

Naïve Bayesian Classification

rec	Age	Income	Student	Credit_rating	Buys_computer
r1	<=30	High	No	Fair	No
r2	<=30	High	No	Excellent	No
r3	31...40	High	No	Fair	Yes
r4	>40	Medium	No	Fair	Yes
r5	>40	Low	Yes	Fair	Yes
r6	>40	Low	Yes	Excellent	No
r7	31...40	Low	Yes	Excellent	Yes
r8	<=30	Medium	No	Fair	No
r9	<=30	Low	Yes	Fair	Yes
r10	>40	Medium	Yes	Fair	Yes
r11	<=30	Medium	Yes	Excellent	Yes
r12	31...40	Medium	No	Excellent	Yes
r13	31...40	High	Yes	Fair	Yes
r14	>40	Medium	No	Excellent	No

X = (age= youth, income = medium, student = yes, credit_rating = fair)

$P(C1) = P(\text{buys_computer} = \text{yes}) = 9/14 = 0.643$
 $P(C2) = P(\text{buys_computer} = \text{no}) = 5/14 = 0.357$
 $P(\text{age}=\text{youth} / \text{buys_computer} = \text{yes}) = 2/9 = 0.222$
 $P(\text{age}=\text{youth} / \text{buys_computer} = \text{no}) = 3/5 = 0.600$
 $P(\text{income}=\text{medium} / \text{buys_computer} = \text{yes}) = 4/9 = 0.444$
 $P(\text{income}=\text{medium} / \text{buys_computer} = \text{no}) = 2/5 = 0.400$
 $P(\text{student}=\text{yes} / \text{buys_computer} = \text{yes}) = 6/9 = 0.667$
 $P(\text{student}=\text{yes} / \text{buys_computer} = \text{no}) = 1/5 = 0.200$
 $P(\text{credit rating}=\text{fair} / \text{buys_computer} = \text{yes}) = 6/9 = 0.667$
 $P(\text{credit rating}=\text{fair} / \text{buys_computer} = \text{no}) = 2/5 = 0.400$

$P(X/\text{Buys a computer} = \text{yes}) = P(\text{age}=\text{youth} / \text{buys_computer} = \text{yes}) * P(\text{income}=\text{medium} / \text{buys_computer} = \text{yes}) * P(\text{student}=\text{yes} / \text{buys_computer} = \text{yes}) * P(\text{credit rating}=\text{fair} / \text{buys_computer} = \text{yes}) = 0.222 * 0.444 * 0.667 * 0.667 = 0.044$

$P(X/\text{Buys a computer} = \text{No}) = 0.600 * 0.400 * 0.200 * 0.400 = 0.019$

Find class C_i that Maximizes $P(X/C_i) * P(C_i)$

$\Rightarrow P(X/\text{Buys a computer} = \text{yes}) * P(\text{buys_computer} = \text{yes}) = 0.028$

$\Rightarrow P(X/\text{Buys a computer} = \text{No}) * P(\text{buys_computer} = \text{no}) = 0.007$

Prediction : Buys a computer for Tuple X