

1)

```
{ proc Q(x)
  integer x;
  begin
  integer y := x * 2;
  Q := y
  end;
```

2)

We can consider  $w = A(i)$  so when P called , in the first line we have :

$i := w = A(1) = 2$

$w := i = 2 \Rightarrow A(2) = 2$

$\Rightarrow A(1) = A(2) = i = 2$

3)

a) fun  $f(x,y) = \text{if}(y=0) \text{ then } x \text{ else if}(x=0) \text{ then } y \text{ else } x+y;$

b) No, since no variable can occur twice in each pattern . Error: duplicate variable in pattern(s)

c) We have to assign different names for different variables and use “if clause” to check equal variables.

fun  $\text{eq}(x,y) = \text{if } x=y \text{ then true else false}$

d) since ML has type variables and as we know “*ML is statically typed*”, meaning that it performs its type checking operations at compile time .also, functions’ behavior cannot be processed at compile time, thus repeated variables are not allowed in ML.

4)

a) fun  $\text{maptree}(f,\text{leaf}(x)) = \text{leaf}(f(x))$   
|  $\text{maptree}(f,\text{node}(x,y)) = \text{node}(\text{maptree}(f,x),\text{maptree}(f,y));$

b)  $( 'a \rightarrow 'b ) * 'a \text{ tree} \rightarrow 'b \text{ tree}$

6)

a) `fun curry f = fn x => fn y => f(x,y);`

`fun uncurry g = fn (x,y) => g x y;`

b)

`uncurry(curry(f)) = uncurry('a → ('b → 'c)) = ('a*'b) → 'c`

`curry(uncurry(g)) = curry(('a*'b) → 'c) = 'a → ('b → 'c)`

8)

a)

`fun merge cmp (nil, yss) = yss`

`| merge cmp (xss, nil) = xss`

`| merge cmp (x::xs, y::ys) = if cmp(x,y) then x :: merge cmp (xs, y::ys)  
else y :: merge cmp (x::xs, ys);`

b)

`- fun compose(f, g) = fn x => f(g(x));`

`> val ('a, 'b, 'c) compose = fn : ('a -> 'b) * ('c -> 'a) -> 'c -> 'b`