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Assignment 1

AI1110: Probability and Random Variables Indian Institute of Technology Hyderabad

SURBHI CS22BTECH11057

12.13.3.4: Question: In answering a question on a multiple choice test, a student either knows the answer or guesses. Let 3/4 be the probability that he knows the answer and 1/4 be the probability that he guesses. Assuming that a student who guesses at the answer will be correct with probability 1/4. What is the probability that the student knows the answer given that he answered it correctly?

Answer:

$$\frac{12}{13}$$

Solution:

Let E1 be the event that the student knows the answer

E2 be the event that the student guess the answer A be the event that the answer is correct Then,

$$Pr(E_1) = \frac{3}{4} \tag{1}$$

$$Pr(E_2) = \frac{1}{4} \tag{2}$$

$$Pr(\frac{A}{F1}) = 1 \tag{3}$$

 $Pr(A|E_1)$ = probability of correct answer given that he knows

 $Pr(A|E_2)$ = probability of correct answer given that he guesses

$$Pr(\frac{A}{E2}) = \frac{1}{4}$$

that the answer is correct is P(E1/A) By using formula :-

$$Pr(E1|A) = \frac{Pr(E1).Pr(A|E1)}{Pr(E1).Pr(A|E1) + Pr(E2).Pr(A|E2)}$$
(4)

$$Pr(E1|A) = \frac{\frac{3}{4}.1}{\frac{3}{4}.1 + \frac{1}{4}.\frac{1}{4}}$$
 (5)

$$Pr(E1|A) = \frac{\frac{3}{4}}{\frac{3}{4} + \frac{1}{16}}$$
 (6)

$$Pr(E1|A) = \frac{\frac{3}{4}}{\frac{13}{16}} \tag{7}$$

$$Pr(E1|A) = \frac{12}{13} \tag{8}$$

$$Pr(E1|A) = \frac{12}{13}$$

So,12/13 is the probability that the student knows the answer given that he answered it correctly.