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10)

$$\begin{array}{cc}
 n^k & c^n \\
 k \geq 1 & c > 1 \\
 k = 1 & c = 2 \\
 n & 2^n
 \end{array}$$

Q) Asymptotic notations are used in computer science and mathematics to describe the behaviour of algorithm or function as their input size approaches infinity. The three main notations are

i) Big $O()$:

Represents another part an upper bound on a growth rate of a function.

ii) Omega $\Omega()$: Represents the lower bound and the growth of wait function.

iii) Theta $\Theta()$: Represents both upper and lower bound indicating tightness bond on the each side

Ans

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for (i = 1 to n)
{
    i = i * 2;
}
  
```

The time complexity of the given loop is $O(\log n)$ this is because variable i is multiplied by 2.

Q3) The recursion relation suggest that that
 $T(n) = 3^k T(n-k)$ until $n-k=1$

$$T(n) = 3^k$$

$$T(n) = 3^{(n-1)}$$

$$T(n) = 3^{(n-1)} = O(3^n)$$

So, time complexity is $O(3^n)$

Q4) $T(n) = 2^n - (2^0 + 2^1 + 2^2 + \dots + 2^{(n-1)})$

$$T(n) = 2^n - (2^n - 1)$$

$$T(n) = 1$$

So time complexity is constant, we can express it as $O(1)$.

Q5) The time complexity is $O(\sqrt{n})$ as the loop trying
 approx \sqrt{n} relations where n is the input
 parameter.

Q6) The time complexity of the given code is $O(\sqrt{n})$,
 This is because the loop iterates until $i*i$
 exceeds n , and in each execution i is increased
 as the loop stops which $i*i$ becomes greater
 than n .

Q7) The outer loop runs, $i = n/2$ to n it
 iterates $(n - n/2) + 1$ times, which is app. $n/2$ times.
 The second loop runs from $j=1$ to n . So it's just app.
 $\log(n)$ times.

The third loop is similar to second loop i.e. $\log(n)$ times.
 Since, they are nested we multiply them.

$$O(n) \times O(\log n) \times O(\log n) = O(n \log^2 n)$$

QSS

Ans:

The inner loop for $(j=1 \text{ to } n)$ runs n times.
 The outer loop for $(i=1 \text{ to } n)$ runs n times.
 The recursive call function $n(n-3)$ reduced size of n by 3 in each recursive call until $n=1$.

$$T(n) = n \times n + T(n-3)$$

$$T(n) = n^2 + T(n-3)$$

Solving this recurrence is bit complex, but we can approximate it to $O(n^2)$.

QSS

Ans:

The outer loop runs from $i=1$ to n
 The inner loop runs from $j=1$ to n but increment is i i.e. $j=j+i$.

When $i=1$, it runs n times

When $i=2$, it runs $n/2$ times

When $i=3$, the inner loop runs $n/3$ times.

When $i=n$, the inner loop runs only once.

$$1 + \frac{n}{2} + \frac{n}{3} + \dots + 1$$

$$\therefore O(\log n) \quad \underline{\underline{\text{Ans}}}$$

~~QSS~~