-:- Numwical Nethock: * The limitations of analytical muthods in practical applications fave and scientists and engineers to evolve numerical muthods.

Hurs crooms, so as to get the East possible the error in the final smult may be due to an error in the introl data or in the method wild be minimize * The input information is howly exact since it comes from some measurement or the other tond the method also introduces some earons. At such

may occur in a problem. Approximate rumburg > Trum on two typus of errore which

* exact numbers > 2, 4, 9, 13, 7/2, 6.45 et

THE INF. $\sqrt{2} = (1.414213...)$ and $\sqrt{2} = (2.414213...)$ and $\sqrt{2} = (3.141592...)$ askich can not by a finite

number of diffits. Thus numbers may * Approximate rumbers > etam our numbers 3.1416 # 3.141.6 approximated by numerum 1.3333, 1.4190

suck number conich supresent the given to a certain degrae, of accuracy are called approximate number. Significant digité (figure) > The digité used to express a number. are called significant digité (figures). * The each of the numbers 7845, 3.589 and 0.4758 contains four significant dégits. * While the numbers 0.00386, 0.000587 and 0.0000296 contains only three signifi--cant figures since scrop only help to fin the positions of the decimal soint. * Similarly the neumbers 45000 & 7300.00 have two significant figures only. Rounding off > There are numbers with large number of digité, e.g. 22 = 3.142857143. In pratice, it is duirable to winit such numbers to a manageable number of digité such as 8:14 or 3:143. This prouse of dropping unwanted digits is called rounding off. Rule to round off a wnumbus to n significant *(i) Discard all digits to the night of the nth digit. (ii) 98 this dip carded number is @ luse than half of a unit in the nth Black, leave the nth digit unchanged of greater than half a unit in the nth place, in one are the nth digit by unity.

increase the nth digit by unity if it is odd otherwise leave it unchanged. for instance, the following numbers rounded off to three significant figures are (20.003 (i) 7.893 to 7.89 1 3.567 to 3.57 (i) 12.865 to 12.9 (84767 to 84800 (iii) 6.4356 to 6.44 (vi) 5.8254 to 5.82 * Also num telle 6.28 4359, 9.864651 and 12.464762 av rounded off to four places.
of decimal as 6.2844, 9.8646, and
12.4648 supertirely. * Numbers there rounded off to n significant figures (or n decimal place) are said to be correct to n significant figures to be correct to n significant figures. Errorg -i-In any numerical computation, we come acrott the tollowing the of orrord: 1) Inherent errors > Errors which are abready present in the statement of a problem before its solution, are called inherent errors. * such errors arise either due to the given data buing approximate or du to the umitations of mathematical tables, calculators, or the digital combile. Scanned with CamScanner better data or by wing night freution computing aids. @ Rounding errors This error aribe from the proubt of rounding off the numbers during i the computation. such errore art un avoidable in most of the calculations due to the similations of the computing aids. can, Rowerer, Be stedució * Konngista beroak for a dure calculation (i) By changing the so as to avoid of nearly subtraction a small division by equal number or number. one more significant (ii) By outaining atleast figure at each step that given in the data and rounding off at the last step. 3) Trancation errors There errors are caused by using.
approximate rusults or on sublacing an infinite proule sy a finite one. * 9¢ use ar using a decimal computer Aring a fired word lingth of four digits, rounding off 13.658 girls 13.66 whereas trancotion gives 13.65. * For example, if example, 18 $e^{x} = 1 + n + \frac{x^{2}}{2!} + \frac{x^{3}}{3!} + \frac{x^{4}}{4!} + \dots = x (30)$ is replaced by $1 + ni + n^2 + n^3 = x!$ (say), then the trancation error is a type of algorithm error

A Absolute, Relative, and privantage, errors of a quantity and x' is its approximate value, then 1x-x'/ i.e (error) is called the abpolute error (Ea).

* The relative error is defined by $E_{r} = \left| \frac{x - x'}{x} \right| \text{ i.e. } \left| \frac{Error}{True \ value} \right|.$

* The purentage error is $E_p = 100 E_{ro}$ = $100 \left| \frac{x-x'}{x} \right|$.

* If \overline{x} be such a number that |x-x'| $\leq \overline{x}$ then \overline{x} is an upper simil on the magnitude of the objective error and measures the objective accuracy.

observation The relative and believed errors are independent of the units white absolute error is expressed in terms of these units.

observation of the cornect to modernal places then the error = 10.0000 for a number if 3.1416 cornect to a decimal places the number if 3.1416 cornect to a decimal places, the number if 3.1416 cornect to a decimal places, the error = 10.0000 for the decimal places, then error = 10.0000 for the decimal places.