



Q1) For a  $(6,3)$  Linear Block code, the parity bits are derived from following equations.

$$P_4 = d_1 \oplus d_2$$

$$P_5 = d_1 \oplus d_2 \oplus d_3$$

$$P_6 = d_2 \oplus d_3$$

- a) Find generator matrix  
b) Find all code words

Q2) For a linear block code  $H$  matrix is given by

$$H = \begin{bmatrix} 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$$

- a) What is value of  $n$  and  $k$  of the linear block code  
b) If the received code word is  $[0001101]$ , find syndrome and comment about it

Q3) Define hamming distance and hamming weight with example



$$Q2) \quad H = \begin{bmatrix} 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$

e)  $n=7$   $k=4$   
 $n-k=3$

$$b) \quad H^T = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$G = \begin{bmatrix} 1 & 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$G = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 1 \end{bmatrix}$$

$$[C_1, C_2, C_3, C_4, C_5, C_6, C_7] = [D_1, D_2, D_3, D_4] \cdot G$$

$$(\cancel{D_1 \oplus D_3 \oplus D_4}) (\cancel{D_1 \oplus D_2 \oplus D_3})$$

$$D_1, D_2, D_3, D_4, (D_1 \oplus D_3 \oplus D_4), (D_1 \oplus D_2 \oplus D_3), (D_2 \oplus D_3 \oplus D_4)$$





Code word: 0001101

$$S = (0001101) \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= [0, 0, 0]$$

There is no error received code word is correct

Q3) If there are binary datas then if take the count the number of bits that are flipped in the data ~~can~~ data that is received compared to data that is sent. This is called hamming distance

ex. 0001101  
1011101

In this the hamming distance is 2.

The count of the number of non zero components in a given codeword is called as the hamming weight.

ex. 01110111

In this the hamming weight would be 6.



