 1

③ combine numbers → (2361)₈

Convert binary to Hexadecimal (4 digits)

* Similar to octal conversion

① Take binary code.

② Divide binary code into parts of 4 digits

③ Convert parts of 4 digits to numbers.

④ combine.

For eg 110011110001

① separate into 4 digits.

→ Separating into parts of 4 digits

→ 100, 1111, 0001

② convert separated 4 digits into numbers.

→ Converting to number → 4, F, 1

= 4F11

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octal
4 \rightarrow Binary }
hexa decimal } ① convert to decimal
 } ② Decimal \rightarrow binary.

#

Conversion of octal to Binary

① convert octal \rightarrow decimal.

i.e. multiply by powers of 8 in descending order.
+ add digits.

② Take the decimal number & make its binary.

\rightarrow by $(\frac{\circ}{2} \text{ by } 2)$ \rightarrow remainder binary

eg : $(63)_8$

① convert to decimal. (8^n) .

$$6 \times 8^1 + 3 \times 8^0 = (51)$$

② decimal \rightarrow binary. (\div by 2)

2 51

$$\begin{array}{r} 2 25 1 \\ 2 12 1 \\ 2 6 0 \\ 2 3 0 \\ 1 1 \end{array} = \underline{(110011)}_2$$

2 12 1

2 6 0

2 3 0

1 1

① hexa \rightarrow decimal

conversion of hexa decimal \rightarrow Binary.

② decimal \rightarrow binary.

① convert hexa decimal \rightarrow Decimal.

\rightarrow multiply by powers of (16^n) in descending order
+ then add.

eg : $(63)_{16}$

② Decimal to Binary.

\rightarrow divide by (2)

2	99	$(11000011)_2$
2	49	
2	24	
2	12	
2	6	
2	3	
2	1	
	1	

Octal to Hexa + Hexa to octal

① convert octal to decimal

$\rightarrow \times$ by powers of (8) & \oplus

① Convert hexa to decimal

$\rightarrow \times$ by powers of (16) & \oplus

② Take decimal & convert to hexa
(\div by 16)

② Take decimal & convert to octal
(\div by 8)

eg: $(76)_8$

$$\begin{aligned} \textcircled{1} \text{ convert octal } &\rightarrow \text{decimal.} \\ &= 7 \times 8^1 + 6 \times 8^0 \\ &= 56 + 6 = \underline{\underline{(62)}_{10}} \end{aligned}$$

eg: $(1A)_{16}$

$$\begin{aligned} \textcircled{1} \text{ convert hexa } &\rightarrow \text{decimal} \\ &= 1 \times 16^1 + 10 \times 16^0 \\ &= 16 + 10 = \underline{\underline{(26)}_{10}} \end{aligned}$$

② Decimal to hexadecimol.
(\div by 16)

$$\begin{array}{r} 16 \quad 62 \\ \underline{\underline{3 \quad (14)}} \\ \textcircled{1} \text{ 14 } \xrightarrow{\text{E}} \\ \underline{\underline{(BE)}_{16}} \end{array}$$

② Decimal to base octal
(\div by 8)

$$\begin{array}{r} 8 \quad 26 \\ \underline{\underline{3 \quad 2 \quad 4}} \\ = \underline{\underline{(32)}_8} \end{array}$$

#

Ex

Decimal to Binary

$$\textcircled{0} \quad (13.375)_{10} \rightarrow \text{Binary}$$

13

$$\begin{array}{r} 2 \cdot 6 \\ 2 \quad 3 \quad 0 \end{array}$$

$$\begin{array}{r} 1 \cdot 1 \cdot 0 \cdot 1 \\ \hline \end{array}$$

$$= (1101.011)$$

0.375

$$\rightarrow 0.375 \times 2 = 0.750 \rightarrow 0.$$

$$\rightarrow 0.750 \times 2 = 1.500 \rightarrow 1$$

$$\rightarrow 0.500 \times 2 = 1.000 \rightarrow 1.$$

$$= 0.11$$

* Keep multiplying by 2, till we get 0.

Sign Magnitude Method:

- * 1 bit is reserved for sign of the number . i.e. (MSB).
- * 0 = +ve
- * 1 = -ve

- * Remaining bits are the number.

B9 (+4) (-ve 4)

$$= 0100$$

$$= + \textcircled{1} 100$$

↑ signbit

$$\begin{array}{r}
 \underline{\text{B9}} \quad 4 \quad 0100 \\
 \rightarrow 3 \quad 0011 \\
 \underline{+} \quad 0111
 \end{array}
 \quad
 \begin{array}{r}
 4 \quad 0100 \quad \therefore 0100 \\
 -3 \oplus 1011 \quad -0011 \\
 \underline{+} \quad \neq 1111 \quad \underline{0001}
 \end{array}$$

compare & subtract \rightarrow -4 = 1100

$$\rightarrow 3 \quad \ominus 0011$$

$$-1 \quad \underline{10001} = \textcircled{-1}$$

#

* 1's complement Method: (invert all bits of +ve no = -ve no)

* For +ve same as sign magnitude method.

$$\text{i.e. } +13 = 0\ 1101$$

* For -ve

① need to invert all bits of same +ve no.

e.g. -13 in 1^s complement.

= invert all bits of $+13$

$$\text{i.e. } = 0\ 1101 \rightarrow +13$$

now invert all bits

$$\therefore (-13 = 1\ 0010)$$

Invert
+ve
of +ve
= -ve

* 2's complement Method (1^s complement +1)

* For +ve no. same as sign magnitude method

$$\text{i.e. } +13 = 0\ 1101$$

* For negative numbers

① Take 1^s complement

(i.e. invert bits of same +ve no.)

$$\rightarrow +13 = 01101$$

② Add $(+1)$ to 1^s complement.

$$\therefore 1^s \text{ complement}$$

$$= -13 = 10010$$

e.g. -13 in 2^s complement

in 2^s complement

① Take 1^s complement (invert bits of $+13$)

$$= 1^s \text{ complement} + 1$$

$$= 01101 = +13$$

$$= 10010 + 1 = 10011$$

$$\therefore -13 \text{ in } 1^s \text{ complement} = 10010$$

i. -13 in 2^s complement = $(1^s \text{ complement} + 1)$

$$= 10010 + 1 = (10011) = -13 \text{ } 2^s \text{ comp.}$$

Rules for addition

A	+	B	sum	carry
0		0	0	0
0		1	1	0
1		0	1	0
1		1	0	1

$1+1=0$ carry 1.

Rules for subtraction

A	-	B	diff	borrow carry
0		0	0	0
0		1	1	1
1		0	1	0
1		1	0	0

$(0-1)=1$ borrow 1.

* $35 - 28 = 35 + (-28)$

$-28 = 2s$ complement or $1s$ complement

1s complement addition (add carry to answer)

(eg) : $35 + (-28)$

① take $1s$ complement of (-28) .

② Add $35 + 1s$ complement of (-28)

③ If carry is generated, add that to answer

* 2s complement addition (ignore if carry is generated)

eg: $35 + (-28)$

① take $2s$ complement of (-28) .

② Add $35 + 2s$ complement of (-28) .

③ (If carry is generated, ignore)

#

Classification of codes

* Weighted codes \rightarrow Binary, 8421, 2421, etc.

\rightarrow each position represent some value.

* Non weighted codes \rightarrow XS-3 code, Gray code.

* Alphanumeric code \rightarrow ASCII code.

#

Binary coded Decimal : (binary code for each digit) (ubit)

* ① Each decimal digit is represented by a 4 bit binary number.

Basically, write binary code for each digit.

Decimal BCD (same as binary just 4 bits).

0

0000

Decimal \rightarrow BCD.

1

0001

$$\star(1)_D = 1 + 0$$

2

0010

 $= 0001 \cdot 0000$

3

0011

 $= (\underline{00010000})_{BCD}$.

4

0100

$$\star(13)_{10} = 1 \quad 4 \quad 3$$

 $= 0001 \quad 0011$

5

0101

 $= 0001 \quad 0011$

6

0110

 $= (\underline{00010011})_{BCD}$

7

0111

$$\star(17)_{10} = 1 \quad 4 \quad 7$$

 $= 0001 \quad 0111$

8

1000

 $= (\underline{00010111})_{BCD}$

9

1001

BCD to Decimal :-

- ① Take decimal no.
- ② write the binary code for (each digit) of decimal.

eg: $(227)_{10}$

$$\begin{aligned} = 2 &= 0010 \rightarrow (0010\ 0010\ 0111) \\ 2 &= 0010 \\ 7 &= 0111 \end{aligned}$$

BCD to Decimal :- [group BCD into 4 bits] & (then calc. decimal value)

- ① Group the ~~BCD~~ BCD into 4 bit group.
- ② Take decimal value of 4 bit groups.

eg: 1001010010101111

0010 ① 0010 ② 0101 ③

① \Rightarrow 2

② \Rightarrow 5

③ \Rightarrow 7

$= (227)_{10}$

Eq 10 in binary

$$10 = \underline{1010}$$

10 in BCD

$$10 = 1 + 0.$$

$$= (\underline{\underline{0001\ 0000}})$$

similar
+ to
binary to
hexa

(self complementing)

Add 3 to BCD

Excess - 8 code (XS - 3 code) [Add 3 to BCD].

** convert Decimal to XS - 3 code

① convert Decimal to BCD.

② Add (0011)(3) to BCD.

= XS 3 code

$$\text{eg: } 5 \rightarrow \text{BCD} = 0101 \rightarrow \text{BCD} + 3 = \underline{\underline{0101}} \\ + 0011$$

$$\text{for } 5 \rightarrow \text{XS-3 code} = \underline{\underline{1000}} = \underline{\underline{8}}$$

<u>Decimal</u>	<u>BCD</u>	<u>BCD + 3</u>
0	0000	$0000 + 0011 = 0011$
1	0001	$0001 + 0011 = 0100$
2	0010	$\underline{\underline{0101}} = 0101$
3	0011	$= 0110$
4	0100	$= 0111$
5	0101	$= 1000$
6	0110	$= 1001$
7	0111	$= 1010$
8	1000	$= 1011$
9	1001	$= 1100$

∴ XS 3 code for 24.

(1) convert 24 to BCD.

(2) Add 0000 0011 to BCD 24.

$$\rightarrow \text{BCD } 24 = 00100100$$

$$\rightarrow \text{BCD } 24 + 3 = 00100100$$

$$\underline{\underline{+ 0011}} \\ \underline{\underline{1001001111}} = \text{XS 3 code for 24}$$

XS - 3 code for digits above 9.

① Take the BCD of the number.

② Add 8 to each BCD value of the number.

Ex XS - 3 code for 24.

① BCD of 24 = 2 4.

(0010 0100)

② Add (0011) to 2 BCD + (0011) to 4 BCD.

$$\begin{array}{r}
 = 0010 \quad 0100 \\
 + 0011 \quad + 0011 \\
 \hline
 0101 \quad 0111
 \end{array}$$

= (01010111)

Ex: XS - 3 code for 156.

① BCD of 156 = 1 5 6.

0001 0101 00110

② Add 8 to each digit BCD.

$$\begin{array}{r}
 = 0001 \quad 0101 \quad 00110 \\
 + 0011 \quad + 0011 \quad + 0011 \\
 \hline
 0100 \quad 1000 \quad 10001
 \end{array}$$

= (010010001001)

Binary \rightarrow Gray } MSB remains
 Gray \rightarrow Binary } the same.

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Graycode: $Y = A\bar{B} \rightarrow \bar{A}B$ (XOR)

* Reflected Binary Code (RBC).

* two successive value differ in only one bit.

* Binary number is converted to Gray code to reduce switching operation.

Binary Gray.

$B_3 B_2 B_1 B_0$ $G_3 G_2 G_1 G_0$

3.	0	0	1	1	0	1	0
4.	0	1	0	0	1	0	0

- To change from 3 to 4,
 we need to change 8 bits.
 ∴ to change from 3 to 4
 in Gray code we need to
change only one bit.

Binary to Graycode Conversion

① Record MSB as it is

* ② Add MSB to next bit, record the sum neglect carry

③ Repeat ②.

* Eg convert 1011 to Gray code.

$\rightarrow \begin{matrix} 1 & 0 & 1 & 1 \\ \uparrow & & & \\ \text{MSB} & & & \end{matrix}$

① Record MSB as it is. = ① .

② Add MSB to next bit = $1 + 0 = 1$.
(record sum, neglect carry).

repeat process

$$= 0 + 1 = 1 \quad = \underline{(1110)}$$

$$= 1 + 1 = 0$$

Binary to ~~Gray~~ Gray:

① Record MSB

② Add 1st & 2nd pos

Add 2nd & 3rd pos

Add 3rd & 4th pos

Record sum ignore

carry .

-- continue till last element

Ex: 1110 .

MSB = 1 .

$1 + 1 = 0 .$

$1 + 1 = 0 . \quad = \underline{(1001)}$

$1 + 0 = 1 .$

$\begin{matrix} 1 & 1 & 1 & 0 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ 1 & 0 & 0 & 1 \end{matrix}$

$\underline{1 \ 0 \ 0 \ 1}$

#

Gray code to Binary Conversion: [Same as ~~Binary to Gray~~]

① Record MSB as it is.

② Add MSB to next bit of gray code.

Basically

① Record MSB

② Add 1st & 2nd position.

Add 2nd & 3rd position

Add 3rd & 4th position

① record sum

② Ignore carry

eg: ~~1110~~ ~~Gray code~~

$$\begin{aligned} &= 1, 1+1=0, 1+1=0, 1+0=1 \\ &= \underline{\underline{1001}} \end{aligned}$$

eg: 1110 ← Gray code

$$\begin{array}{r} 1110 \\ +0110 \\ \hline 1001 \end{array}$$

$$B_1 = G_1$$

$$B_2 = G_2 \oplus B_1$$

$$B_3 = G_3 \oplus B_2$$

$$B_4 = G_4 \oplus B_3$$

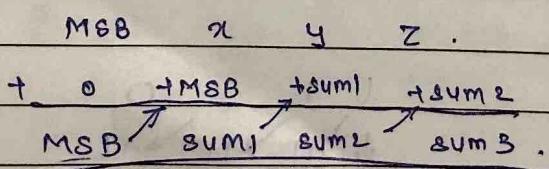
Basically

① Record MSB → 0 = MSB.

② Add $MSB + 0 = MSB$ to next bit = sum ①

Add sum ① to next bit = sum ②.

Add sum ② to next bit = sum ③.



Basically add result
of previous sum
to next bit

eg. 1 0 0 1 (Gray code)

$$\begin{array}{cccc} \downarrow & \rightarrow +1 & \rightarrow +1 & \rightarrow +1 \\ 1 & 1 & 1 & 0 \end{array}$$

(if 1001 = binary to Gray)

$$\begin{array}{c} \therefore 1, 1+0, 0+0, 0+1 \\ = (1101) \end{array}$$

ASCII - codes (Group 7 bits in binary).

$$\ast 48 - 57 = 0 - 9.$$

$$\ast 65 - 90 = A - Z \text{ capital.}$$

$$97 - 122 = a - z \text{ small}$$

ASCII

Binary \rightarrow Decimal \rightarrow ASCII

Group 7 bits in binary.

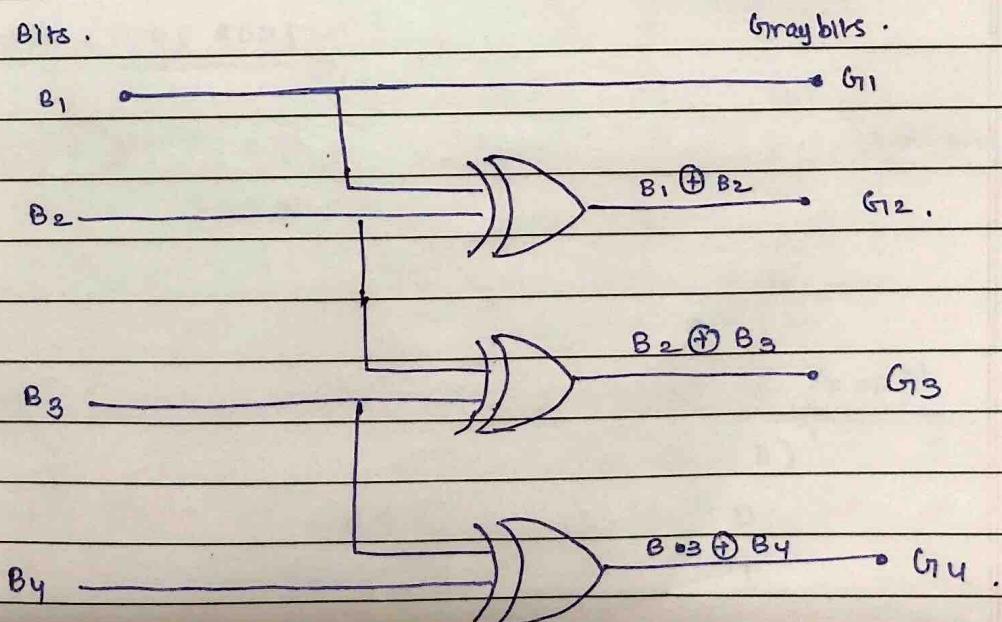
convert each group to decimal.

10100011001011
81 75

\therefore from 65-90, A-Z capital.

Binary \rightarrow Gray code = (XOR) . (Just apply XOR)

Binary Bits.



Gray bits.

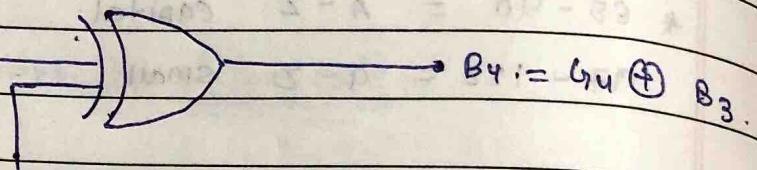
#

Gray code to Binary (XOR logic)

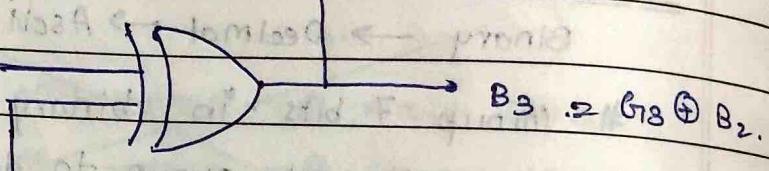
Gray code

Binary

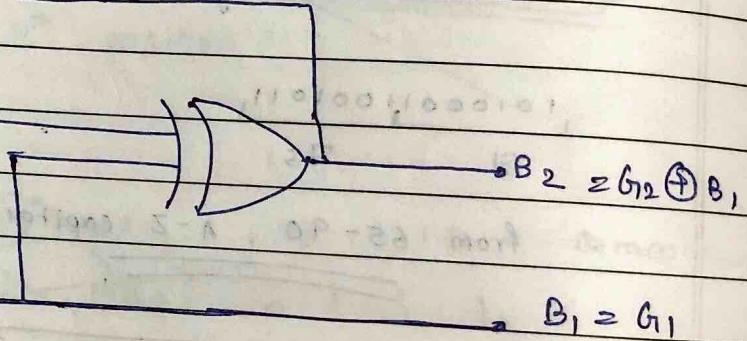
G_4



G_3



G_2



~~Binary to Gray code~~

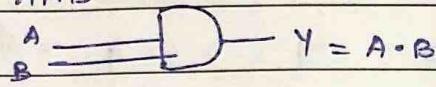
$B_1 = G_1$

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Basic Logic Gates

A . B Y

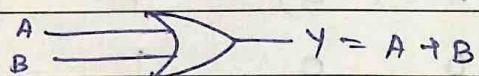
① AND (Multiplication)



0	0	0
0	1	0
1	0	0
1	1	1

AND (x).

② OR (Addition)



A + B Y

0	0	0
0	1	1
1	0	1

OR (y).

③ NOT (complement)



A Y

NOT (complement).

④ XOR (Pure Addition)

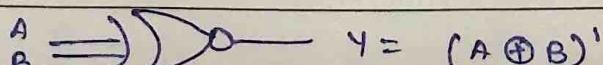


A ⊕ B Y

0	0	0
0	1	1
1	0	1

XOR (pure addition)

$$= \bar{A}B + A\bar{B}$$

⑤ X-NOR (pure addition)' = complement of (XOR)' (y).

(A ⊕ B)' Y.

0	0	1
0	1	0
1	0	0
1	1	1

(XOR)' = X-NOR

⑥ NAND $x = (A \cdot B)'$ (complement of AND)

$$(A \cdot B)' = y.$$

$$\Rightarrow \text{Do } y = (AB)'$$

$$0 \cdot (1 \cdot 1) = 1$$

0	1	0	0	1	1	0
0	0	1	1	0	0	1
1	1	1	1	1	1	0

⑦ NOR $x = (A + B)'$ (Complement of OR)

$$(A + B)' = y$$

$$(Y) \text{ OR} = \overline{(1+1=1)}$$

A	1	0	1	0	1	0
B	1	1	0	1	0	0
	1	0	1	1	0	1

(Invertors) for

(Invertors) for

(Invertors) for

(Invertors) for

'(AxB) do to minimize' '(minimize)' (min-X)

'P' '(A + B)'

'(A + B) = P' = A' + B'

A + B = A'B' + AB



serial \rightarrow use AND.
parallel \rightarrow use OR.

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Boolean Algebra

- * Commutative law * Associative law * Distributive law
- (10) • $A + B = B + A$ (12) $(A + B) + C = A + (B + C)$ (14) $A \cdot (B + C) = AB + AC$
(11) • $A \cdot B = B \cdot A$ (13) $(A \cdot B) \cdot C = A \cdot (B \cdot C)$ (15) $A \cdot (B + C) = (A \cdot B) + (A \cdot C)$

Duality theorem

① change each OR to AND

② change each AND to OR

③ complement each 0 & 1

Fundamental laws

* AND laws

$$x=1 \quad x'=0$$

① $x \cdot x = x$

② $x \cdot 1 = x$

③ $x \cdot 0 = 0$ AND

④ $x \cdot \bar{x} = 0$ Complement

because $x=1$

$$\bar{x}=0$$

* OR laws

$$A=01, \bar{A} + A' = 1$$

⑤ $A + 0 = A$

⑥ $A + 1 = 1$ OR

⑦ $A + A = A$

⑧ $A + \bar{A} = 1$ OR

$$0+1=1$$

⑨ $\bar{\bar{x}} = x$

Dual of Distributive law

⑩ Top of page

⑯ $(x + (y \cdot z)) = (x + y) \cdot (x + z)$

$$\text{DeMorgan's} = A \cdot B = \overline{A} \cdot \overline{B}$$

$$\overline{A \cdot B} = \overline{A} + \overline{B}$$

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DeMorgan's Theorem

$$* \overline{A + B} = \overline{A} \cdot \overline{B} \quad \left. \begin{array}{l} \text{converting AND to OR} \\ \text{OR} \end{array} \right\}$$

$$* \overline{A \cdot B} = \overline{A} + \overline{B} \quad \left. \begin{array}{l} \text{OR to AND} \\ \text{OR} \end{array} \right\}$$

Identity Theorem:

$$* x \rightarrow (\bar{x} \cdot y) = (x \rightarrow y)$$

$$* \underline{x \cdot (\bar{x} \rightarrow y)} = (x \cdot y)$$

$$\rightarrow x \rightarrow (\bar{x} \cdot y)$$

$$= (x \rightarrow \bar{x}) \cdot (\underline{x \rightarrow y}) = (x \rightarrow y)$$

$$x \geq 1, \therefore \bar{x} \geq 0$$

$$= 0 \cdot 1 = 0$$

$$x \cdot \bar{x} = 1 \quad x=0, \bar{x}=1$$

$$\therefore \underline{(x \rightarrow \bar{x})} = 1$$

$$\rightarrow x(\bar{x} \rightarrow y) = x \cdot y$$

$$(x \cdot \bar{x}) + (\underline{y \cdot x}) = (x \cdot y)$$

$$0 + (\underline{y \cdot x}) = (x \cdot y)$$

1 + any input = 1.

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$$A=1, \bar{A}=0, B=1, \bar{B}=0.$$

(Q1) $Y = \bar{A}B + A\bar{B} + AB.$

Take A common.

$$\bar{A}B + A(\bar{B} + B). \quad \therefore \bar{B} + B = 1.$$

$$\bar{A}B + A =$$

$$\therefore (C+AD) = (C+A) \cdot (C+D)$$

$$\therefore (A+\bar{A}) \cdot (A+B)$$

$$\therefore \underline{(A+\bar{A})} = 1$$

$$\therefore \underline{(A+B)}$$

(Q2) $Y = \underline{\bar{ABC}} + \bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C} + \underline{A\bar{B}C}$

Take $\bar{B}C$ common.

$$Y = \underline{\bar{ABC}} + A\bar{B}\bar{C} + \bar{B}C(\bar{A} + A).$$

$$\therefore (\bar{A} + A) = 1.$$

$$= \bar{ABC} + \underline{A\bar{B}\bar{C}} + \bar{BC}$$

Take \bar{B} common.

$$= \bar{B}\bar{C} + \bar{B}(A\bar{C} + C)$$

~~absorbing~~.

$$= \bar{B}\bar{C} + \bar{B}[(A\bar{C}) \cdot (C+\bar{C})]$$

$$(C+\bar{C}) = 1.$$

$$= \bar{B}\bar{C} + \bar{B}[A+\bar{C}]$$

$$= \bar{ABC} + \underline{A\bar{B} + A\bar{C}}$$

(Q3) $F = \underline{\bar{y}\bar{z}} + \bar{w}\bar{x}\bar{z} + \underline{\bar{w}\bar{x}\bar{y}\bar{z}} + y\bar{z}$

Take $\bar{y}\bar{z}$ common.

$$= \underline{\bar{y}\bar{z}} + (1 - \bar{w}\bar{x}) + \bar{w}\bar{x}\bar{z} + y\bar{z})$$

$$(x-1) = x.$$

$$= \underline{\bar{y}\bar{z}} + (1) + \underline{\bar{w}\bar{x}\bar{z} + y\bar{z}}$$

Take \bar{z} common.

$$\bar{z}(\bar{y}+y) + \bar{w}\bar{x}\bar{z} = \bar{z} + \bar{w}\bar{x}\bar{z}.$$

$$(\bar{y}+y)=1.$$

$$\bar{z} + \bar{w}\bar{x}\bar{z}$$

take \bar{z} common.

$$\bar{z}(1 + \bar{w}\bar{x})$$

$$(1+1) = 1 \quad \therefore xz = 1$$

$$= \bar{z}$$

*Solving XNOR.

$$\rightarrow \bar{A}\bar{B} + AB$$

$$\rightarrow \overline{\bar{A}B + A\bar{B}}$$

$$= \overline{x+y} = \bar{x} \cdot \bar{y} \text{ demorgans}$$

$$\bar{A}\bar{B} \cdot \bar{A}\bar{B} + \bar{A}\bar{B} + \bar{A}\bar{B}$$

$$= \text{again demorgans}$$

$$= (\bar{A} + \bar{B}) \cdot (\bar{A} + \bar{B})$$

$$= (A + B) \cdot (A + B)$$

$$= A\bar{A} + AB + \bar{A}\bar{B} + B\bar{B}$$

$$\therefore A\bar{A} + B\bar{B} = 0$$

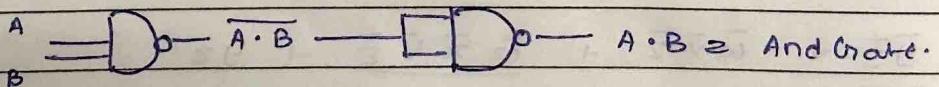
$$= \underline{(AB + \bar{A}\bar{B})}$$

#

Construct AND using NAND.

$$\therefore (A \cdot B)' \rightarrow A \cdot B \quad (\underline{2 \text{Nand gates}})$$

2 nand gates
series



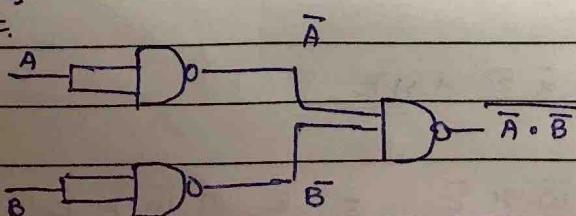
#

Construct OR using NAND. $(A + B)' \leftarrow (A \cdot B)'$

Short input

2 nand
gates
parallel

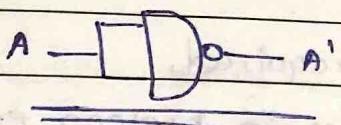
again
nand gate



APPLY demorgan $\rightarrow \bar{A} \cdot \bar{B}$

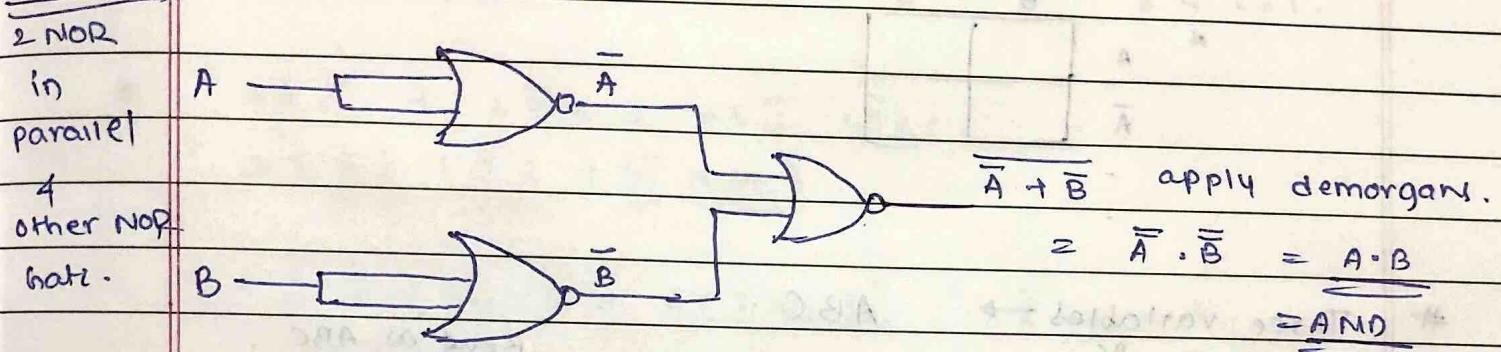
$$= \bar{A} + \bar{B} = \underline{(A + B)}$$

NOT using NAND: $(A \cdot B)' \rightarrow A'$

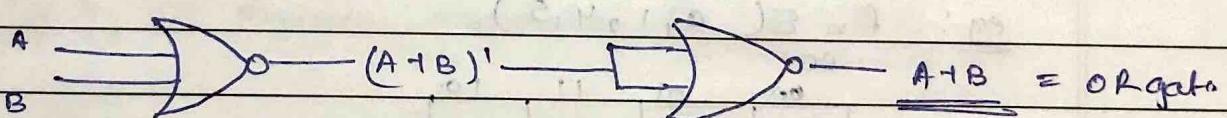


Construction of AND using NOR

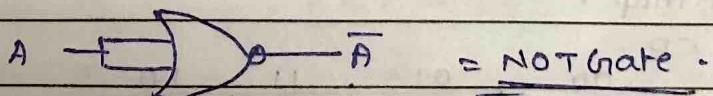
$$(A + B)' \rightarrow A \cdot B.$$



OR Gate using NOR $(A + B)' \rightarrow A + B.$



NOT Gate using NOR



$$\overline{A} = 0 \quad A = 1$$

K-map is always made for Input Output

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#

K-maps

$$N = 2^n$$

, N = no. of cells required

n = no. of variables in boolean exp.

#

Two variables \rightarrow

\overline{A}	\overline{B}	B	\overline{B}
\overline{A}	$A\overline{B}$	AB	$A\overline{B}$
B	$\overline{A}\overline{B}$	$\overline{A}B$	$\overline{A}B$
\overline{B}			

A	B	\overline{B}	B
\overline{A}	\overline{B}	B	\overline{B}
A	\overline{B}	B	\overline{B}

A	B	\overline{B}
\overline{A}		
A		

$$B = A \oplus B = OR(A, B)$$

#

Three variables $\rightarrow ABC$

		BC			
		00	01	11	10
A		0			
1					

Read as ABC.

$$\text{eg: } f = \Sigma(0, 1, 4, 5)$$

BC.

AD		00	01	11	10
1		1	1		
0		1	1		

quad $\rightarrow B$

#

4 variable Kmap.

CD.

AB		00			
01					
10					
A	B	00			
0	1				
1	0				
1	1				

1 group ①

KMap for Minterm

(SOP)

①.

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Ex. Plot eqn $AB + A\bar{B} + BC$. (Three variable.

BC

A	00	01	11	10
00				
01	1	1	1	1
11				
10				

* All spots where $A \neq B$ are 1

* All spots where $A=1, B=0$.

$A + \bar{B}C$

* All spots where $B \neq C = 1$.

$A\bar{B}\bar{C} + A\bar{B}C + AB\bar{C} + ABC$.

$A(\underline{\bar{B}\bar{C}} + \underline{\bar{B}C} + \underline{B\bar{C}} + \underline{BC})$.

$A(\bar{B}(\bar{C}+C) + B(\bar{C}+C))$ $\bar{C}+C = 1$.

$A(\bar{B}+B) = \underline{A}$ $\bar{B}+B = 1$.

$F = A + \bar{B}C$ Three variables.

$2^3 = 8$ prepare truthtable for $A + \bar{B}C$.

A B C F.

$F = (\bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C} + A\bar{B}C + ABC + ABC)$.

0 0 0 0

~~+ ABC~~)

0 0 1 0

= (for which $F=1$)

0 1 0 1

$= \bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C} + A\bar{B}C + ABC + ABC$

1 0 0 1

$= \bar{A}\bar{B}\bar{C}(B+\bar{B}) + AB(\bar{C}+C) + ABC$

1 0 1 1

$= \bar{A}\bar{C} + AB + ABC$.

1 1 0 1

$= \bar{A}\bar{C} + AB(C+\bar{C})$.

1 1 1 1

$= \bar{A}\bar{C} + AB$. $\therefore 1+0=1$.

1 → Minterm

0 → maxterm

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A	BC	00	01	11	10
B					
C					
0					
1		1	1	1	1

$$\underline{A + BC}$$

g) $F(A, B, C) = \text{sop} (1, 3, 5, 7)$.

A	B	C	00	01	11	10
0						
1						
0			0	1	1	1
1			1	1	1	1

$$\Rightarrow \underline{C}$$

group 0

[POS]

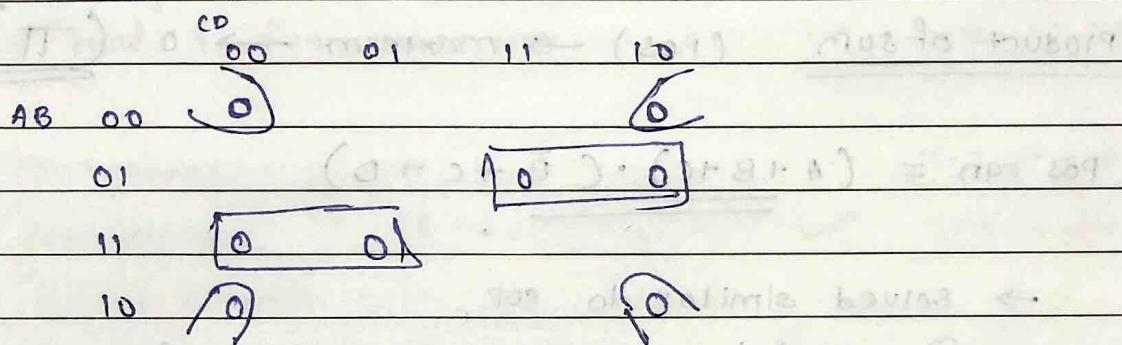
Kmap for max-term ①.

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eg $f(A, B, C, D) = \overline{\Sigma m}(1, 3, 4, 5, 9, 11, 14, 15)$.
 \hookrightarrow min-terms (1).

$= \prod m(0, 2, 6, 7, 8, 10, 12, 13)$.
 \hookrightarrow max-terms (0).

$\therefore 2^4 = 16$.



$$(\bar{B}\bar{D}) + AB\bar{C} + \bar{A}BG$$

4. Write it as, invert everything, | complement everything.

~~$$= (\bar{B} + D) \cdot (\bar{A} + \bar{B} + C) \cdot (A + \bar{B} + \bar{C})$$~~

① change $A \rightarrow \bar{A}$

4 change $(\cdot \rightarrow +) \text{ and } (+ \rightarrow \cdot)$

Standard forms

Sum of products (SOP) \rightarrow minterms $\rightarrow \oplus . (\Sigma) / (\Sigma)$

$$\text{SOP eqn} = \underline{\oplus A B C} + \underline{\oplus D E F}$$

Product of sum (POS) \rightarrow maxterm $\rightarrow \ominus . (\Pi)$

$$\text{POS eqn} = \underline{(A + B + C)} \cdot \underline{(C \bar{B} + C + D)}$$

\rightarrow solved similar to SOP,

① plot '0' in the K map instead of 1.

② group '0' instead of 1.

③ get eqn in the form of POS.

④ convert SOP \rightarrow POS.

\rightarrow change (\ominus) to (+)

+ viceversa.

$(\ominus \oplus +) + \ominus \rightarrow$ change $\bar{A} \rightarrow A$ + viceversa

SOP (minterms) POS (max terms)

