

RAMJET PROPULSION ANALYSIS PROJECT

MAE 563: AIRCRAFT PROPUSLSION

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## Introduction

In this project, we will develop an analysis tool using MATLAB programming language for parametric studies of ramjet propulsion performance and to examine performance variation across a range of key parameters. We will implement different sets of equation taught in lectures to analyze performance of a 'Non-Ideal Ramjet Propulsion System.'

We will use following set of parameters in analysis tool to obtain detailed results:

Flight Altitude	$Z$
Flight Mach Number	$M_1$
Inlet/Diffuser Efficiency	$\eta_d$
Diffuser Exit Mach Number	$M_2$
Combustor Exit Max Allowable Temperature	$(T_{t3})_{\max}$
Fuel Heating Value	$q_f$
Nozzle Efficiency	$\eta_n$
Nozzle Exit Area	$A_e$
Universal Gas Constant	$R$
Standard Gravity	$g$

Table 1: Analysis Tool Inputs

Total and Static Temperatures	$T_t \text{ \& } T$
Total and Static Pressures	$P_t \text{ \& } P$
Relative Change in Entropy	$\Delta s$
Flow Speed	$V$
Mach Number	$M$

Table 2: State Outputs

Below are the outputs of parametric analysis tool which are included in states of 1,2,3, e and 4.

Thrust	$T$
Propulsive Power	$P$
Thermal Efficiency	$\eta_{th}$
Propulsive Efficiency	$\eta_p$
Overall Efficiency	$\eta_o$
Required Fuel Flow Rate	$\dot{m}_f$
Thrust Specific Fuel Consumption	$TSFC$
Specific Impulse	$I_{sp}$

Before beginning parametric analysis, we must validate analysis tool by running it for two test cases which are:

1. Non-Thermally Choked Test Case
2. Thermal choked Test Case

<b>Case # 1 Non-Thermally Choked</b>	
Flight Altitude	4300 <i>m</i>
Flight Mach Number	2.4
Inlet/Diffuser Efficiency	0.92
Diffuser Exit Mach Number	0.15
Combustor Exit Max Allowable Temperature	2400 <i>K</i>
Fuel Heating Value	46 <i>MJ</i>
Nozzle Efficiency	0.94
Nozzle Exit Area	0.015 <i>m</i> <sup>2</sup>
R	$\frac{J}{kg * K}$ 286.9

Table 4: Inputs for Validation Case (a)

<b>Case # 2 Thermally Choked</b>	
Flight Altitude	4300 <i>m</i>
Flight Mach Number	2.4
Inlet/Diffuser Efficiency	0.92
Diffuser Exit Mach Number	0.4
Combustor Exit Max Allowable Temperature	2400 <i>K</i>
Fuel Heating Value	46 <i>MJ</i>
Nozzle Efficiency	0.94
Nozzle Exit Area	0.015 <i>m</i> <sup>2</sup>
R	$\frac{J}{kg * K}$ 286.9

Table 5: Inputs for Validation Case (b)

Note:

The gamma values of combustor upstream is 1.4 and downstream of combustor is 1.3.

$C_p(t) = a + bt$ , where  $a=986$  and  $b=0.170$

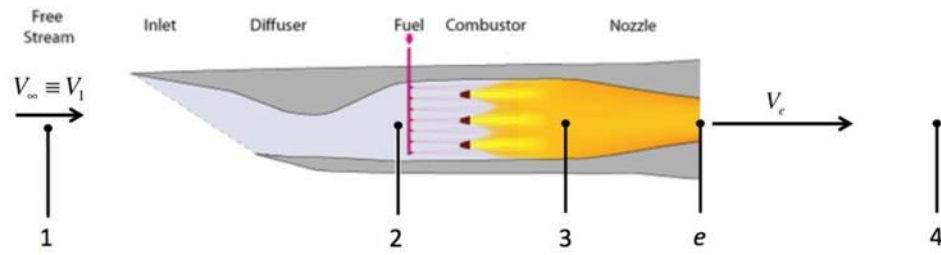


Fig1: Propulsion System Used

## Problem A:

Below are graphs of two cases of thermally choked and non-thermally choked test cases. The T-S diagrams show net work of cycle and enclosed area shows net work done. Fig 2 represents a non-thermally choked test case and fig 3 represents thermally choked test case. The value of  $C_p$  is taken to be  $1004 \text{ J/kg}$  for 4-1.

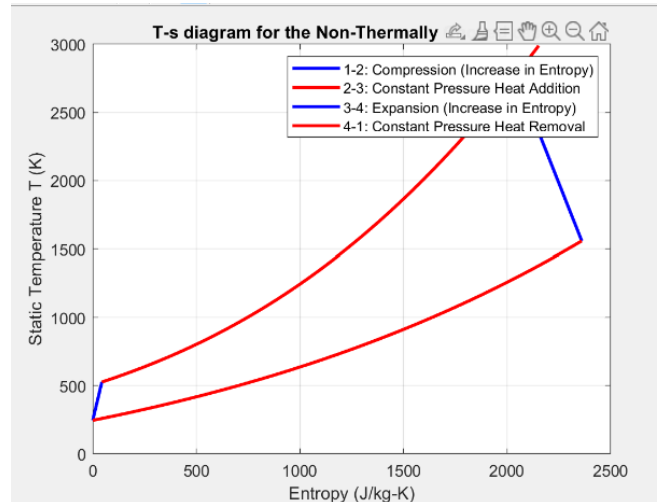


Fig 2: Non-Thermally Choked Test case

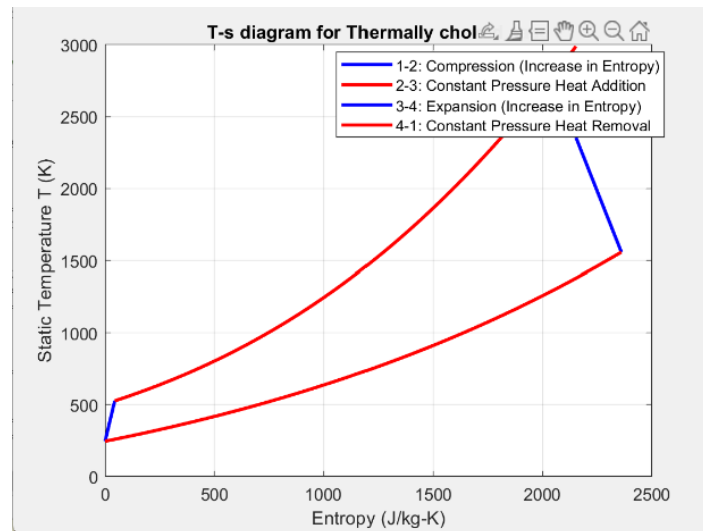


Fig 3: Thermally Choked Test case

## Problem B:

Comparing  $p(z)$  and  $T(z)$  from module1 with results from International Standard Atmosphere.

From module 1, we get equations:

Where  $T_s=288K$ ,  $P_s=101.3kPa$ ,  $\Gamma=1.4$  and  $z^*=8404$

$$\frac{T_1}{T_s} \equiv \frac{T(z)}{T_s} = \left[ 1 - \frac{\Gamma-1}{\Gamma} (z/z^*) \right]$$
$$\frac{p_1}{p_s} \equiv \frac{p(z)}{p_s} = \left[ 1 - \frac{\Gamma-1}{\Gamma} (z/z^*) \right]^{\frac{\Gamma}{\Gamma-1}}$$

**For Altitudes  $z < 7958m$ :**

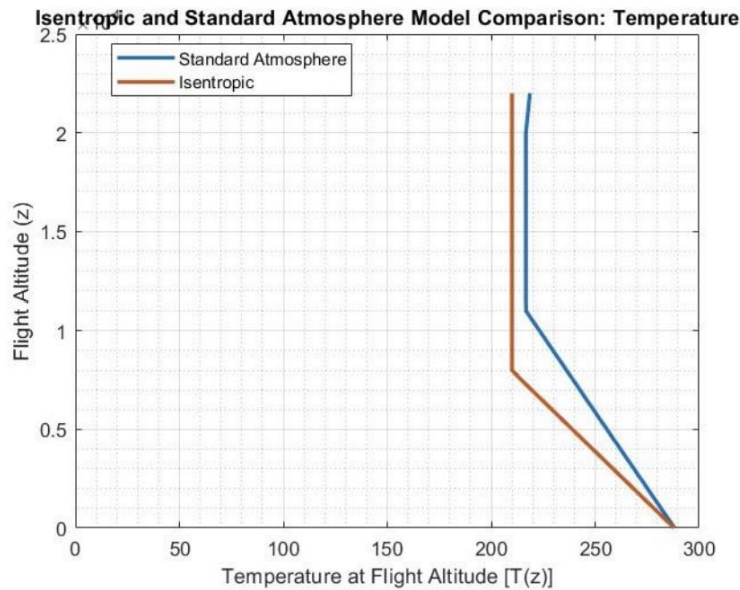


Fig 4 Isentropic VS ICAO model: Temperature

As seen in the graph, we can see temperatures exhibit comparable characteristics for altitudes above 1100m, and below 300m they exhibit strong association.

So, we can say that the isentropic model for temperature can be deemed suitable for analysis.

Based on the pressure comparison graph between the ICAO and Isentropic models, it is evident that these models exhibit a strong association, with only minimal variations. Therefore, with confidence, it can be asserted that the Isentropic model for pressure is suitable for analytical purposes.

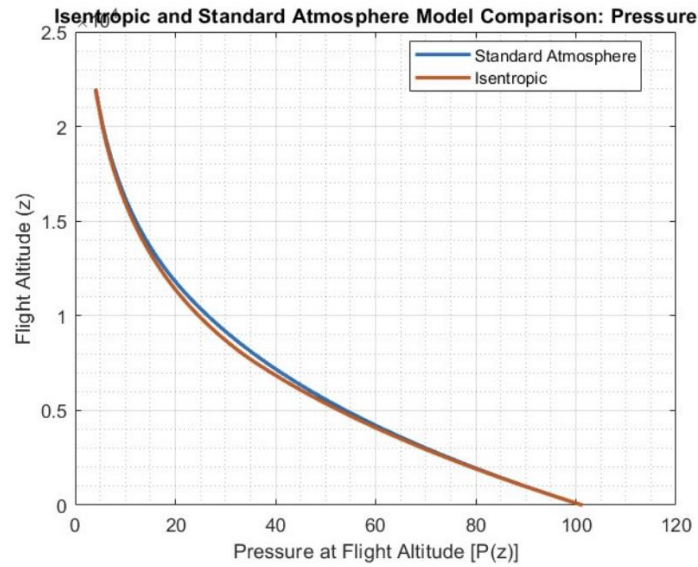


Fig 5: Isentropic Vs ICAO model : Pressure

## Problem C

Using same input parameters as in unchoked validation case, we can vary  $0.8 < M_1 < 5$  in small steps we determine:

### 1. The Overall Efficiency $\eta_o$

Given that this propulsion system is a RAMJET, it can be deduced that its efficiency is notably high only when the operational Mach number exceeds 1, indicating supersonic conditions. This heightened efficiency is attributed to the absence of a compressor, a feature absent in conventional jet engines designed for subsonic operations. To ensure optimal performance, the RAMJET requires inlet pressure ratios in the diffuser well surpassing 40. Achieving such ratios is contingent upon harnessing the "RAM" effect generated at speeds substantially exceeding sonic speed, specifically with Mach numbers greater than 1.5

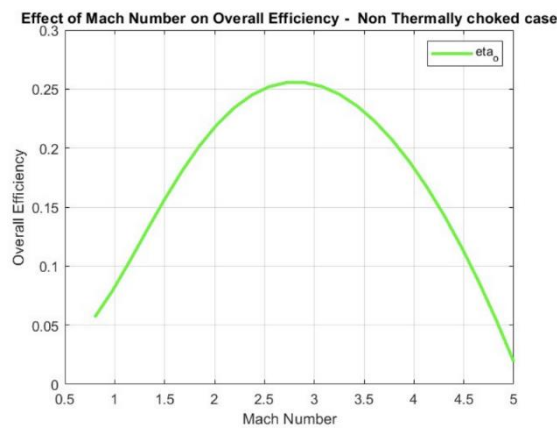


Fig 6 Mach # VS  $\eta_o$

### 2. The Thrust T

From graph we can see that thrust is proportional to mach number, as seen in mach number 4.5 the thrust is highest showing peak value at 39kN.

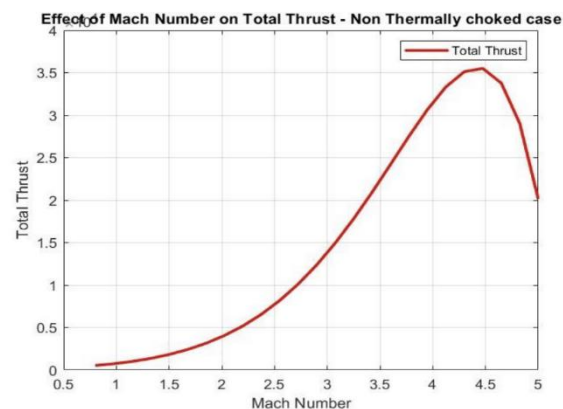


Fig 7 Mach 3 VS Thrust



### 3. TSFC

The graph indicates a low Thrust-Specific Fuel Consumption (TSFC) at low Mach numbers, demonstrating efficiency at lower speeds. As Mach numbers increase, the TSFC rises in a quadratic fashion, reaching a peak value at the highest Mach number, suggesting a notable change in efficiency with varying speeds.

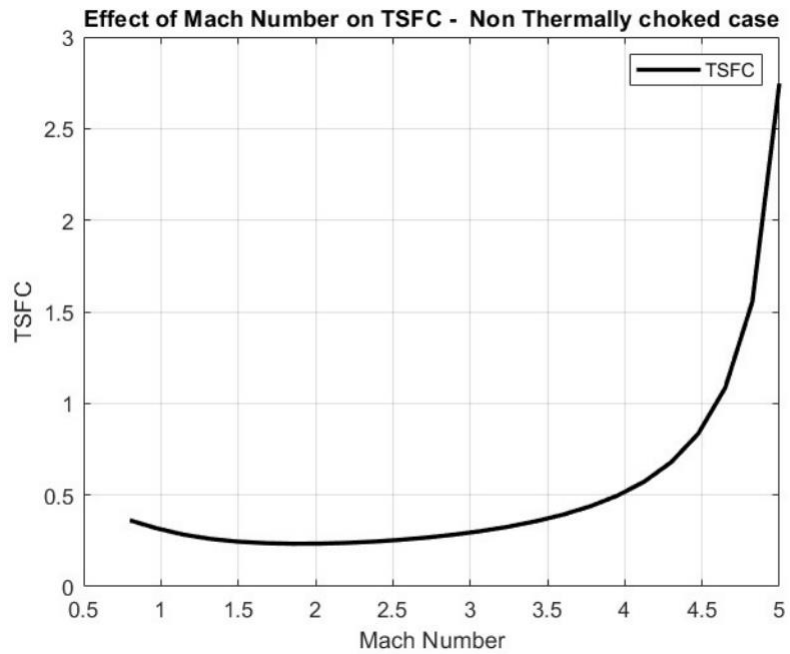


Fig 8 Mach # VS TSFC

## Problem D

Using same inputs parameters used in unchoked case, varying flight altitude  $z$  in small strps from 2000m to 30000m to determine:

### 1. The Overhaul Efficiency $\eta_o$

The highest overall efficiency is observed at the initial lowest altitude of  $z = 2000\text{m}$ . It experiences a continuous linear decline as the altitude increases until reaching  $z = 7958\text{ m}$ . Beyond this point, the overall efficiency remains constant despite further increases in altitude.

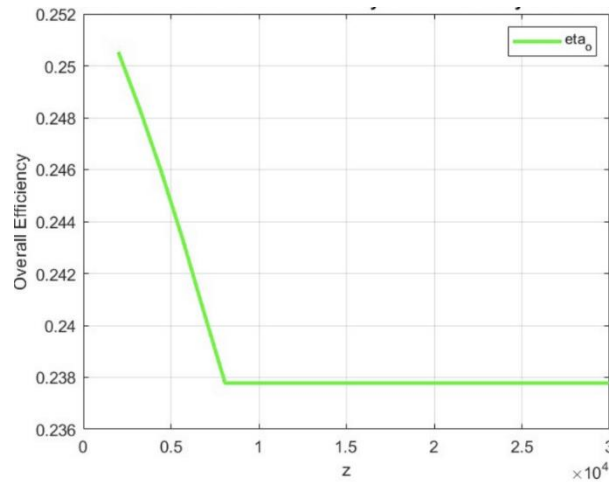


Fig 9 Altitude VS  $\eta_o$

### 2. The total thrust (T)

exhibits a gradual decrease with the ascent of flight altitude ( $z$ ). This phenomenon is likely attributed to the reduced air density at higher altitudes, resulting in a lower mass flow rate of ambient air into the diffuser.

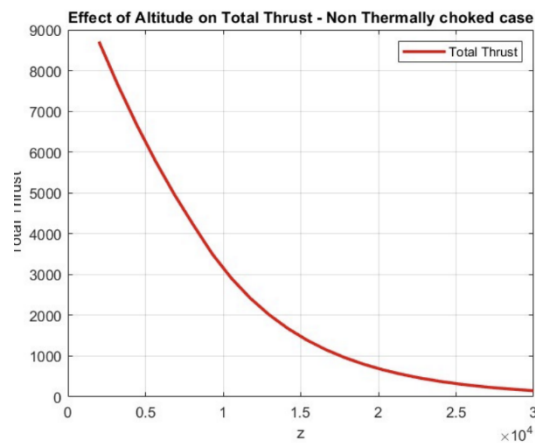


Fig 10 Altitude VS Thrust

### 3. TSFC

We can see that TSFC is the same as overall efficiency.

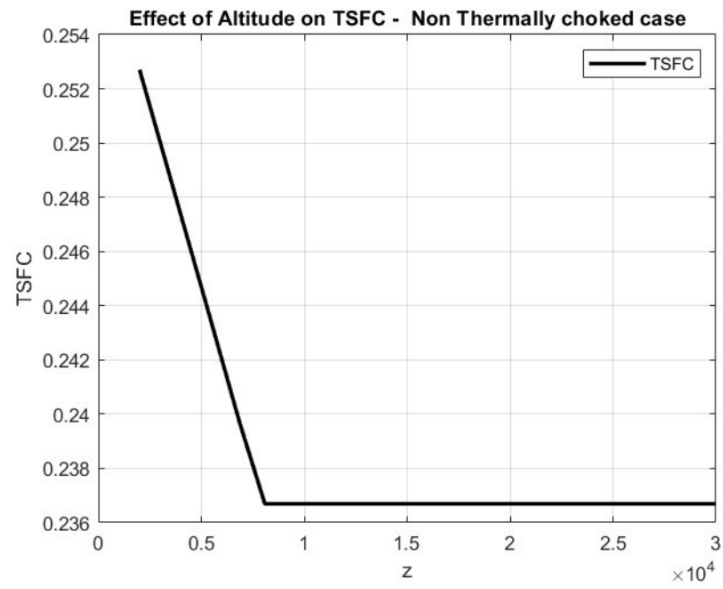


Fig 11 Altitude VS TSFC

## Problem E

Using same input in unchoked case, where  $2000\text{m} < z < 20000\text{m}$  in steps of 500m and for each  $z$  value systematically vary  $M_1$  to find the flight Mach number that:

1. Maximizes the overall efficiency  $\eta_o$

The overall efficiency remains constant irrespective of altitude variation after  $z=7985\text{m}$ .

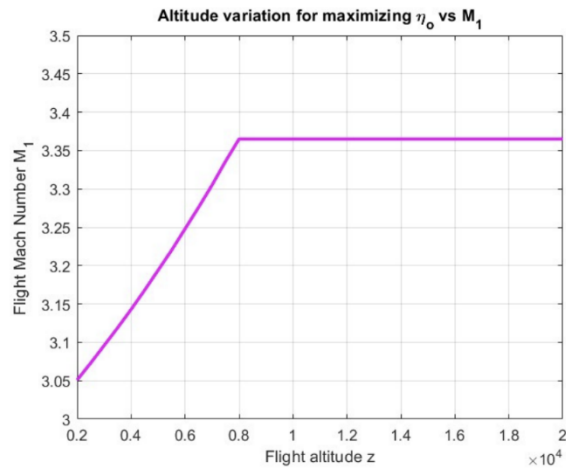


Fig 12 Altitude VS Mach #  $M_1$

2. Minimizes the TSFC

As seen from the following graph, the flight Mach number that minimizes the TSFC has a steep decline at the altitudes ranging from 2000 m and 4000 m.

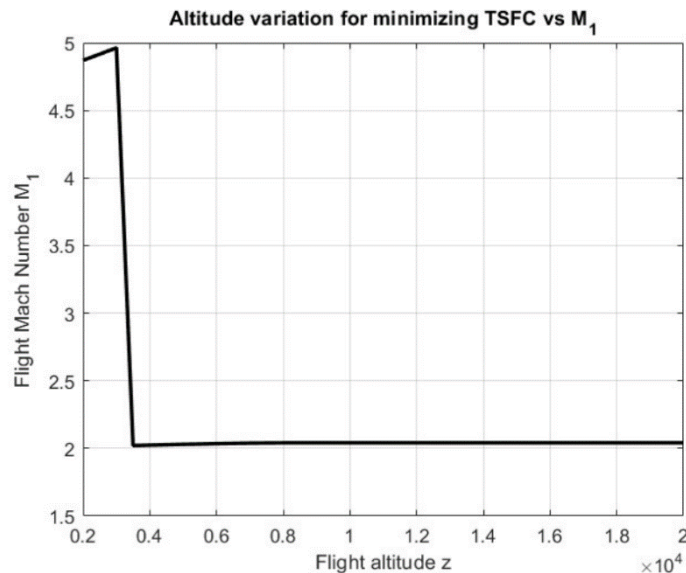


Fig 13 Altitude VS Mach #  $M_1$

## Problem F

Using same parameters as in unchoked case, including  $z=4300\text{m}$  and  $M1=2.4$ , but systematically vary the inlet/diffuser efficiency from  $0.5 < \eta_d < 1$  in steps of 0.05 to compute:

### 1. The Overall Efficiency $\eta_o$

As depicted in the graph below, the maximum overall efficiency, reaching 0.257, aligns with a diffuser efficiency of 1.0. This correlation is attributed to the presence of isentropic conditions at  $\eta_d = 1$ , signifying the absence of irreversibility's under these conditions.

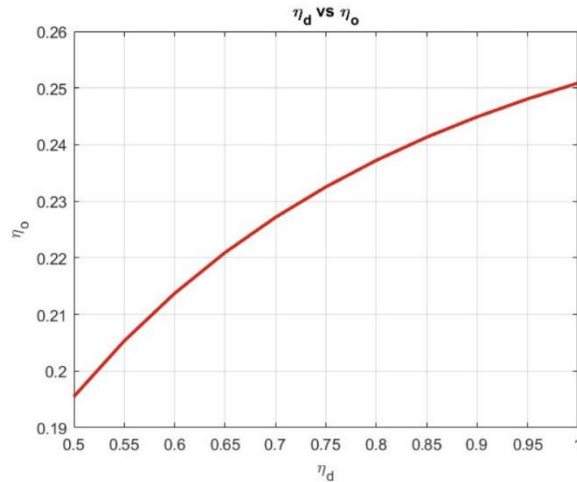


Fig 14  $\eta_d$  VS  $\eta_o$

### 2. The Thrust T

The graph illustrates a notable rise in total thrust output as the efficiency of the diffuser ( $\eta_d$ ) increases. Specifically, at the lowest specified efficiency of the diffuser ( $\eta_d = 0.5$ ), the total thrust is recorded at 2000 N.

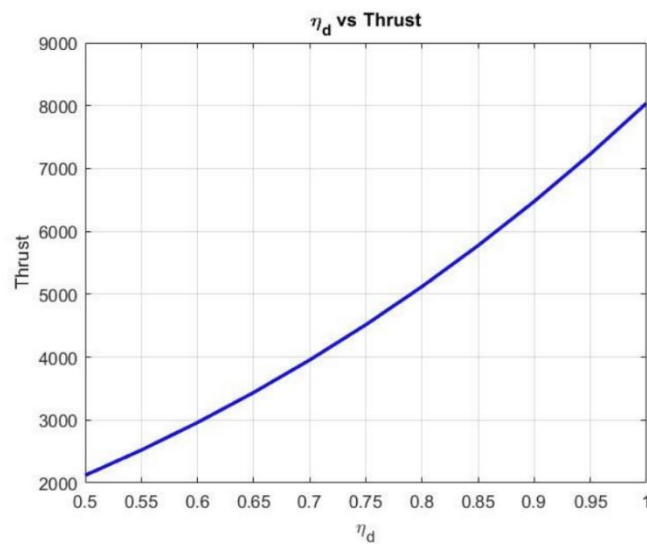


Fig 15  $\eta_d$  VS Thrust

### 3. TSFC

TSFC gradually decreases with increasing efficiency of diffuser.

The value of TSFC is highest at efficiency of diffuser is 0.5 and lowest thrust at efficiency of diffuser at 1.

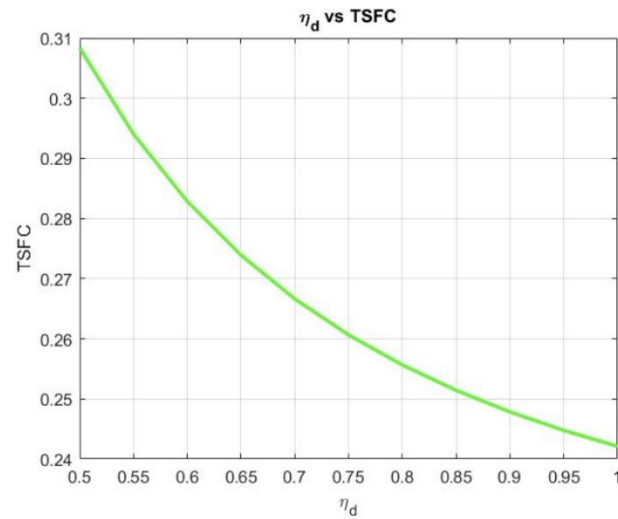


Fig 16  $\eta_d$  VS TSFC

## Problem G

We use same input parameters as in unchoked case, including  $z=4300\text{m}$  and  $M_1=2.4$ , but now systematically vary the nozzle efficiency from  $0.5 < \eta_n < 1$  in steps of 0.05 to compute the resulting:

### 1. The Overall Efficiency $\eta_o$

As we can see by examining the graph, the overall efficiency is largest when nozzle efficiency is equal to 1, this means irreversibility does not exist at isentropic conditions.

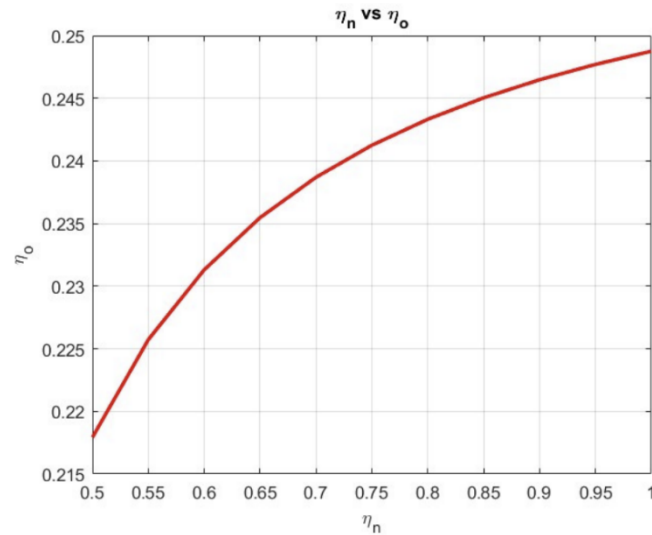


Fig 17  $\eta_n$  VS  $\eta_o$

### 2. The Thrust T,

From the graph, we get to know that nozzle efficiency is highest at thrust 7500N and lowest thrust 3257N is at smallest nozzle efficiency 0.44.

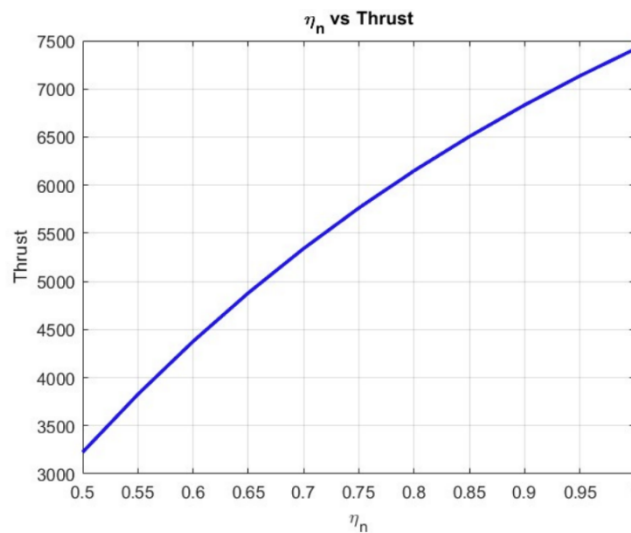


Fig 18  $\eta_n$  VS Thrust

### 3. TSFC

From the graph we know that TSFC at 0.28 is highest at nozzle efficiency 0.5 where it's the lowest, and highest nozzle efficiency gives out lowest value of TSFC.

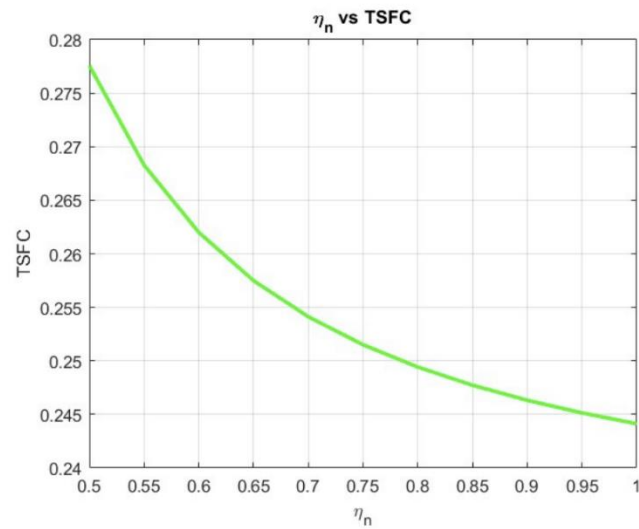


Fig 19  $\eta_n$  VS TSFC



## Problem H

Now using same input parameters as unchoked case, including  $z=4300$  m and  $M_1=2.4$ , but systematically vary Mach number  $M_2$  from  $0.1 < M_2 < 2.5$  in steps of 0.1 to compute the resulting:

1. The Overall Efficiency  $\eta_o$
2. Observing the graph, it is evident that the overall efficiency experiences a steep decline and even turns negative as the combustor inlet Mach Number ( $M_2$ ) surpasses 0.6. This abrupt change may be attributed to the potential occurrence of engine flameout at supersonic speeds.

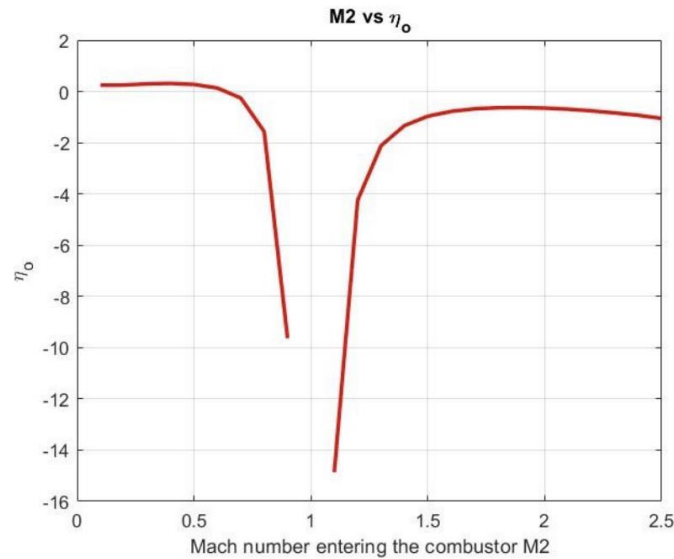


Fig 20 Variation of Overall Efficiency for  $M_2$

3. The Thrust  $T$

As seen on graph, the thrust spikes and decreases as combustor inlet Mach # goes after 0.3.

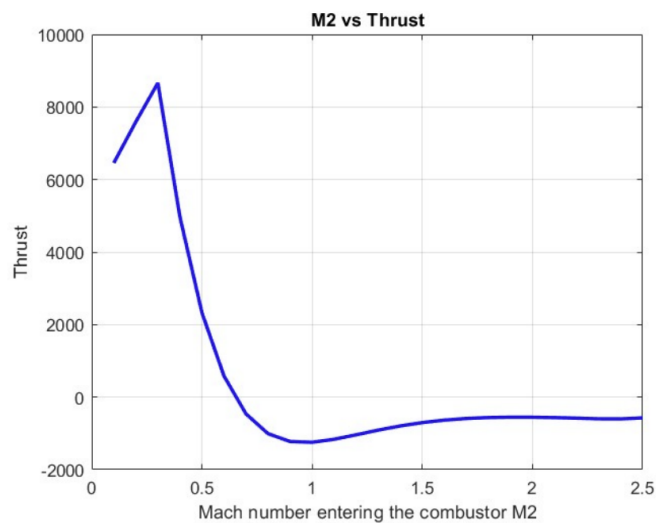


Fig 21 Variation of Thrust for  $M_2$

#### 4. TSFC

The graph depicting  $M_2$  vs. TSFC reveals a decreasing trend up to 0.45, followed by a steep increase beyond  $M_2 = 0.5$ , and then a sharp decrease.

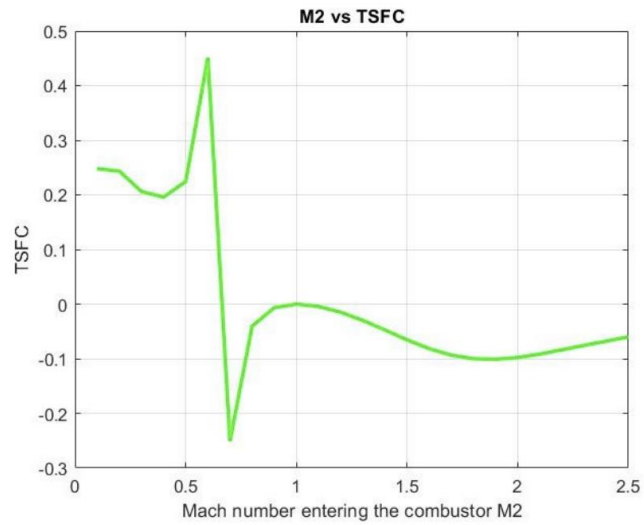


Fig 22 Variation of TSFC for  $M_2$

## Problem I

Using parametric analysis tool developed to design ram/scramjet propulsion system, we need to develop for hypersonic flight at  $M_1 = 5$  and  $z = 90,000\text{ft}$  (27,400m) with same fuel heating value and inlet/ diffuser and nozzle efficiencies as in validation cases.

It is required that to limit combustor exit total temperature to  $T_{t3\text{max}} < 2400\text{K}$ , it is to find two optimal design, one that produces the maximum positive thrust and second that maximizes the overall efficiency.

1. Determination of optimal system that maximizes the thrust:

We get values:

1. Diffuser exit Mach # = 0.41
2.  $T_{t3} = 2460\text{K}$
3. Thrust  $N = 1972.5\text{ N}$

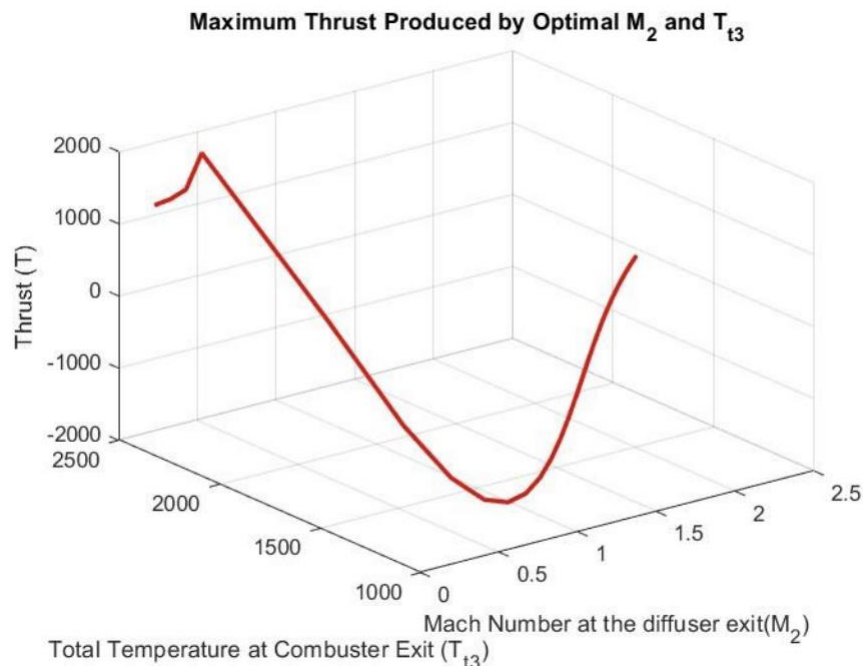


Fig 23 Optimized Thrust

2. Determination of optimal system that maximizes overall efficiency.

We get values:

1. Diffuser Exit Mach# = 0.40
2.  $T_{t3} = 2439\text{K}$
3. Overall Efficiency = 0.1401

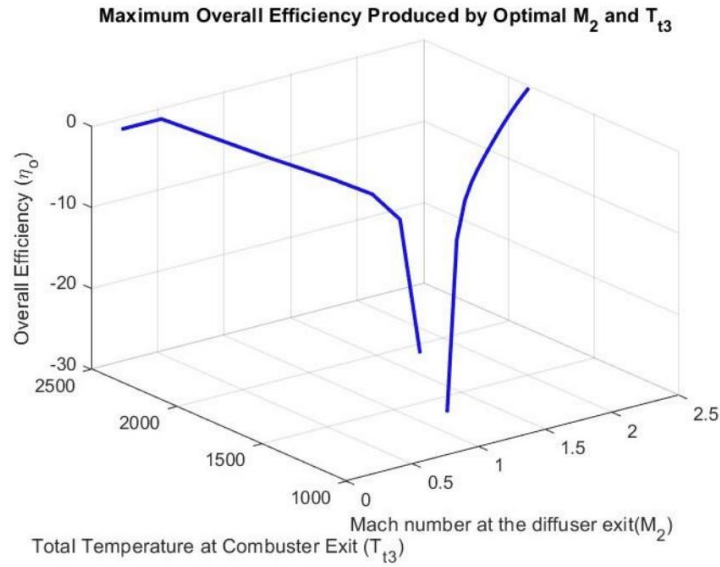


Fig 23 Optimized Overall Efficiency

## Conclusion:

This research project delves deep into the intricate interplay between engine operating conditions and thermodynamic constraints, shedding light on the profound influence they exert on the performance of the RAMJET propulsion system. By meticulously analyzing key performance parameters like Overall Efficiency, Total Thrust, and Thrust-Specific Fuel Consumption (TSFC), we gain invaluable insights into the nuanced dynamics that shape the system's capabilities. The significance of these parameters varies, contingent upon the specific mission requirements, emphasizing the need for a nuanced and context-dependent evaluation.

Moreover, practical limitations further underscore the complexity of the RAMJET propulsion system. The imposed material constraint, for instance, acts as a critical factor preventing the maximum total temperature ( $T_{t3\_max}$ ) from surpassing 2400. This constraint introduces a unique set of challenges and restrictions, particularly when assessing the system's performance under exceptionally high  $T_{t3}$  values. Navigating these limitations becomes integral to a comprehensive understanding of the RAMJET propulsion system's capabilities and feasibility in real-world applications.

## Appendix:

*Function statements used to derive each module:*

### Module 1

```
function [P1, T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1, z,z_star)
gamma = 1.4;
z=4300;
R=286.7;
Z_star=8404;
if z < 7958
    Ts = 288;
    Ps = 101.3;

    Cp1 = (gamma*R)/(gamma - 1);
    part1 = (1 - ((gamma - 1)/gamma)*(z/z_star));
    T1 = Ts * part1; % Temperature 1
    P1 = Ps * part1^((gamma)/(gamma - 1)); % Pressure 1
    part2 = (1 + ((gamma - 1)/2).*M1.^2);
    Tt1 = T1 * part2;
    Pt1 = P1 * part2^((gamma)/(gamma - 1));
    a1 = sqrt(gamma*R * T1);
    V1 = a1 .* M1;

else
    Cp1 = (gamma*R)/(gamma - 1);
    T1 = 210 ;
    P1 = 33.6.*exp(-1.*((z-7958)./6605));
    Tt1 = T1.*(1+((gamma-1)/2).*M1.^2);
    Pt1 = P1.*(1+((gamma-1)/2).*M1.^2).^(gamma./(gamma-1));

    a1 = sqrt(gamma*R * T1);
    V1 = a1 .* M1;

end
```

### Module2

```
function [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1, eta_d,Tt1,P1,Pt1)
gamma = 1.4;
Cp2 = R*gamma/(gamma-1);
Tt2 = Tt1;
T2 = Tt2/(1+((gamma-1)/2)*M2^2);
Pt2 = P1*(1+eta_d*((gamma-1)/2).*M1.^2).^(gamma/(gamma-1));
P2 = Pt2/(1+((gamma-1)/2)*M2^2)^(gamma/(gamma-1));
deltaS12 = Cp2*log(Tt2/Tt1)-R*log(Pt2/Pt1);
a2 = sqrt(gamma*R*T2);
V2 = M2*a2;
end
```

### Module 3

```
function [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12)
gamma = 1.3;
Tt3_choked = Tt2*((1/(2*gamma+2))*(1/(M2.^2))*((1+gamma*M2.^2)^2)*(1+((gamma-1)/2)*M2^2)^-1);

if Tt3_choked < Tt3_max % Thermally Choked
    M3 = 1;
    Tt3 = Tt3_choked;
else % Thermally Unchoked
    Tt3 = Tt3_max;
    C = (Tt3/Tt2)*(M2^2)*((1 + ((gamma - 1)/2)*M2^2)/((1 + gamma*(M2^2))^2));

    % Solving quadratic
```

```

a = C*gamma^2 - (gamma-1)/2;
b = 2*C*gamma - 1;
c = C;

M3_1 = sqrt((-b+sqrt(b.^2-4*a*c))/(2*a));
M3_2 = sqrt((-b-sqrt(b.^2-4*a*c))/(2*a));

    if M2 < 1 && M3_1 > M2 && M3_1 <= 1
        M3 = M3_1;
    else
        M3 = M3_2;
    end
end
% Find specific heats using specific heat model as given
A = 986;
B = 0.179;
q23 = A*(Tt3-Tt2)+0.5*B*(Tt3^2 - Tt2^2);

% Constant Pressure Combustion
P3 = P2;

% Total to static relations
T3 = Tt3/(1+((gamma-1)/2)*M3^2);
Pt3 = P3*(1+((gamma-1)/2)*M3^2)^(gamma/(gamma-1));

% Velocity at exit of combustor
a3 = sqrt(gamma*R*T3);
V3 = M3*a3;

% Entropy Increase
Cp = A + B*T3;
Cp3 = Cp;
deltaS23 = Cp3*log(Tt3/Tt2) - R*log(Pt3/Pt2);
deltaS13 = deltaS12 + deltaS23;

end

Module 4
function [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test]
=module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23)
gamma = 1.3;
P_ratio = P1/Pt3;
M_Test = ((2/(gamma-1))*(eta_n*(1-(P_ratio)^((gamma-1)/gamma)))...
/(1-eta_n*(1-(P_ratio)^((gamma-1)/gamma))))^0.5;
if M_Test < 1
    Me = M_Test;
    Pe = P1;
else
    Me = 1;
    Pe = Pt3*(1-(1/eta_n)*((gamma-1)/(gamma+1)))^(gamma/(gamma-1));
end
Tte = Tt3; % From First Law

% Total to Static Relations
Te = Tte/(1+((gamma-1)/2)*(Me^2));
Pte = Pe*(1+((gamma-1)/2)*Me^2)^(gamma/(gamma-1));

% Velocity
ae = sqrt(gamma*R*Te);
Ve = Me*ae;

% Exit Mass Flow
mdot_exit = Pe*Ve*Ae*1000/(R*Te);

% Entropy Increase
Cp = 986+0.179*Te;
Cpe = Cp;
deltaS3e = Cp*log(Tte/Tt3)-R*log(Pte/Pt3);

```

```

    deltaS1e = deltaS3e + deltaS23 + deltaS12;

end
Module 5
function [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e)

P4 = P1;% Because P4 = P1
Tt4 = Tte; % From the 1st law of thermodynamics
gamma = 1.3;

if M_Test < 1
    etan_e = 1;
else
    etan_e = M_Test^(-0.3);
end
T4 = Tte * (1 - (etan_e*(1 - (P1/Pte)^((gamma -1)/gamma))));
M4 = sqrt((2/(gamma - 1)) * ((Tt4/T4)-1));
Pt4 = P4 * (1 + ((gamma -1)/2)*M4^2)^(gamma/(gamma-1));
a4 = sqrt(gamma*R*T4);
V4 = a4 * M4;
Cp4 = 986 + 0.179*T4;
deltaS4e = Cp4*log(Tt4/Tte) - R*log(Pt4/Pte);
deltaS41 = deltaS1e + deltaS4e;

end

```

## Module 6

```

function [T,Tj,Tp,TSFC,Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o,Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae)
g = 9.81; % acceleration due to gravity
mdot_in = mdot_exit/(1+q23/qf);
mdot_f = mdot_exit - mdot_in;
f = mdot_f/mdot_in;
% Thrust
Tj = mdot_in*((1+f)*Ve - V1);
Tp = (Pe-P1)*Ae*1000;
T = Tj + Tp;
% Thrust Specific Fuel Consumption
TSFC = mdot_f*3600./T;
% Specific Impulse
Isp = T./(mdot_f*g);
% Equivalent Velocity
Veq = Ve + (Pe-P1)*1000*Ae/mdot_exit;
% Thermal Efficiency
eta_th = ((mdot_exit*0.5*Veq.^2) - (mdot_in*0.5*V1.^2))./(mdot_in*q23);
% Propulsive Efficiency
eta_prop = 2/(1+Veq/V1);
% Overall Efficiency
eta_o = eta_th*eta_prop;
% Propulsive Power
Propulsive_Power = T.*V1; % In Watts
end

```



#### MAIN CODE USED:

```
R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z_star = 8404;
eta_d = 0.92;
M1 = 2.4;
M2 = 0.15;
Tt3_max = 2400;
Ae = 0.015;
eta_n = 0.94;
qf = 43.2e6;
% Module. 1
% Determination of the quantities at the inlet of the diffuser
z = input('Please enter the flight altitude in meters');

%% Computation of the outputs for the module 1
[P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1,z,z_star);

%% computation of the outputs for the module 2

[P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1,eta_d,Tt1,P1,Pt1);

%% computation of the outputs for the module 3

[P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12);
%% computation of the outputs for the module 4

[Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
%% computation of the outputs for the module 5
[P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);

%% computation of the outputs for the module 6
% heating value of the fuel
[T,Tj,Tp,TSFC,Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o,Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);
```

## Problem A

### 1. Non-Thermally choked Test Case

```
clear; close all; clc

% Defining the constants
R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z_star = 8404;
eta_d = 0.92;
M1 = 2.4;
M2 = 0.15;
Tt3_max = 2400;
Ae = 0.015;
eta_n = 0.94;
qf = 43.2e6;
% Module. 1
% Determination of the quantities at the inlet of the diffuser
z = input('Please enter the flight altitude in meters');

%% Computation of the outputs for the module 1
[P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1,z,z_star);

%% computation of the outputs for the module 2
[P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1,eta_d,Tt1,P1,Pt1);

%% computation of the outputs for the module 3
[P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,R,Tt2,P2,Pt2,M2,R,deltaS12);
%% computation of the outputs for the module 4
[Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
%% computation of the outputs for the module 5
[P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);

%% computation of the outputs for the module 6
% heating value of the fuel
[T,Tj,Tp,TSFC,Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o,Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);

%% Part b

%% Part C
M1 = linspace(0.8,5,24);

for m = 1 : length(M1)
    [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1(m),z,z_star);
    [P2,T2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1(m),eta_d,Tt1,P1,Pt1);
    [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,R,Tt2,M2,P2,Pt2,deltaS12);
    [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
    [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
    [T(m),Tj,Tp,TSFC(m),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o(m),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);
end
figure(5)
plot(M1, T, 'Linewidth',2, 'Color','r');
grid ON
xlabel('Mach Number');
ylabel('Total Thrust');
title('Effect of Mach Number on Total Thrust - Non Thermally choked case');
legend('Total Thrust');
```

```

figure(6)
plot (M1, eta_o, 'Linewidth',2,'Color','g');
grid ON
xlabel('Mach Number');
ylabel('Overall Efficiency');
title('Effect of Mach Number on Overall Efficiency - Non Thermally choked case');
legend('eta_o');
figure(7)
plot(M1, TSFC, 'Linewidth',2,'Color','k');
grid ON
xlabel('Mach Number');
ylabel('TSFC');
title('Effect of Mach Number on TSFC - Non Thermally choked case');
legend('TSFC');

```

## 2. Thermally Chocked Test Case

```

3. clear; close all; clc;
4.
5. % Defining the constants
6.
7. R = 286.9; % gas constant in KJ/ Kg-K
8. gamma = 1.4;
9. z = 4300;
10. z_star = 8404;
11. eta_d = 0.92;
12. M1 = 2.4;
13. M2 = 0.4;
14. Tt3_max = 2400;
15. Ae = 0.015;
16. eta_n = 0.94;
17. qf = 43.2e6;
18.
19. [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1,z,z_star);
20. [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1,eta_d,Tt1,P1,Pt1);
21. [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12);
22. [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
    module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
23. [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
24. [T,Tj,Tp,TSFC,Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o,Propulsive_Power] =
    module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);
25.
26. plot([0, deltaS12], [T1 T2], 'b-', 'LineWidth',2)
27. hold on
28.
29. T23(1) = T2(1);
30. S23 = linspace(deltaS12,deltaS13,100000);
31. ds = deltaS13(1)/100000;
32. for n = 1:length(S23)
33.     if n + 1 == length(S23) + 1
34.         break
35.     end
36.     T23(n+1) = T23(n) + (T23(n)/(986+0.179*T23(n)))*ds;
37.     % if T23(n) >= T3(1)
38.     % break
39.     % end
40. end
41. S23 = linspace(deltaS12,deltaS13,length(T23));
42. plot(S23, T23, 'r-', 'LineWidth',2);
43.
44. plot([deltaS13 deltaS41], [T3 T4], 'b-', 'LineWidth',2)
45. hold on
46.
47. T41(1) = T1(1);
48. S41 = linspace(0,deltaS41,100000);
49. ds = deltaS41(1)/100000;
50. for n = 1:length(S41)
51.     if n + 1 == length(S41) + 1

```

```

52.         break
53.     end
54. T41(n+1) = T41(n) + (T23(n)/1004)*ds;
55.     if T41(n) >= T4(1)
56.         break
57.     end
58. end
59. S41 = linspace(0,deltaS41,length(T41));
60. plot(S41, T41, 'r-','LineWidth',2)
61. hold on
62. grid on
63. title('T-s diagram for Thermally choked case')
64. xlabel('Entropy (J/kg-K)')
65. ylabel('Static Temperature T (K)')
66. legend('1-2: Compression (Increase in Entropy)','2-3: Constant Pressure Heat Addition','3-4:
Expansion (Increase in Entropy)','4-1: Constant Pressure Heat Removal','Location','Best');

```

### Problem B

```

clear; close all; clc;

% Defining the constants
R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z_star = 8404;
eta_d = 0.92;
M1 = 2.4;
M2 = 0.4;
Tt3_max = 2400;
Ae = 0.015;
eta_n = 0.94;
qf = 43.2e6;

% defining the altitude
z = [0:500:20000 22000] ;

for i = 1:length(z)
    [P1(i),T1(i),Cp1(i),Tt1(i), Pt1(i), a1(i), V1(i)] = module1(R,M1,z(i),z_star);
end

data = readtable('Validation of Atmospheric Model.xlsx','Range','G14:H55');
T_z = table2array(data(:,1));
P_z = table2array(data(:,2));

figure(1)
plot(T_z,z,'LineWidth',2);
xlim([0 300]);
hold on;
plot(T1,z,'LineWidth',2);
title('Isentropic and Standard Atmosphere Model Comparison: Temperature')
legend('Standard Atmosphere','Isentropic','Location','Best')
xlabel('Temperature at Flight Altitude [T(z)]')
ylabel('Flight Altitude (z)')
grid on;
grid minor;

figure(2)
plot(P_z,z,'LineWidth',2);
hold on;
plot(P1,z,'LineWidth',2);
title('Isentropic and Standard Atmosphere Model Comparison: Pressure')
legend('Standard Atmosphere','Isentropic','Location','Best')
xlabel('Pressure at Flight Altitude [P(z)]')
ylabel('Flight Altitude (z)')
grid on;
grid minor;

```

### Problem C

```
clear; close all; clc;

% Defining the constants
R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z_star = 8404;
eta_d = 0.92;
M2 = 0.15;
Tt3_max = 2400;
Ae = 0.015;
eta_n = 0.94;
qf = 43.2e6;
z = 4300;
M1 = linspace(0.8,5,25);

for m = 1 : length(M1)
    [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1(m),z,z_star);
    [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1(m),eta_d,Tt1,P1,Pt1);
    [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12);
    [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
    [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
    [T(m),Tj,Tp,TSFC(m),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o(m),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);
end

figure(1)
plot(M1, T, 'Linewidth',2, 'Color', 'r');
grid ON
xlabel('Mach Number');
ylabel('Thrust');
title('Effect of Mach Number on Engine Thrust - Thermally Unchoked Case');
legend('Total Thrust');

figure(2)
plot (M1, eta_o, 'Linewidth',2,'Color','b');
grid on
xlabel('Mach Number');
ylabel('Overall Efficiency');
title('Effect of Mach Number on Overall Efficiency- Thermally Unchoked Case');
legend('Overall Efficiency');

figure(3)
plot(M1, TSFC, 'Linewidth',2,'Color','g');
grid on
xlabel('Mach Number');
ylabel('TSFC');
title('Effect of Mach Number on TSFC- Thermally Unchoked Case');
legend('TSFC');
```

### Problem D

```
clear; close all; clc;

% Defining the constants
R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z_star = 8404;
eta_d = 0.92;
M2 = 0.15;
Tt3_max = 2400;
```

```

Ae = 0.015;
eta_n = 0.94;
qf = 43.2e6;
M1 = 2.4;

z = linspace(2000,3e4,24);
for zz = 1 : length(z)
    [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1,z(zz),z_star);
    [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1,eta_d,Tt1,P1,Pt1);
    [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12);
    [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
    [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
    [T(zz),Tj,Tp,TSFC(zz),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o(zz),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);
end

figure(8)
plot(z, T,'Linewidth',2,'Color','r');
grid ON
xlabel('z');
ylabel('Total Thrust');
title('Effect of Altitude on Total Thrust - Non Thermally choked case');
legend('Total Thrust');

figure(9)
plot(z, eta_o, 'Linewidth',2,'Color','g');
grid ON
xlabel('z');
ylabel('Overall Efficiency');
title('Effect of Altitude on Overall Efficiency - Non Thermally choked case');
legend('eta_o');

figure(10)
plot(z, TSFC, 'Linewidth',2,'Color','k');
grid ON
xlabel('z');
ylabel('TSFC');
title('Effect of Altitude on TSFC - Non Thermally choked case');
legend('TSFC');

```

### Problem E

```

R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z_star = 8404;
eta_d = 0.92;
M2 = 0.15;
Tt3_max = 2400;
Ae = 0.015;
eta_n = 0.94;
qf = 43.2e6;

% varying the Mach number M1
M1 = 0.8:0.001:5;

% varying the altitude from 2000 m to 20,000 m
z = 2e3:500:2e4;

for i = 1 : length(z)
    for j = 1 : length(M1)
        [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1(j),z(i),z_star);
        [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1(j),eta_d,Tt1,P1,Pt1);
        [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12);
        [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
        [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
        [T(i,j),Tj,Tp,TSFC(i,j),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o(i,j),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);
    end
end

```

```

    end
end

for i = 1:length(z)
    [eta_o_max(i),I(i)] = max(eta_o(i,:));
end

figure(1);
plot(z,M1(I),'LineWidth',2,'Color','magenta')
ylim([3 3.5])
title('Altitude variation for maximizing \eta_o vs M_1')
xlabel('Flight altitude z')
ylabel('Flight Mach Number M_1')
grid on;

for i = 1:length(z)
    [TSFC_min(i),J(i)] = min(TSFC(i,:));
end

figure(2);
plot(z,M1(J),'LineWidth',2,'Color','k')
ylim([1.5 5])
title('Altitude variation for minimizing TSFC vs M_1')
xlabel('Flight altitude z')
ylabel('Flight Mach Number M_1')
grid on;

```

### Problem F

```

clear; close all; clc;

% Defining the constants
R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z = 4300;
M1 = 2.4;
z_star = 8404;
M2 = 0.15;
Tt3_max = 2400;
Ae = 0.015;
eta_n = 0.94;
qf = 43.2e6;

% Variation of the isentropic efficiency of the diffuser
eta_d = 0.5 : 0.05 : 1;

for i = 1 : length(eta_d)

    [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1,z,z_star);
    [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1,eta_d(i),Tt1,P1,Pt1);
    [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12);
    [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
    [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
    [T(i),Tj,Tp,TSFC(i),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o(i),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);

end

figure(1);
plot(eta_d,eta_o,'LineWidth',2,'Color','red');
grid on
title('\eta_d vs \eta_o')
xlabel('\eta_d')

```

```

ylabel('\eta_o')
grid on

figure(2);
plot(eta_d,T,'LineWidth',2,'Color','blue')
grid on
title('\eta_d vs Thrust')
xlabel('\eta_d')
ylabel('Thrust')
grid on

figure(3);
plot(eta_d,TSFC,'LineWidth',2,'Color','green')
grid on
title('\eta_d vs TSFC')
xlabel('\eta_d')
ylabel('TSFC')
grid on

```

### Problem G

```

clear; close all; clc;

% Defining the constants

R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z = 4300;
M1 = 2.4;
z_star = 8404;
M2 = 0.15;
Tt3_max = 2400;
Ae = 0.015;
eta_d = 0.92;
qf = 43.2e6;

% Variation of the isentropic efficiency of the nozzle
eta_n = 0.5 : 0.05 : 1;

for i = 1 : length(eta_n)

    [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1,z,z_star);
    [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2,M1,eta_d,Tt1,P1,Pt1);
    [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2,R,deltaS12);
    [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n(i),P1,Tt3,Pt3,R,deltaS12,deltaS23);
    [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
    [T(i),Tj,Tp,TSFC(i),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o(i),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);

end

figure(1);
plot(eta_n,eta_o,'LineWidth',2,'Color','red');
grid on
title('\eta_n vs \eta_o')
xlabel('\eta_n')
ylabel('\eta_o')
grid on

figure(2);
plot(eta_n,T,'LineWidth',2,'Color','blue')
grid on
title('\eta_n vs Thrust')
xlabel('\eta_n')
ylabel('Thrust')

```



```

grid on

figure(3);
plot(eta_n,TSFC,'LineWidth',2,'Color','green')
grid on
title('\eta_n vs TSFC')
xlabel('\eta_n')
ylabel('TSFC')
grid on

Problem H

clear; close all; clc;

% Defining the constants

R = 286.9; % gas constant in KJ/ Kg-K
gamma = 1.4;
z = 4300;
M1 = 2.4;
z_star = 8404;
Tt3_max = 2400;
Ae = 0.015;
eta_d = 0.92;
eta_n = 0.94;
qf = 43.2e6;

% Variation of the Mach number entering the combustor M2
M2 = 0.1 : 0.1 : 2.5;

for i = 1 : length(M2)

    [P1,T1,Cp1,Tt1, Pt1, a1, V1] = module1(R,M1,z,z_star);
    [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2(i),M1,eta_d,Tt1,P1,Pt1);
    [P3,Pt3,T3,Tt3,Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2(i),R,deltaS12);
    [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
    [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
    [T(i),Tj,Tp,TSFC(i),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop,eta_o(i),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve,V1,Pe,P1,Ae);

end

figure(1);
plot(M2,eta_o,'LineWidth',2,'Color','red');
grid on
title('M2 vs \eta_o')
xlabel('Mach number entering the combustor M2')
ylabel('\eta_o')
grid on

figure(2);
plot(M2,T,'LineWidth',2,'Color','blue')
grid on
title('M2 vs Thrust')
xlabel('Mach number entering the combustor M2')
ylabel('Thrust')
grid on

figure(3);
plot(M2,TSFC,'LineWidth',2,'Color','green')
grid on
title('M2 vs TSFC')
xlabel('Mach number entering the combustor M2')
ylabel('TSFC')
grid on

```

## Problem I

```
clear; close all; clc
R = 286.9; % gas constant in KJ/ Kg-K
z = 27400;
z_star = 8404;
M1 = 5;
eta_d = 0.92;
M2 = 0.1:0.01:2.5;
qf = 43.2e6;
Tt3_max = 2400;
eta_n = 0.94;
Ae = 0.015;
% Variation of the Mach number entering the combustor M2
M2 = 0.1 : 0.1 : 2.5;

for i = 1 : length(M2)

    [P1,T1(i),Cp1,Tt1, Pt1, a1, V1(i)] = module1(R,M1,z,z_star);
    [P2,T2,Tt2,Cp2,Pt2,a2,V2,deltaS12] = module2(R,M2(i),M1,eta_d,Tt1,P1,Pt1);
    [P3,Pt3,T3,Tt3(i),Cp3,a3,V3,M3,q23,deltaS23,deltaS13] = module3(Tt3_max,Tt2,P2,Pt2,M2(i),R,deltaS12);
    [Pe,Pte,Te,Tte,Cpe,Me,Ve,ae,deltaS3e,deltaS1e,mdot_exit,M_Test] =
module4(Ae,eta_n,P1,Tt3,Pt3,R,deltaS12,deltaS23);
    [P4,Pt4,T4,Tt4,Cp4,a4,V4,M4,etan_e,deltaS4e,deltaS41] = module5(R,M_Test,Tte,P1,Pte,deltaS1e);
    [T(i),Tj,Tp,TSFC(i),Isp,mdot_f,mdot_in,f,Veq,eta_th,eta_prop(i),eta_o(i),Propulsive_Power] =
module6(q23,qf,mdot_exit,Ve(i),V1(i),Pe,P1,Ae);

end

figure(1)
plot3(M2,Tt3,T,'b-','LineWidth',2,'Color','r');
grid on;
xlabel('Mach Number at the diffuser exit(M_2)');
ylabel('Total Temperature at Combuster Exit (T_t_3)');
zlabel('Thrust (T)');
title('Maximum Thrust Produced by Optimal M_2 and T_t_3');

figure(2)
plot3(M2,Tt3,eta_o,'b-','LineWidth',2,'Color','blue');
grid on;
xlabel('Mach number at the diffuser exit(M_2)');
ylabel('Total Temperature at Combuster Exit (T_t_3)');
zlabel('Overall Efficiency (\eta_o)');
title('Maximum Overall Efficiency Produced by Optimal M_2 and T_t_3');
```