

# ARYAMAN MISHRA

## 19BCE1027

**Aim:**Implement HITS Algorithm.

**Data Structures Used:**2D Arrays.

### Algorithm:

First, we have to explain what is authority and hub. HITS uses hubs and authorities to define a recursive relationship between webpages.

- Authority: A node is high-quality if many high-quality nodes link to it
- Hub: A node is high-quality if it links to many high-quality nodes

### Algorithm Steps

- Initialize the hub and authority of each node with a value of 1
- For each iteration, update the hub and authority of every node in the graph
- The new authority is the **sum of the hub** of its parents
- The new hub is the **sum of the authority** of its children
- Normalize the new authority and hub

Function to calculate the authority and hub score of all the nodes in the network.

Parameters:

outlinks: (n, n) int matrix where 1 represents the presence of a link and 0 represents absence of a link

Returns: hub\_score: nd-array, containing the hub scores of the nodes

authority\_score: nd-array, containing the authority scores of the nodes

1. Write a python program that takes the outlink data of a subsection of the web and that computes the Normalized Hub and authority score. The program should take the following parameters :
  - a. Number of sites in the sub-section of the web
  - b. Outlink data of the sites

**IMPLEMENTATION AND RESULTS:**

```
# Implementing HITS Algorithm

import numpy as np

# Function to calculate the authority and hub score of the nodes
def authority_hub_score(outlinks):

    # size of the matrix
    size = outlinks.shape[0]

    # Initializing the lists
    hub_scores = [1.0 for i in range(size)]
    authority_scores = [1.0 for i in range(size)]

    # Printing initial Hub scores
    print(hub_scores)

    for _ in range(100):
        # Calculating the authority scores of the nodes
        for j in range(size):
            temp_auth = 0.0
            for i in range(size):
                if outlinks[i][j] == 1:
                    temp_auth += hub_scores[i]
            authority_scores[j] = temp_auth

        # Normalizing the authority scores
        auth_sum = sum(authority_scores)
        # print(auth_sum)
        for i in range(len(authority_scores)):
            authority_scores[i] /= auth_sum

        # Calculating the hub scores of the nodes
        for i in range(size):
            temp_hub = 0.0
            for j in range(size):
                if outlinks[i][j] == 1:
                    temp_hub += authority_scores[j]
            hub_scores[i] = temp_hub
```

```

    # Normalizing the hub scores
    hub_sum = sum(hub_scores)
    # print(hub_sum)
    for i in range(len(hub_scores)):
        hub_scores[i] /= hub_sum

    return authority_scores, hub_scores

n = int(input('Enter the size of the matrix:\t'))
outlinks = []
for i in range(n*n):
    temp = int(input('Enter the element:\t'))
    outlinks.append(temp)
outlinks = np.reshape(outlinks, (n, n))
authority_scores, hub_scores = authority_hub_score(outlinks)
print("Authority Scores:")
for i in (authority_scores):
    print(round(i, 4))
print("Hub Scores:")
for i in (hub_scores):
    print(round(i, 4))

```

```

Enter the size of the matrix:
Enter the element:      1
Enter the element:      0
Enter the element:      1
Enter the element:      0
Enter the element:      0
Enter the element:      1
Enter the element:      1
Enter the element:      0
Enter the element:      0
Enter the element:      0
Enter the element:      1
Enter the element:      1
Enter the element:      1
Enter the element:      1
Enter the element:      1
Enter the element:      0
Enter the element:      0
Enter the element:      0
Enter the element:      1
Enter the element:      0
Enter the element:      1
Enter the element:      0
Enter the element:      1
Enter the element:      1
Enter the element:      1
Enter the element:      1
Enter the element:      1
Enter the element:      0
Enter the element:      1
Enter the element:      0
Enter the element:      0
Enter the element:      1
Enter the element:      1
Enter the element:      0
Enter the element:      0
Enter the element:      1
Enter the element:      1
Enter the element:      0
Enter the element:      0
[1.0, 1.0, 1.0, 1.0, 1.0, 1.0]

```

```

Authority Scores:
0.205
0.1708
0.2034
0.2007
0.0315
0.1887
Hub Scores:
0.1599
0.1138
0.2088
0.15
0.2593
0.1082

```

2. Test your program using the following linkage data. Assume each site consists of only one text page.
  - a. Site A(outlinks to B,C,D)
  - b. Site B(outlinks to A,C,D)
  - c. Site C(outlinks to A,D)
  - d. Site D(outlinks to C,D,E)
  - e. Site E(outlinks to B,C,D)
  - f. Site F(outlinks to A)

### IMPLEMENTATION AND RESULTS:

```
# Implementing HITS Algorithm

import numpy as np

# Function to calculate the authority and hub score of the nodes
def authority_hub_score(outlinks):

    # size of the matrix
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    # Initializing the lists
    hub_scores = [1.0 for i in range(size)]
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    print(hub_scores)

    for _ in range(100):
        # Calculating the authority scores of the nodes
        for j in range(size):
            temp_auth = 0.0
            for i in range(size):
                if outlinks[i][j] == 1:
                    temp_auth += hub_scores[i]
            authority_scores[j] = temp_auth

        # Normalizing the authority scores
        auth_sum = sum(authority_scores)
        # print(auth_sum)
        for i in range(len(authority_scores)):
            authority_scores[i] /= auth_sum

        # Calculating the hub scores of the nodes
        for i in range(size):
            temp_hub = 0.0
            for j in range(size):
                if outlinks[i][j] == 1:
                    temp_hub += authority_scores[j]
```

```

        hub_scores[i] = temp_hub

    # Normalizing the hub scores
    hub_sum = sum(hub_scores)
    # print(hub_sum)
    for i in range(len(hub_scores)):
        hub_scores[i] /= hub_sum

    return authority_scores, hub_scores

outlinks = [[0,1,1,1,0,0],[1,0,1,1,0,0],[1,0,0,1,0,0],[0,0,1,1,1,0],[0,
1,1,1,0,0],[1,0,0,0,0,0]]
outlinks = np.reshape(outlinks, (6, 6))
authority_scores, hub_scores = authority_hub_score(outlinks)
print("Authority Scores:")
links=['A','B','C','D','E','F']
j=0
for i in (authority_scores):
    print(links[j],":",round(i, 4))
    j=j+1

j=0
print("Hub Scores:")
for i in (hub_scores):
    print(links[j],":",round(i, 4))
    j=j+1

```

```

[1.0, 1.0, 1.0, 1.0, 1.0, 1.0]
Authority Scores:
A : 0.1345
B : 0.1541
C : 0.2981
D : 0.3444
E : 0.0688
F : 0.0
Hub Scores:
A : 0.2156
B : 0.2103
C : 0.1296
D : 0.1925
E : 0.2156
F : 0.0364

```

CONCLUSION:HITS ALGORITHM HAS BEEN SUCCESFULLY IMPLEMENTED AND EXECUTED.