

# Assignment 1

AI1110: Probability and Random Variables  
Indian Institute of Technology Hyderabad

SURBHI  
CS22BTECH11057

**12.13.3.4: Question:** In answering a question on a multiple choice test, a student either knows the answer or guesses. Let  $\frac{3}{4}$  be the probability that he knows the answer and  $\frac{1}{4}$  be the probability that he guesses. Assuming that a student who guesses at the answer will be correct with probability  $\frac{1}{4}$ . What is the probability that the student knows the answer given that he answered it correctly?

Therefore, the probability that the student knows the answer given that he answered it correctly is  $\frac{12}{13}$ .

Answer:  $\frac{12}{13}$

Solution: Let  $K$  be the event that the student knows the answer and  $C$  be the event that the student answered the question correctly. We want to find the conditional probability  $\Pr(K|C)$ , which is the probability that the student knows the answer given that he answered correctly.

Parameters	Description	Values
$\Pr(K)$	the student knows the answer	0.75
$\Pr(K^c)$	the student guesses	0.25
$\Pr(C K)$	the student answers correctly given that he knows the answer	1
$\Pr(C K^c)$	the student answers correctly given that he guesses	0.25

TABLE 0: Given Information

We can use Bayes' theorem to find  $\Pr(K|C)$ :

$$\begin{aligned}
 \Pr(K|C) &= \Pr(C|K) \cdot \Pr\left(\frac{C}{K}\right) \\
 &= \Pr(C|K) \cdot \Pr\left(\frac{K}{C|K}\right) \cdot \Pr(K) + \Pr(C|K^c) \cdot \Pr(K^c) \\
 &= 1 \cdot \left(\frac{\frac{3}{4}}{1 \cdot \frac{3}{4} + \frac{1}{4} \cdot \frac{1}{4}}\right) \\
 &= \frac{12}{13}
 \end{aligned}$$