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Experiment No.	2

AIM:	Experiment based on divide and conquer approach
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Program 2

PROBLEM STATEMENT :	<p>For this experiment, you need to implement two sorting algorithms namely Quicksort and Merge sort methods. Compare these algorithms based on time and space complexity. Time required for sorting algorithms can be performed using <code>high_resolution_clock::now()</code> under namespace <code>std::chrono</code>. You have to generate 1,00,000 integer numbers using C/C++ <code>Rand</code> function and save them in a text file. Both the sorting algorithms uses these 1,00,000 integer numbers as input as follows. Each sorting algorithm sorts a block of 100,200,300,...,100000 integer numbers with array indexes numbers <code>A[0..99]</code>, <code>A[100..199]</code>, <code>A[200..299]</code>,..., <code>A[99900..99999]</code>. You need to use <code>high_resolution_clock::now()</code> function to find the time required for 100, 200, 300.... 100000 integer numbers. Finally, compare two algorithms namely Quicksort and Merge sort by plotting the time required to sort integers using LibreOffice Calc/MS Excel. The x-axis of 2-D plot represents the block no. of 1000 blocks. The y-axis of 2-D plot represents the tuning time to sort 1000 blocks of 100,200,300,...,100000 integer numbers.</p>
ALGORITHM/THEORY:	<p>Quick Sort Algorithm:</p> <p>Step 1 – Make the right-most index value pivot</p> <p>Step 2 – partition the array using pivot value</p> <p>Step 3 – quicksort left partition recursively</p> <p>Step 4 – quicksort right partition recursively</p> <p>Quick Sort Partition Algorithm:</p> <p>Step 1 – Choose the highest index value has pivot</p> <p>Step 2 – Take two variables to point left and right of the list excluding pivot</p>

	<p>Step 3 – left points to the low index Step 4 – right points to the high Step 5 – while value at left is less than pivot move right Step 6 – while value at right is greater than pivot move left Step 7 – if both step 5 and step 6 does not match swap left and right Step 8 – if $\text{left} \geq \text{right}$, the point where they met is new pivot</p> <p>Merge Sort Algorithm: Step 1 - If only one element is there then return Step 2 – Find the middle element of the array Step 3 – Recursively call the merge sort for left half of the array. Step 4 – Recursively call the merge sort for right half of the array. Step 5 – Merge the smaller parts of the array in a sorted manner.</p> <p>In order to implement solution for this problem statement I used the rand() function to generate 100000 random numbers in C and saved them to a text file. Then I sorted these numbers using both the algorithms. Alongside, the time taken for sorting each number as also calculated and lastly a graph was plotted in which the Y-axis represents the running time to sort 100 blocks.</p>
PROGRAM:	<pre> #include <stdio.h> #include <stdlib.h> #include <time.h> void merge(int arr[], int p, int q, int r) { int i, j, k; int n1 = q - p + 1; int n2 = r - q; int L[n1], R[n2]; for (i = 0; i < n1; i++) L[i] = arr[p + i]; for (j = 0; j < n2; j++) R[j] = arr[q + 1 + j]; i = 0; j = 0; k = p; while (i < n1 && j < n2) { </pre>

```

if (L[i] <= R[j])
{
arr[k] = L[i];
i++;
}
else
{
arr[k] = R[j];
j++;
}
k++;
}
while (i < n1)
{
arr[k] = L[i];
i++;
k++;
}
while (j < n2)
{
arr[k] = R[j];
j++;
k++;
}
}
void mergeSort(int arr[], int l, int r)
{
if (l < r)
{
int m = l + (r - l) / 2;
mergeSort(arr, l, m);
mergeSort(arr, m + 1, r);
merge(arr, l, m, r);
}
}
int quicksort(int a[], int start, int end)
{

```

```

int pivot = a[end];
int i = (start - 1);
for (int j = start; j <= end - 1; j++)
{
    if (a[j] < pivot)
    {
        i++;
        int t = a[i];
        a[i] = a[j];
        a[j] = t;
    }
}
int t = a[i + 1];
a[i + 1] = a[end];
a[end] = t;
return (i + 1);
}

double quick(int a[], int start, int end)
{
    if (start < end)
    {
        int p = quicksort(a, start, end);
        quick(a, start, p - 1);
        quick(a, p + 1, end);
    }
}

int main()
{
    double qust,mest;
    srand(time(0));
    FILE *fp;
    fp = fopen("random.txt", "w");
    for (int i = 0; i < 100000; i++)
    {
        fprintf(fp, "%d\n", rand() % 100000);
    }
    int upper_limit = 100;

```

```
fclose(fp);
printf("Merge Sort\tQuick Sort\n");
for (int i = 0; i < 1000; i++)
{
    fp = fopen("random.txt", "r");
    int arr1[upper_limit], arr2[upper_limit], temp_num;
    for (int j = 0; j < upper_limit; j++)
    {
        fscanf(fp, "%d", &temp_num);
        arr1[j] = temp_num;
        arr2[j] = temp_num;
    }
    fclose(fp);
    clock_t t;
    t = clock();
    mergeSort(arr2,0,upper_limit-1);
    t = clock() - t;
    mest = ((double)t) / CLOCKS_PER_SEC;
    clock_t t1;
    t1 = clock();
    qust=quick(arr1,0,upper_limit-1);
    t1 = clock() - t1;
    qust = ((double)t1) / CLOCKS_PER_SEC;
    printf("%f\t%f\n", mest, qust);
    fflush(stdout);
    upper_limit += 100;
}
return 0;
}
```

OUTPUT AND RESULT ANALYSIS:

The screenshot shows the OnlineGDB interface. The code editor contains a C program with the following code:

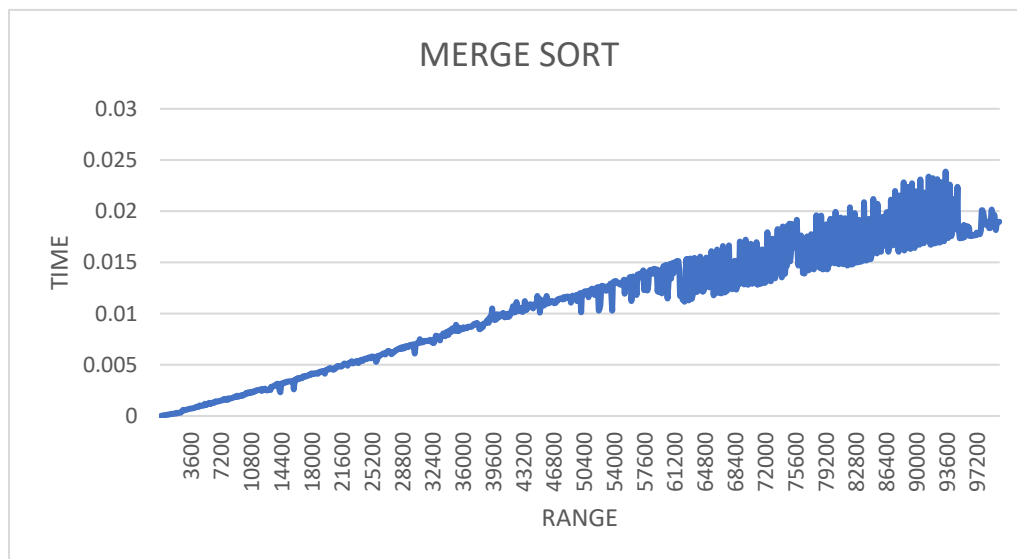
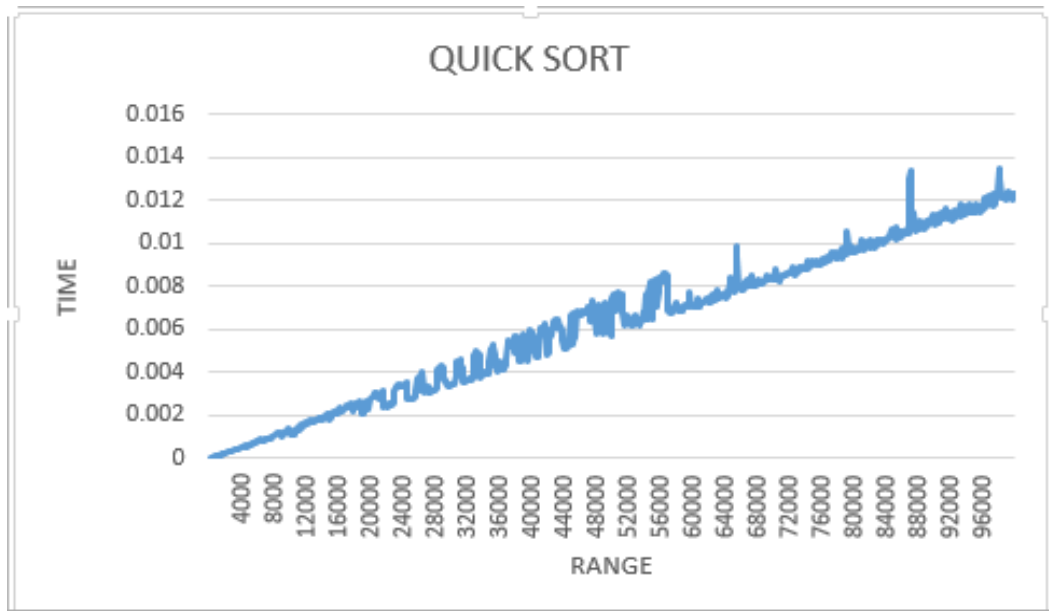
```
1 #include <stdio.h>
2 #include <stdlib.h>
3 #include <time.h>
4 void
5 merge (int arr[], int p, int q, int r)
6 {
7     int i, j, k;
```

The output window displays the following data:

0.014560	0.011001
0.014427	0.010846
0.014412	0.010659
0.014430	0.010605
0.014432	0.010525
0.014417	0.010976
0.014493	0.010680
0.014558	0.010829
0.014509	0.010742
0.014565	0.011140
0.014554	0.010813
0.014614	0.010909
0.014659	0.011001
0.014713	0.010900
0.014663	0.010962
0.014730	0.011153
0.014746	0.011008
0.014742	0.010933
0.015659	0.012616
0.016729	0.012889
0.015668	0.011062

The screenshot shows the OnlineGDB interface. The code editor contains a C program with the following code:

```
1 98613
2 41391
3 7358
4 54505
5 54066
6 47998
7 865
8 53216
9 14413
10 63188
11 32547
12 21188
13 52931
14 29298
15 80669
16 93191
17 65961
18 61706
19 4092
20 23569
21 66125
22 1013
23 41054
24 77659
25 98840
26 69003
27 55132
28 8707
29 44991
```



We observe that quick sort beats merge sort for almost all input sizes i.e. quick sort is quicker and takes less time than merge sort. Time taken by quicksort ranged from 0 to 0.014 whereas for merge sort it ranged from 0 to 0.025.

CONCLUSION:

- Implemented Quick Sort and Merge Sort in c.
- Quick Sort is a in-place sorting algorithm and has Space Complexity of $O(1)$.

	<ul style="list-style-type: none">• For merging of sorted sub-arrays, it needs a temporary array with the size equal to the number of input elements, therefore it has Space Complexity of $O(n)$.• Time Complexity(Average case): Quick Sort – $O(n \log n)$ Merge Sort – $O(n \log n)$
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