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1 Base

1.1 vimrc

```
cd ~/Documents/Contest/
_2 set sw=4
₃ set ts=4
                    " super indentation
4 set si
                   " line numbers
5 set number
                   " syntax highlighting
6 syntax on
7 set cursorline
                  " highlight current line
s set guifont=consolas:h11
g set bs=2
                   " mouse works normally
10 set mouse=a
                   " global replacement
11 set gdefault
12 set fdm=indent
                            " folding method
set foldlevelstart=99
                            " at first all folds are open
```

1.2 Template

```
#include <bits/stdc++.h>
using namespace std;
#define pb push_back
4 #define mp make_pair
5 #define SQR(a) ((a)
                        (a))
6 #define SZ(x) ((int) (x).size())
#define ALL(x) (x).begin(), (x).end()
8 #define CLR(x, a) memset(x, a, sizeof x)
^{9} #define VAL(x) #x << " = " << (x) << " "
#define FOREACH(i, x) for(__typeof((x).begin()) i = (x).begin();
     i != (x).end(); i ++)
#define FOR(i, n) for (int i = 0; i < (n); i ++)
12 #define X first
13 #define Y second
14 typedef long long ll;
typedef pair<11, 11> pll;
typedef pair<int, int> pii;
const int MAXN = 1 1000 + 10;
18 int main () {
ios::sync_with_stdio(false);
   return 0;
```

2 Graph

2.1 LCA

```
vector<int> adj[MAXN];
int par[MAXN][MAXL], h[MAXN];
3 bool mark[MAXN];
4 void dfs(int x) {
    mark[x] = true;
    for (int i = 0; i < SZ(adj[x]); i ++) {
     int v = adj[x][i];
      if (!mark[v]) {
        par[v][0] = x, h[v] = h[x] + 1;
        dfs(v);
12
int get_parent(int x, int k) {
    for (int i = 0; i < MAXL; i ++)
      if ((1 << i) \& k) x = par[x][i];
    return x;
18
int lca(int x, int y) {
    if (h[y] > h[x]) swap(x, y);
    x = get_parent(x, h[x] - h[y]);
    if (x == y) return x;
    for (int i = MAXL - 1; i >= 0; i--)
      if (par[x][i] != par[y][i])
        x = par[x][i], y = par[y][i];
    return par[x][0];
28 int main () {
    par[0][0] = -1;
    dfs(0);
    for (int i = 1; i < MAXL; i ++)
     for (int j = 0; j < n; j ++)
        par[j][i] = par[par[j][i - 1]][i - 1];
```

2.2 SCC

```
vector <int> adj[N];
```

```
stack <int> S, P;
int mrk[N], ind, col[N], CL;
4 void dfs(int v) {
    mrk[v] = ++ind;
    S.push(v);
    P.push(v);
    for(int i = 0; i < Size(adj[v]);++i) {</pre>
     int u = adj[v][i];
      if(!mrk[u])
10
        dfs(u);
11
      else
12
        while(mrk[u] < mrk[S.top()])</pre>
13
          S.pop();
14
15
    if(S.top() == v) {
16
      mrk[v] = INF;
17
      col[v] = ++CL;
18
      while(P.top() != v) {
19
        col[P.top()] = CL;
20
        mrk[P.top()] = INF;
22
        P.pop();
23
      P.pop();
24
      S.pop();
25
26
^{28} //main: for(int i = 1; i <= n; ++i)
29 //
         if(!mrk[i]) dfs(i);
```

2.3 Matching

```
int match[3][MAXN]; // 0 for first part, 1 for second part
bool mark[MAXN];
vector<int> adj[MAXN]; // adjacent list for first part nodes
int n, m, p;
// n: number of nodes in first part
// m: number of nodes in second part
// p: number of edges
bool dfs(int x) {
   if (mark[x]) return false;
   mark[x] = true;
```

```
for (int i = 0; i < SZ(adj[x]); i ++) {
      int v = adj[x][i];
      if (match[1][v] == -1 || dfs(match[1][v])) {
        match[0][x] = v;
        match[1][v] = x;
16
        return true;
17
18
19
    return false;
21
void bi_match() {
    CLR(match, -1);
    for (int i = 0; i < n; i ++) {
      CLR(mark, 0);
      bool check = false;
      for (int j = 0; j < n; j ++)
       if (!mark[j] && match[0][j] == -1)
          check = dfs(j);
      if (!check) break;
31
32
33 int main () {
    cin >> n >> m >> p;
    for (int i = 0; i < p; i ++) {
     int x, y; cin >> x >> y; x ---, y ---;
     // x: a node in first part [0, n)
      // y: a node in second part [0, m)
      adj[x].pb(y);
40
    bi_match();
    int ans = 0;
    FOR(i, n) ans += (match[0][i] != -1);
    cout << ans << endl;</pre>
    return 0;
```

2.4 Max Flow BFS

```
#include <queue>
  #include <cstring>
const int N = 100;
int mat[N][N];
```

```
6 bool anotherPath(int start, int end) {
    memset(viz, 0, sizeof viz);
    memset(parent, -1, sizeof parent);
    viz[start] = true;
    queue<int> q;
10
    q.push(start);
11
    while (!q.empty()) {
12
     int z = q.front(); q.pop();
13
      viz[z] = true;
14
      for (int i=0; i<N; i++) {
15
        if (network[z][i] <= 0 || viz[i]) continue;</pre>
16
        viz[i] = true;
17
        parent[i] = z;
18
        if (i == end) return true;
19
        q.push(i);
20
21
22
    return false;
23
24
int maxflow(int start, int end) {
    memcpy(network, mat, sizeof(mat));
    int total = 0;
    while (anotherPath(start, end)) {
      int flow = network[parent[end]][end];
29
      int curr = end;
30
      while (parent[curr] >= 0) {
31
        flow = min(flow, network[parent[curr]][curr]);
        curr = parent[curr];
33
34
      curr = end;
35
      while (parent[curr] >= 0) {
36
        network[parent[curr]][curr]—=flow;
        network[curr][parent[curr]]+=flow;
        curr = parent[curr];
39
40
      total += flow;
41
42
    return total;
44 }//O(max_flow E) to net neveshte bood nemidoonam chejorie
```

int viz[N], network[N][N], parent[N];

2.5 Max Flow Dinic

```
#include <iostream>
2 #include <queue>
3 using namespace std;
#define REP(i,n) for((i)=0;(i)<(int)(n);(i)++)</pre>
5 typedef int F;
6 #define F_INF (1<<29)
7 #define MAXV 10000
8 #define MAXE 1000000 // E 2!
9 F cap[MAXE], flow[MAXE];
int to[MAXE], _prev[MAXE], last[MAXV], used[MAXV], level[MAXV];
struct MaxFlow {
      int V, E;
13
      MaxFlow(int n) {
          int i:
          V = n; E = 0;
          REP(i,V) last[i] = -1;
17
18
      void add_edge(int x, int y, F f) { //directed edge
19
          cap[E] = f; flow[E] = 0; to[E] = y;
          _prev[E] = last[x]; last[x] = E; E++;
          cap[E] = 0; flow[E] = 0; to[E] = x;
          _prev[E] = last[y]; last[y] = E; E++;
2.4
25
      bool bfs(int s, int t){
26
          int i:
          REP(i,V) level[i] = -1;
28
          queue <int> q;
          q.push(s); level[s] = 0;
          while(!q.empty()){
              int x = q.front(); q.pop();
              for(i=last[x]; i>=0; i=_prev[i])
                   if(level[to[i]] == -1 \&\& cap[i] > flow[i]) {
                       q.push(to[i]);
                       level[to[i]] = level[x] + 1;
          return (level[t] !=-1);
```

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```
F dfs(int v, int t, F f){
41
          int i;
42
          if(v == t) return f;
43
          for(i=used[v]; i>=0; used[v]= i =_prev[i])
44
               if(level[to[i]] > level[v] && cap[i] > flow[i]) {
45
                   F tmp = dfs(to[i], t, min(f, cap[i]-flow[i]));
46
                   if(tmp > 0) {
                       flow[i] += tmp;
48
                       flow[i^1] = tmp;
49
                       return tmp;
50
51
52
          return 0;
53
54
      F maxflow(int s, int t) {
55
          int i;
56
          while(bfs(s,t)) {
57
               REP(i,V) used[i] = last[i];
58
               while(dfs(s,t,F_INF) != 0);
60
          F ans = 0;
          for(i=last[s];i>=0;i=_prev[i])
62
               ans += flow[i];
63
          return ans;
64
65
66 }; //O(E V ^ 2) no idea
```

2.6 Min Cost Max Flow

```
#include <iostream>
#include <queue>
using namespace std;
#define REP(i,n) for((i)=0;(i)<(int)(n);(i)++)

//XXX change these lines!

typedef int F;
typedef long long C;
#define F_INF (1<<29)
#define C_INF (1LL<<60)
#define MAXV 3000
#define MAXE 10000 // E 2! [or E 4 for bidirected graphs]
//no need to initialize these variables!</pre>
```

```
13 int V, E;
14 F cap[MAXE];
15 C cost[MAXE], dist[MAXV], pot[MAXV];
int to[MAXE],prv[MAXE],last[MAXV],path[MAXV];
bool used[MAXV];
priority_queue <pair <C, int> > q;
19 F flow[MAXE];//output
20 class MinCostFlow {
21 public:
     MinCostFlow(int n);
     int add_edge(int x, int y, F w, C c); // zero based &&
     directed!
      pair <F, C> mincostflow(int s, int t);
      pair <F, C> search(int s, int t);
     void bellman(int s);
28 };
30 MinCostFlow::MinCostFlow(int n){
     V = n; E = 0;
     int i; REP(i,V) last[i] = -1;
32
33
int MinCostFlow::add_edge(int x, int y, F w, C c){
      cap[E] = w; flow[E] = 0; cost[E] = c; to[E] = y; prv[E] =
     last[x]; last[x] = E; E++;
     cap[E] = 0; flow[E] = 0; cost[E] = -c; to[E] = x; prv[E] = 0
     last[y]; last[y] = E; E++;
     return E-2;
void MinCostFlow::bellman(int s){
     int i,x,e;
     REP(i,V) pot[i] = C_INF;
     pot[s] = 0;
     REP(i,V+10) REP(x,V) for (e=last[x];e>=0;e=prv[e]) if (cap[e]>
      0) pot[to[e]] = min(pot[to[e]], pot[x] + cost[e]);
44
45 pair <F, C> MinCostFlow::search(int s, int t){
     F ansf=0; C ansc=0;
     int i:
     REP(i,V) used[i] = false;
     REP(i,V) dist[i] = C_INF;
```

```
dist[s] = 0; path[s] = -1; q.push(make_pair(0,s));
      while(!q.empty()){
51
          int x = q.top().second; q.pop();
          if(used[x]) continue; used[x] = true;
          for(int e=last[x];e>=0;e=prv[e]) if(cap[e] > 0){
              C \text{ tmp} = dist[x] + cost[e] + pot[x] - pot[to[e]];
              if(tmp < dist[to[e]] && !used[to[e]]){</pre>
                  dist[to[e]] = tmp;
                  path[to[e]] = e;
58
                  q.push(make_pair(-dist[to[e]],to[e]));
59
60
61
62
      REP(i,V) pot[i] += dist[i];
63
      if(used[t]){
64
          ansf = F_{INF};
65
          for(int e=path[t];e>=0;e=path[to[e^1]]) ansf = min(ansf,
66
     cap[e]);
          for(int e=path[t];e>=0;e=path[to[e^1]]) {ansc += cost[e]
67
       ansf; cap[e] -= ansf; cap[e^1] += ansf; flow[e] += ansf;
     flow[e^1] = ansf;
68
      return make_pair(ansf,ansc);
69
70 }
71 pair <F, C> MinCostFlow::mincostflow(int s, int t){
      F ansf=0; C ansc=0;
      int i;
      bellman(s);
74
      while(1){
75
          pair \langle F, C \rangle p = search(s,t);
76
          if(!used[t]) break;
          ansf += p.first; ansc += p.second;
78
79
      return make_pair(ansf,ansc);
80
83 int main() {
      return 0;
```

```
2.7 Bellman Ford
```

```
int n, m;
int ex[MAXN], ey[MAXN], ew[MAXN], d[MAXN];
3 bool bellman(int start) {
    FOR(i, n) d[i] = INF;
    d[start] = 0;
    FOR(i, n - 1) FOR(j, m) {
     int x = ex[j], y = ey[j]; double w = tw[j];
      d[y] = min(d[y], d[x] + w);
    // check if graph has a negative cycle
    FOR(i, m) {
     int x = ex[i], y = ey[i]; double w = tw[i];
      if (d[y] > d[x] + w) return false;
14
    return true;
16 } // O(n m) ye start midim ham distance ha ro bedast miare o
     ham dor manfi ro check mikone
```

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2.8 Dijkstra

```
const int MAXN = 10
                       1000 + 10;
const 11 INF = 1e9;
3 11 dis[MAXN];
4 set<pii> s;
5 bool mark[MAXN];
6 vector<pii> adj[MAXN];
void dij(int start) {
   for (int i = 0; i < MAXN; i ++) dis[i] = INF;
   CLR(mark, 0); s.clear();
   mark[start] = true;
   dis[start] = 0;
   s.insert(mp(0, start));
   while (SZ(s)) {
     int x = s.begin()->Y; s.erase(s.begin());
     for (int i = 0; i < SZ(adj[x]); i ++) {
       int v = adj[x][i].X, w = adj[x][i].Y;
       if (dis[v] > dis[x] + w) {
         if (mark[v]) s.erase(mp(dis[v], v));
         else mark[v] = true;
         dis[v] = dis[x] + w;
         s.insert(mp(dis[v], v));
```

2.9 Prim

```
_{1} const int N = 1000
                        100 + 5;
vector <pii> adj[N];
int ans, mrk[N];
4 void prim(int v) {
5 int w;
    set <pii> st;
    st.insert(mp(0, v));
    while(!st.empty()) {
      v = st.begin() -> Y;
      w = st.begin()-> X;
10
      st.erase(st.begin());
11
      if(mrk[v]++) continue;
12
      ans += w;
13
      for(int i = 0; i < Size(adj[v]);++i)</pre>
15
        if(!mrk[adj[v][i].Y])
16
          st.insert(adj[v][i]);
17
18
19
```

2.10 DSU

```
int par[MAXN];
pair <int, pii> e[MAXN];
int father(int x) {
   return par[x] == -1 ? x : par[x] = father(par[x]);
}
bool merge(int x, int y) {
   x = father(x);
   y = father(y);
   if (x != y) par[y] = x;
   return x != y;

fill(par, par + n, -1);
```

2.11 Eulerian Tour

```
void euler(int x) {
   for (int i = 0; i < SZ(graph[x]); i ++) {
     int v = graph[x][i];
     if (!vis[x][v]) {
        vis[x][v] = vis[v][x] = true;
        euler(v);
     }
   }
   tour.pb(x);
}//O(n + m) tour oileri migere</pre>
```

2.12 Topological Sort

```
1 // This function uses performs a non-recursive topological sort.
_{2} // Running time: O(|V|^{2}). If you use adjacency lists (vector<
     map < int > >),
3 //
                   the running time is reduced to O(|E|).
               w[i][j] = 1 if i should come before j, 0 otherwise
5 //
      OUTPUT: a permutation of 0, \ldots, n-1 (stored in a vector)
6 //
                which represents an ordering of the nodes which
                is consistent with w
8 // If no ordering is possible, false is returned.
9 #include <iostream>
#include <queue>
#include <cmath>
#include <vector>
13 using namespace std;
14 typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<int> VI;
typedef vector<VI> VVI;
19 bool TopologicalSort (const VVI &w, VI &order){
   int n = w.size();
   VI parents (n);
   queue<int> q;
   order.clear();
   for (int i = 0; i < n; i++)
    for (int j = 0; j < n; j++)
       if (w[j][i]) parents[i]++;
```

```
if (parents[i] == 0) q.push (i);
    while (q.size() > 0){
      int i = q.front();
30
      q.pop();
31
      order.push_back (i);
32
      for (int j = 0; j < n; j++) if (w[i][j]){
33
        parents[j]--;
34
        if (parents[j] == 0) q.push (j);
35
36
37
    return (order.size() == n);
38
39
```

2.13 Kardak General Graph matching3

```
1 // GETS:
2 // V—>number of vertices
3 // E—>number of edges
4 // pair of vertices as edges (vertices are 1..V) O(E V^2)
5 // GIVES:
6 // output of edmonds() is the maximum matching
7 // match[i] is matched pair of i (-1 if there isn't a matched
     pair)
8 #include <bits/stdc++.h>
using namespace std;
10 const int M=500;
struct struct_edge{int v; struct_edge n; };
typedef struct_edge edge;
struct_edge pool[M M 2];
14 edge top=pool,adj[M];
int V,E,match[M],qh,qt,q[M],father[M],base[M];
bool inq[M], inb[M], ed[M][M];
void add_edge(int u,int v){
   top->v=v,top->n=adj[u],adj[u]=top++;
   top->v=u,top->n=adj[v],adj[v]=top++;}
int LCA(int root, int u, int v){
   static bool inp[M];
    memset(inp,0,sizeof(inp));
   while(1){
23
        inp[u=base[u]]=true;
        if (u==root) break;
```

```
u=father[match[u]];}
  while(1){
      if (inp[v=base[v]]) return v;
      else v=father[match[v]];}}
void mark_blossom(int lca,int u){
  while (base[u]!=lca){
      int v=match[u];
      inb[base[u]]=inb[base[v]]=true;
      u=father[v];
      if (base[u]!=lca) father[u]=v;}}
void blossom_contraction(int s,int u,int v){
  int lca=LCA(s,u,v);
  memset(inb,0,sizeof(inb));
  mark_blossom(lca,u);
  mark_blossom(lca,v);
  if (base[u]!=lca)
    father[u]=v;
  if (base[v]!=lca)
    father[v]=u;
  for (int u=0; u<V; u++)
    if (inb[base[u]]){
      base[u]=lca;
      if (!inq[u])
        inq[q[++qt]=u]=true;}}
int find_augmenting_path(int s){
  memset(inq,0,sizeof(inq));
  memset(father, -1, sizeof(father));
  for (int i=0;i<V;i++) base[i]=i;</pre>
  ing[q[qh=qt=0]=s]=true;
  while (qh<=qt){</pre>
      int u=q[qh++];
      for (edge e=adj[u];e;e=e->n){
        int v=e->v;
        if (base[u]!=base[v]&&match[u]!=v)
          if ((v==s)||(match[v]!=-1 \&\& father[match[v]]!=-1))
            blossom_contraction(s,u,v);
          else if (father[v]==-1){
            father[v]=u;
            if (match[v]==-1)
              return v;
            else if (!inq[match[v]])
```

```
inq[q[++qt]=match[v]]=true; }}
    return -1;
int augment_path(int s,int t){
    int u=t,v,w;
    while (u!=-1)
        v=father[u];
72
        w=match[v];
73
        match[v]=u;
        match[u]=v;
75
        u=w;
76
    return t!=-1;
77
78 int edmonds(){
    int matchc=0;
    memset(match,-1,sizeof(match));
    for (int u=0;u<V;u++)</pre>
81
     if (match[u]==-1)
82
        matchc+=augment_path(u, find_augmenting_path(u));
83
    return matchc;}
85 int main(){
    int u,v;
    cin>>V>>E;
    while (E--){
      cin>>u>>v;
89
     if (!ed[u-1][v-1]){
        add_edge(u-1,v-1);
91
        ed[u-1][v-1]=ed[v-1][u-1]=true; }}
    cout<<edmonds()<<endl;</pre>
    for (int i=0; i<V; i++)
      if (i<match[i])</pre>
        cout<<i+1<<" "<<match[i]+1<<endl;}
```

2.14 Kardak Min Cost Max Flow

```
struct Edge{
  int from, to, capacity, cost;
};

vector<vector<int>>> adj, cost, capacity;

const int INF = 1e9;

void shortest_paths(int n, int v0, vector<int>& d, vector<int>& p
  ) {
  d.assign(n, INF);
  d[v0] = 0;
```

```
vector<bool> inq(n, false);
    queue<int> q;
    q.push(v0);
    p.assign(n, -1);
    while (!q.empty()) {
     int u = q.front();
      q.pop();
      inq[u] = false;
      for (int v : adj[u]) {
        if (capacity[u][v] > 0 && d[v] > d[u] + cost[u][v]) {
          d[v] = d[u] + cost[u][v];
          p[v] = u;
          if (!inq[v]) {
21
            ing[v] = true;
            q.push(v);}}}}
int min_cost_flow(int N, vector<Edge> edges, int K, int s, int t)
    adj.assign(N, vector<int>());
    cost.assign(N, vector<int>(N, 0));
    capacity.assign(N, vector<int>(N, 0));
    for (Edge e : edges) {
      adj[e.from].push_back(e.to);
      adj[e.to].push_back(e.from);
      cost[e.from][e.to] = e.cost;
      cost[e.to][e.from] = -e.cost;
      capacity[e.from][e.to] = e.capacity;}
    int flow = 0;
    int cost = 0;
    vector<int> d, p;
    while (flow < K) {</pre>
      shortest_paths(N, s, d, p);
      if (d[t] == INF)
        break:
      // find max flow on that path
      int f = K - flow;
      int cur = t;
      while (cur != s) {
        f = min(f, capacity[p[cur]][cur]);
        cur = p[cur];}
      // apply flow
```

```
flow += f;
cost += f d[t];
cur = t;
while (cur != s) {
    capacity[p[cur]][cur] -= f;
    capacity[cur][p[cur]] += f;
    cur = p[cur];}
if (flow < K)
return -1;
else
return cost;}</pre>
```

3 Geometry

3.1 Geometry

```
#include <iostream>
#include <vector>
3 #include <cmath>
#include <cassert>
s using namespace std;
6 double INF = 1e100;
_{7} double EPS = 1e-12;
8 struct PT {
      double x, y;
10
     PT() {}
      PT(double x, double y) : x(x), y(y) {}
11
      PT(const PT \&p) : x(p.x), y(p.y)
12
      PT operator + (const PT &p) const { return PT(x+p.x, y+p.y);
13
      PT operator – (const PT &p) const { return PT(x-p.x, y-p.y);
14
      PT operator
                    (double c)
                                   const { return PT(x c, y c );
15
      PT operator / (double c)
                                   const { return PT(x/c, y/c );
16
double dot(PT p, PT q)
                             { return p.x q.x+p.y q.y; }
double dist2(PT p, PT q)
                           { return dot(p-q,p-q); }
20 double cross(PT p, PT q)
                            { return p.x q.y-p.y q.x; }
ostream & operator << (ostream & os, const PT & p) {
```

```
return os << "(" << p.x << "," << p.y << ")";
23
_{24} // if movement from a to b to c is done in a CW path returns 1
_{25} // else if it's CCW returns -1 and if they make a line returns 0
int IsCWTurn(PT a, PT b, PT c) {
      double r = cross((b - c), (a - c));
      return (fabs(r) < EPS)? 0: (r > 0)? 1: -1;
29
30 // rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y,p.x); }
PT RotateCW90(PT p) { return PT(p.y,-p.x); }
33 PT RotateCCW(PT p, double t) {
      return PT(p.x cos(t)-p.y sin(t), p.x sin(t)+p.y cos(t));
36 // project point c onto line through a and b
37 // assuming a != b
38 PT ProjectPointLine(PT a, PT b, PT c) {
      return a + (b-a) dot(c-a, b-a)/dot(b-a, b-a);
40
41 // project point c onto line segment through a and b
42 PT ProjectPointSegment(PT a, PT b, PT c) {
      double r = dot(b-a, b-a);
      if (fabs(r) < EPS) return a;</pre>
      r = dot(c-a, b-a)/r;
      return (r < 0)? a: (r > 1)? b: a + (b - a) r;
46
_{
m 48} // compute distance from c to segment between a and b
49 double DistancePointSegment(PT a, PT b, PT c) {
      return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
_{52} // compute distance between point (x,y,z) and plane ax+by+cz=d
double DistancePointPlane(double x, double y, double z, double a,
      double b,
       double c, double d) {
      return fabs(a x+b y+c z-d)/sqrt(a a+b b+c c);
57 // determine if lines from a to b and c to d are parallel or
     collinear
58 bool LinesParallel(PT a, PT b, PT c, PT d) {
      return fabs(cross(b-a, c-d)) < EPS;</pre>
60
```

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```
61 bool LinesCollinear(PT a, PT b, PT c, PT d) {
      return LinesParallel(a, b, c, d)
      && fabs(cross(a-b, a-c)) < EPS
      && fabs(cross(c-d, c-a)) < EPS;
64
65
66 // determine if line segment from a to b intersects with
67 // line segment from c to d
68 bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
      if (LinesCollinear(a, b, c, d)) {
69
          if (dist2(a, c) < EPS \mid | dist2(a, d) < EPS \mid |
70
          dist2(b, c) < EPS \mid dist2(b, d) < EPS) return true;
71
          if (dot(c-a, c-b) > 0 \& dot(d-a, d-b) > 0 \& dot(c-b, d-a)
72
     b) > 0)
               return false:
73
          return true;
74
75
      if (cross(d-a, b-a)
                             cross(c-a, b-a) > 0) return false;
76
      if (cross(a-c, d-c)
                             cross(b-c, d-c) > 0) return false;
77
      return true;
78
79
so // compute intersection of line passing through a and b
_{
m 81} // with line passing through c and d, assuming that unique
82 // intersection exists; for segment intersection, check if
83 // segments intersect first
84 PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
      b=b-a; d=c-d; c=c-a;
85
      assert(dot(b, b) > EPS \&\& dot(d, d) > EPS);
86
      return a + b cross(c, d)/cross(b, d);
87
88
89 // compute center of circle given three points
90 PT ComputeCircleCenter(PT a, PT b, PT c) {
      b=(a+b)/2:
91
      c = (a+c)/2;
92
      return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+
93
     RotateCW90(a-c));
94
95 // determine if point is in a possibly non-convex polygon (by
96 // Randolph Franklin); returns 1 for strictly interior points, 0
     for
97 // strictly exterior points, and 0 or 1 for the remaining points.
```

```
98 // Note that it is possible to convert this into an exact test
      using
99 // integer arithmetic by taking care of the division
      appropriately
100 // (making sure to deal with signs properly) and then by writing
      exact
101 // tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
       bool c = 0;
       for (int i = 0; i < p.size(); i++) {
           int j = (i+1)\%p.size();
           if (((p[i].y <= q.y && q.y < p[j].y) || (p[j].y <= q.y &&</pre>
       q.y < p[i].y) &&
            q.x < p[i].x + (p[j].x - p[i].x)
                                               (q.y - p[i].y) / (p[j]
107
      ].y - p[i].y))
           c = !c;
108
109
       return c;
110
111
  // determine if point is on the boundary of a polygon
  bool PointOnPolygon(const vector<PT> &p, PT q) {
       for (int i = 0; i < p.size(); i++)
      if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q)
115
       < EPS)
       return true:
116
      return false;
117
118
119 // compute intersection of line through points a and b with
  // circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
       vector<PT> ret;
       b = b-a:
       a = a-c:
       double A = dot(b, b);
125
       double B = dot(a, b);
       double C = dot(a, a) - r r;
       double D = B B - A C;
       if (D < -EPS) return ret;
       ret.push_back(c+a+b(-B+sqrt(D+EPS))/A);
130
      if (D > EPS)
       ret.push_back(c+a+b(-B-sqrt(D))/A);
```

```
return ret;
134
_{
m 135} // compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double
     R) {
      vector<PT> ret;
138
      double d = sqrt(dist2(a, b));
139
      if (d > r+R \mid | d+min(r, R) < max(r, R)) return ret;
140
      double x = (d d-R R+r r)/(2d);
141
      double y = sqrt(r r - x x);
142
      PT v = (b-a)/d;
143
      ret.push_back(a+v x + RotateCCW90(v) y);
144
      if (y > 0)
145
      ret.push_back(a+v x - RotateCCW90(v) y);
146
      return ret;
147
148
_{
m 149} // This code computes the area or centroid of a (possibly
     nonconvex)
_{
m 150} // {
m polygon} , assuming that the coordinates are listed in a
     clockwise or
<sub>151</sub> // counterclockwise fashion. Note that the centroid is often
     known as
152 // the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
      double area = 0;
154
      for(int i = 0; i < p.size(); i++) {
155
          int j = (i+1) \% p.size();
          area += p[i].x p[j].y - p[j].x p[i].y;
158
      return area / 2.0;
159
160
double ComputeArea(const vector<PT> &p) {
      return fabs(ComputeSignedArea(p));
162
163
PT ComputeCentroid(const vector<PT> &p) {
      PT c(0,0);
      double scale = 6.0
                             ComputeSignedArea(p);
      for (int i = 0; i < p.size(); i++)
          int j = (i+1) \% p.size();
          c = c + (p[i]+p[j]) (p[i].x p[j].y - p[j].x p[i].y);
```

```
return c / scale;
172
173 // tests whether or not a given polygon (in CW or CCW order) is
      simple
bool IsSimple(const vector<PT> &p) {
       for (int i = 0; i < p.size(); i++) {
           for (int k = i+1; k < p.size(); k++) {
               int j = (i+1) \% p.size();
               int 1 = (k+1) \% p.size();
               if (i == 1 \mid | j == k) continue;
               if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
               return false;
182
183
       return true;
184
185
```

3.2 Convex Hull

```
1 // Compute the 2D convex hull of a set of points using the
     monotone chain
2 // algorithm. Eliminate redundant points from the hull if
     REMOVE_REDUNDANT is
3 // #defined.
4 // Running time: O(n log n)
5 // INPUT: a vector of input points, unordered.
      OUTPUT: a vector of points in the convex hull,
     counterclockwise, starting
7 //
                with bottommost/leftmost point
8 #include <cstdio>
9 #include <cassert>
#include <vector>
#include <algorithm>
12 #include <cmath>
using namespace std;
#define REMOVE_REDUNDANT
typedef double T;
const T EPS = 1e-7;
17 struct PT {
     T x, y;
     PT() {}
```

```
bool operator<(const PT &rhs) const { return make_pair(y,x) <</pre>
      make_pair(rhs.y,rhs.x); }
      bool operator == (const PT &rhs) const { return make_pair(y,x)
     == make_pair(rhs.y,rhs.x); }
23 };
T cross(PT p, PT q) { return p.x q.y-p.y q.x; }
T area2(PT a, PT b, PT c) { return cross(a,b) + cross(b,c) +
     cross(c,a); }
#ifdef REMOVE_REDUNDANT
bool between(const PT &a, const PT &b, const PT &c) {
      return (fabs(area2(a,b,c)) < EPS && (a.x-b.x) (c.x-b.x) <= 0
     && (a.y-b.y) (c.y-b.y) <= 0);
29
30 #endif
31 void ConvexHull(vector<PT> &pts) {
      sort(pts.begin(), pts.end());
32
      pts.erase(unique(pts.begin(), pts.end()), pts.end());
33
      vector<PT> up, dn;
34
      for (int i = 0; i < pts.size(); i++) {
35
          while (up.size() > 1 \& area2(up[up.size()-2], up.back(),
36
      pts[i]) >= 0) up.pop_back();
          while (dn.size() > 1 \& area2(dn[dn.size()-2], dn.back(),
37
      pts[i]) <= 0) dn.pop_back();</pre>
          up.push_back(pts[i]);
38
          dn.push_back(pts[i]);
39
40
      pts = dn;
41
      for (int i = (int) up.size() - 2; i >= 1; i--) pts.push_back(
42
     up[i]);
      #ifdef REMOVE_REDUNDANT
43
      if (pts.size() <= 2) return;</pre>
44
      dn.clear();
45
      dn.push_back(pts[0]);
46
      dn.push_back(pts[1]);
47
      for (int i = 2; i < pts.size(); i++) {
48
          if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i])) dn
49
     .pop_back();
          dn.push_back(pts[i]);
50
51
      if (dn.size() >= 3 \& between(dn.back(), dn[0], dn[1])) {
```

 $PT(T x, T y) : x(x), y(y) {}$

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3.3 Kardak Find intersection between lines

```
struct Point{
int x, y;};
3 // A line segment with left as Point
4 // with smaller x value and right with
5 // larger x value.
6 struct Segment{
    Point left, right; };
8 struct Event {
    int x, y;
    bool isLeft;
    int index;
    Event(int x, int y, bool 1, int i) : x(x), y(y), isLeft(1),
     index(i) {}
    bool operator<(const Event& e) const {</pre>
        if(y==e.y)return x<e.x;</pre>
        return y < e.y; \} \};
16 // point q lies on line segment 'pr'
bool onSegment(Point p, Point q, Point r){
   if (q.x \le max(p.x, r.x) \& q.x >= min(p.x, r.x) \& \&
      q.y \le max(p.y, r.y) \& q.y >= min(p.y, r.y)
    return true:
    return false;}
int orientation(Point p, Point q, Point r){
    int val = (q.y - p.y) (r.x - q.x) -
        (q.x - p.x) (r.y - q.y);
    if (val == 0) return 0; // collinear
    return (val > 0)? 1: 2; // 1clock or 2counterclock wise
28 // The main function that returns true if line segment 'p1q1'
29 // and 'p2q2' intersect.
bool doIntersect(Segment s1, Segment s2){
    Point p1 = s1.left, q1 = s1.right, p2 = s2.left, q2 = s2.right;
    int o1 = orientation(p1, q1, p2);
```

```
int o2 = orientation(p1, q1, q2);
   int o3 = orientation(p2, q2, p1);
   int o4 = orientation(p2, q2, q1);
   if (o1 != o2 && o3 != o4)
    return true:
   if (o1 == 0 && onSegment(p1, p2, q1)) return true;
   if (o2 == 0 && onSegment(p1, q2, q1)) return true;
   if (o3 == 0 && onSegment(p2, p1, q2)) return true;
   if (o4 == 0 && onSegment(p2, q1, q2)) return true;
return false; // Doesn't fall in any of the above cases}
43 set<Event>::iterator pred(set<Event> &s, set<Event>::iterator it)
return it == s.begin() ? s.end() : —it;}
45 set<Event>::iterator succ(set<Event> &s, set<Event>::iterator it)
  return ++it;}
47 // Returns true if any two lines intersect.
48 int isIntersect(Segment arr[], int n){
   unordered_map<string,int> mp;
   vector<Event> e;
   for (int i = 0; i < n; ++i) {
      e.push_back(Event(arr[i].left.x, arr[i].left.y, true, i));
52
      e.push_back(Event(arr[i].right.x, arr[i].right.y, false, i))
53
     ; }
   sort(e.begin(), e.end(), [](Event &e1, Event &e2) {return e1.x
    < e2.x; \});
   set < Event > s;
   int ans=0;
   for (int i=0; i<2n; i++){
      Event curr = e[i];
58
      int index = curr.index;
59
      if (curr.isLeft){
60
        auto next = s.lower_bound(curr);
61
        auto prev = pred(s, next);
        bool flag=false;
63
        if (next != s.end() && doIntersect(arr[next->index], arr[
     index])){
          string s=to_string(next->index+1)+" "+to_string(index+1);
65
          if (mp.count(s) == 0) \{mp[s] ++; ans ++; \} //if not already
66
     checked we can increase count in map
```

```
if (prev != s.end() && doIntersect(arr[prev->index], arr[
                    index])){
                                             string s=to_string(prev->index+1)+" "+to_string(index
                    +1);
                                     if (mp.count(s)==0) \{mp[s]++; ans++;\} //if not already
70
                     checked we can increase count in map
71
                               if(prev != s.end() && next != s.end() && next->index==prev
72
                    ->index)ans--:
                               s.insert(curr);}
                       else{
74
                               auto it=s.find(Event(arr[index].left.x, arr[index].left.y,
                     true, index));
                               auto next = succ(s, it);
                               auto prev = pred(s, it);
                               if (next != s.end() && prev != s.end())
                              { string s=to_string(next->index+1)+" "+to_string(prev->
                    index+1):
                                             string s1=to_string(prev->index+1)+" "+to_string(next->
                    index+1);
                                     if (mp.count(s)==0&&mp.count(s1)==0&&doIntersect(arr[prev
                    ->index], arr[next->index]))
                                             ans++;
                                             mp[s]++;}
                               s.erase(it);
84
85
86
                for(auto &pr:mp){
                        cout << pr. first << "\n";}
               return ans;}
90 int main() {
               Segment arr[] = \{\{1, 5\}, \{4, 5\}\}, \{\{2, 5\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 1\}\}, \{\{3, 2\}, \{10, 2\}, \{10, 2\}\}, \{\{3, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}\}, \{\{3, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}\}, \{\{3, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}\}, \{\{3, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 2\}, \{10, 
                   \{10, 3\}\}, \{\{6, 4\}, \{9, 4\}\}, \{\{7, 1\}, \{8, 1\}\}\};
               int n = sizeof(arr)/sizeof(arr[0]);
               cout << isIntersect(arr, n);</pre>
               return 0;}
```

3.4 Kardak Half Plane Intersection

```
const long double eps = 1e-9, inf = 1e9;
struct Point {
```

```
long double x, y;
      explicit Point(long double x = 0, long double y = 0) : x(x),
     y(y) {}
      friend Point operator + (const Point& p, const Point& q) {
          return Point(p.x + q.x, p.y + q.y);
      friend Point operator — (const Point& p, const Point& q) {
9
          return Point(p.x - q.x, p.y - q.y);
10
11
      friend Point operator (const Point& p, const long double& k
12
     ) {
          return Point(p.x
                              k, p.y
                                        k);
13
14
      friend long double cross(const Point& p, const Point& q) {
15
          return p.x q.y - p.y q.x;
16
17
18 };
19 struct Halfplane {
      // 'p' is a passing point of the line and 'pq' is the
     direction vector of the line.
      Point p, pq;
21
      long double angle;
22
      Halfplane() {}
23
      Halfplane(const\ Point\&\ a,\ const\ Point\&\ b): p(a), pq(b-a)
24
          angle = atan21(pq.y, pq.x);
25
26
27
      // Every half-plane allows the region to the LEFT of its line
      bool out(const Point& r) {
28
          return cross(pq, r - p) < -eps;
29
30
      bool operator < (const Halfplane& e) const {</pre>
31
          if (fabsl(angle - e.angle) < eps) return cross(pq, e.p -</pre>
32
     p) < 0;
          return angle < e.angle;</pre>
33
34
      bool operator == (const Halfplane& e) const {
35
          return fabsl(angle - e.angle) < eps;</pre>
36
37
      friend Point inter(const Halfplane& s, const Halfplane& t) {
38
          long double alpha = cross((t.p - s.p), t.pq) / cross(s.pq)
39
```

```
, t.pq);
          return s.p + (s.pq)
                                alpha);
42 };
43 vector<Point> hp_intersect(vector<Halfplane>& H) {
      Point box[4] = { // Bounding box in CCW order
45
          Point(inf, inf),
46
          Point(-inf, inf),
47
          Point(-inf, -inf),
          Point(inf, -inf)
      };
50
      for(int i = 0; i < 4; i++) { // Add bounding box half-planes.
51
          Halfplane aux(box[i], box[(i+1) % 4]);
52
          H. push_back(aux);
53
54
      sort(H.begin(), H.end());
55
      H.erase(unique(H.begin(), H.end());
      deque<Halfplane> dq;
      int len = 0;
      for(int i = 0; i < int(H.size()); i++) {
          while (len > 1 && H[i].out(inter(dq[len-1], dq[len-2])))
              dq.pop_back();
              -len;
62
          while (len > 1 && H[i].out(inter(dq[0], dq[1]))) {
              dq.pop_front();
              -len;
          dq.push_back(H[i]);
          ++len:
70
      while (len > 2 && dq[0].out(inter(dq[len-1], dq[len-2]))) {
71
          dq.pop_back();
72
          -len;
73
74
      while (len > 2 && dq[len-1].out(inter(dq[0], dq[1]))) {
75
          dq.pop_front();
          -len;
77
```

```
if (len < 3) return vector<Point>();
vector<Point> ret(len);
for(int i = 0; i+1 < len; i++) {
    ret[i] = inter(dq[i], dq[i+1]);
}
ret.back() = inter(dq[len-1], dq[0]);
return ret;
}</pre>
```

4 Data Structures

4.1 Fenwick1

```
\frac{1}{1} const int MAXN = 1 1000 + 10;
int fen[MAXN]; // 0-based, [)
void add(int x, int val = 1) {
for (int i = x + 1; i < MAXN; i += i & (-i))
      fen[i] += val;
6 }
7 int get(int x) {
s int ans = 0;
   for (int i = x; i > 0; i = i & (-i))
     ans += fen[i];
   return ans;
11
12
int sum(int x, int y) {
return get(y) - get(x);
15
```

4.2 Fenwick2

```
int fen[MAXN]; // 0-based, [)
void add(int x, int val) {
   for (int i = x; i > 0; i -= i & (-i))
      fen[i] += val;
}
int get(int x) {
   int ans = 0;
   for (int i = x + 1; i < MAXN; i += i & (-i))
      ans += fen[i];
   return ans;
}</pre>
```

```
void update(int 1, int r, int val) {
   add(r, +val);
   add(1, -val);
}
```

4.3 Segment Tree Lazy Propagation

```
int seg[4 MAXN], add[4 MAXN];
inline void shift(int x, int s, int e) {
    int 1c = x + x + 0, rc = x + x + 1;
    int mid = (s + e) / 2;
    int 11 = mid - s, 12 = e - mid;
    seg[lc] += 11 \quad add[x];
    seg[rc] += 12 add[x];
    add[lc] += add[x];
    add[rc] += add[x];
    add[x] = 0;
^{12} // lo, hi -> [)
\frac{13}{3} // s = 0, e = n, x = 1
void update(int lo, int hi, int s, int e, int x, int delta) {
   if (lo == s && hi == e) {
     int len = (e - s);
      seg[x] = seg[x] + len
                              delta;
      add[x] = add[x] + delta;
     return ;
    shift(x, s, e);
    int mid = (s + e) / 2;
    int 1c = x + x + 0, rc = x + x + 1;
    if (lo < mid) update(lo, min(mid, hi), s, mid, lc, delta);</pre>
    if (hi > mid) update(max(lo, mid), hi, mid, e, rc, delta);
    seg[x] = seg[lc] + seg[rc];
int get(int lo, int hi, int s, int e, int x) {
   if (lo == s && hi == e) return seg[x];
    shift(x, s, e);
    int mid = (s + e) / 2;
    int res = 0;
    if (lo < mid) res += get(lo, min(mid, hi), s, mid, x + x + 0);
    if (hi > mid) res += get(max(lo, mid), hi, mid, e, x + x + 1);
    return res;
```

```
4.4 RMQ
_{1} const int N = 1000
                      100 + 5, LOG = 20;
class RMQ{
int f[LOG][N], Lgl[N], S;
4 public:
    RMQ() {
      for(int i = 1, p = 0; i < N; ++i) {
        if(i == 1 << (p + 1))
         ++p;
        Lgl[i] = p;
9
10
11
    void build(int a[], int n) {
12
      for(int i = 0; i < n; ++i)
13
        f[0][i] = a[i];
14
15
      for (int j = 1, p = 1; j < LOG; ++j, p = 2)
16
        for(int i = 0; i < n; ++i) {
17
          f[j][i] = f[j - 1][i];
18
         if(i + p < n)
19
            f[j][i] = min(f[j-1][i], f[j-1][i+p]);
21
22
    int find(int s, int e) {
23
     int l = Lgl[e - s + 1];
      return min(f[1][s], f[1][e + 1 - (1 << 1)]);
25
```

4.5 Trie

26

27 };

```
struct Node {
   char x;
   vector<Node > adj;
   Node () {
       x = 0;
   }
   Node (char a) {
       x = a;
   }
}
```

```
Node add_edge(char a) {
      for (int i = 0; i < SZ(adj); i ++)
        if (adj[i]->x == a)
          return adj[i];
13
      adj.pb(new Node(a));
14
      return adj.back();
16
17 };
18 struct Trie {
    Node root;
    Trie() {
      root = new Node();
21
    void add(string &s) {
      add(s, 0, root);
    void add(string &s, int pos, Node node) {
      if (pos == SZ(s)) {
        return ;
      } else {
        Node next = node->add_edge(s[pos]);
        add(s, pos + 1, next);
32
33
34 };
```

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5 String

5.1 Hash

```
1 ll p[MAXN], hash[MAXN];
2 int main () {
3  p[0] = 1;
4  for (int i = 1; i < MAXN; i ++)
5  p[i] = p[i - 1]  BASE;
6  string s;
7  getline(cin, s);
8  for (int i = 1; i <= SZ(s); i ++)
9  hash[i] = hash[i - 1]  BASE + s[i - 1];
10  // hash in [i, j], 1-based</pre>
```

```
11 ll h = hash[j] - (hash[i - 1] p[j - i + 1]);
 5.2 KMP
#define SZ(x) (int)((x).size())
_2 const int M = 1000
                      100 + 4;
3 int f[M];
4 string s,t;
5 bool match[M];
6 void kmp() {
   f[0] = -1;
   int pos = -1;
   for (int i = 1; i \le SZ(t); i++) {
      while (pos != -1 \&\& t[pos] != t[i - 1]) pos = f[pos];
      f[i] = ++pos;
11
12
    pos = 0;
13
   for (int i = 0; i < SZ(s); i++) {
     while (pos != -1 \&\& (pos == SZ(t) || s[i] != t[pos])) pos = f[
15
     pos];
      pos ++;
16
     if (pos == SZ(t)) match[i] = 1;
17
      else match[i] = 0;
18
19
20 }
```

5.3 Suffix Array

```
const int N = 1000     100 + 5; //max string length
namespace Suffix{
   int sa[N], rank[N], lcp[N], gap, S;

bool cmp(int x, int y) {
   if(rank[x] != rank[y])
      return rank[x] < rank[y];
   x += gap, y += gap;
   return (x < S && y < S)? rank[x] < rank[y]: x > y;
}

void Sa_build(const string &s) {
   S = s.size();
   int tmp[N] = {0};
   for(int i = 0; i < S; ++i)</pre>
```

```
rank[i] = s[i],
        sa[i] = i;
      for(gap = 1;; gap <<= 1) 
        sort(sa, sa + S, cmp);
        for(int i = 1; i < S; ++i)
          tmp[i] = tmp[i - 1] + cmp(sa[i - 1], sa[i]);
        for (int i = 0; i < S; ++i)
          rank[sa[i]] = tmp[i];
        if(tmp[S - 1] == S - 1)
          break;
24
25
    void Lcp_build() {
      for (int i = 0, k = 0; i < S; ++i, --k)
        if(rank[i] != S - 1) {
          k = max(k, 0);
          while(s[i + k] == s[sa[rank[i] + 1] + k])
            ++k:
          lcp[rank[i]] = k;
        else
          k = 0;
35
36
37 };
```

5.4 Kardak AhoCorasick

```
// for string matching
using namespace std;
#include <bits/stdc++.h>

// Max number of states in the matching machine.

// Should be equal to the sum of the length of all keywords.

const int MAXS = 500;

// Maximum number of characters in input alphabet

const int MAXC = 26;

// OUTPUT FUNCTION IS IMPLEMENTED USING out[]

// Bit i in this mask is one if the word with index i

// appears when the machine enters this state.

int out[MAXS];

// FAILURE FUNCTION IS IMPLEMENTED USING f[]

int f[MAXS];

// GOTO FUNCTION (OR TRIE) IS IMPLEMENTED USING g[][]
```

int g[MAXS][MAXC];

```
17 // Builds the string matching machine.
_{18} // arr - array of words. The index of each keyword is important:
19 //
         "out[state] & (1 << i)" is > 0 if we just found word[i]
20 //
         in the text.
21 // Returns the number of states that the built machine has.
_{22} // States are numbered 0 up to the return value - 1, inclusive.
int buildMatchingMachine(string arr[], int k)
24 {
    memset(out, 0, sizeof out);
25
    memset(g, -1, sizeof g);
   int states = 1;
27
    for (int i = 0; i < k; ++i)
28
29
      const string &word = arr[i];
30
      int currentState = 0;
31
      for (int j = 0; j < word.size(); ++j)
32
33
        int ch = word[j] - 'a';
34
        if (g[currentState][ch] == -1)
35
          g[currentState][ch] = states++;
36
        currentState = g[currentState][ch];
37
38
      out[currentState] |= (1 << i);
39
40
    for (int ch = 0; ch < MAXC; ++ch)
41
      if (g[0][ch] == -1)
        g[0][ch] = 0;
43
    memset(f, -1, sizeof f);
44
    queue<int> q;
    for (int ch = 0; ch < MAXC; ++ch)
46
47
      if (g[0][ch] != 0)
48
49
        f[g[0][ch]] = 0;
50
        q.push(g[0][ch]);
51
52
53
    while (q.size())
54
55
      int state = q.front();
```

```
q.pop();
      for (int ch = 0; ch \leq MAXC; ++ch)
58
        if (g[state][ch] != -1)
61
          int failure = f[state];
62
          while (g[failure][ch] == -1)
63
            failure = f[failure];
64
          failure = g[failure][ch];
          f[g[state][ch]] = failure;
          out[g[state][ch]] |= out[failure];
          q.push(g[state][ch]);
69
71
    return states;
74 // Returns the next state the machine will transition to using
     goto
75 // and failure functions.
<sub>76</sub> // currentState — The current state of the machine. Must be
     between
77 //
           0 and the number of states -1, inclusive.
<sub>78</sub> // nextInput — The next character that enters into the machine.
int findNextState(int currentState, char nextInput)
    int answer = currentState;
    int ch = nextInput - 'a';
    while (g[answer][ch] == -1)
      answer = f[answer];
    return g[answer][ch];
87 // This function finds all occurrences of all array words
88 // in text.
void searchWords(string arr[], int k, string text)
90
    buildMatchingMachine(arr, k);
    int currentState = 0;
    for (int i = 0; i < text.size(); ++i)
      currentState = findNextState(currentState, text[i]);
```

```
if (out[currentState] == 0)
        continue;
97
      for (int j = 0; j < k; ++ j)
        if (out[currentState] & (1 << j))</pre>
100
           cout << "Word " << arr[j] << " appears from "</pre>
102
            << i - arr[j].size() + 1 << " to " << i << endl;
104
105
106
107
108 // Driver program to test above
int main()
110
    string arr[] = {"he", "she", "hers", "his"};
    string text = "ahishers";
112
    int k = sizeof(arr)/sizeof(arr[0]);
113
    searchWords(arr, k, text);
114
    return 0;
115
116
```

6 Number Theory

6.1 Phi

```
#include <iostream>
# include <vector>
3 using namespace std;
_{4} const int N = 1000
                        1000;
5 vector <int> pr;
6 int lp[N], phi[N];
void Sieve(int n){
   for (int i = 2; i < n; ++i) {
      if (lp[i] == 0)
        lp[i] = i,
10
        pr.push_back(i);
11
12
      for (int j = 0; j < pr. size() && pr[j] <= lp[i] && i</pre>
                                                               pr[j] <
13
      n; ++j
        lp[i
               pr[j]] = pr[j];
```

```
16
void Find_Phi(int n) {
    phi[1] = 1;
    for (int i = 2; i < n; ++i) {
      if(lp[i] == i)
        phi[i] = i - 1;
21
      else {
22
        phi[i] = phi[lp[i]]
                               phi[(i / lp[i])];
23
        if(lp[i / lp[i]] == lp[i])
          phi[i] = lp[i], phi[i] /= (lp[i] - 1)
26
27
```

6.2 370 SGU

```
bool mark[MAXN];
vector<int> dv[MAXN];
3 int n, m;
4 // counts positive integers up to n that are relatively prime to
5 int f(int x) {
   int res = 0;
    for (int mask = 0; mask < (1 << SZ(dv[x])); mask ++) {
     int t = __builtin_popcount(mask), a = n - 1;
      for (int i = 0; i < SZ(dv[x]); i ++)
       if (mask & (1 << i))
          a /= dv[x][i];
      if (t & 1) res -= a;
      else res += a;
    return res;
int main () {
    for (int i = 2; i < n; i ++)
     if (!mark[i]) {
        for (int j = i; j < m; j += i) {
          mark[j] = true;
          dv[j].pb(i);
23
```

```
11 ans = 2;
  for (int i = 1; i < m; i ++) ans += f(i);
cout << ans << endl;
return 0;
}</pre>
```

6.3 Euclid

```
typedef vector<int> VI;
typedef pair<int, int> PII;
3 // computes gcd(a,b)
4 int gcd(int a, int b) {
while (b) { int t = a%b; a = b; b = t; }
6 return a;
7 }
_{\rm 8} // returns g = gcd(a, b); finds x, y such that d = ax + by
int extended_euclid(int a, int b, int &x, int &y) {
   int xx = y = 0;
   int yy = x = 1;
   while (b) {
12
    int q = a / b;
13
    int t = b; b = a%b; a = t;
14
    t = xx; xx = x - q xx; x = t;
15
     t = yy; yy = y - q yy; y = t;
16
17
   return a;
18
19
20 // finds all solutions to ax = b (mod n)
21 VI modular_linear_equation_solver(int a, int b, int n) {
int x, y;
   VI ret;
   int g = extended_euclid(a, n, x, y);
   if (!(b%g)) {
    x = mod(x (b / g), n);
     for (int i = 0; i < g; i++)
        ret.push_back(mod(x + i (n / g), n));
28
29
   return ret;
30
_{
m 32} // Chinese remainder theorem (special case): find z such that
_{33} // z % m1 = r1, z % m2 = r2. Here, z is unique modulo M = lcm(m1
  , m2).
```

```
^{34} // Return (z, M). On failure, M = -1.
PII chinese_remainder_theorem(int m1, int r1, int m2, int r2) {
    int s, t;
    int g = extended_euclid(m1, m2, s, t);
    if (r1\%g != r2\%g) return make_pair(0, -1);
    return make_pair(mod(s r2 m1 + t r1 m2, m1 m2) / g, m1 m2 / g);
41 // Chinese remainder theorem: find z such that
_{42} // z % m[i] = r[i] for all i. Note that the solution is
_{43} // unique modulo M = lcm_i (m[i]). Return (z, M). On
_{44} // failure, M = -1. Note that we do not require the a[i]'s
45 // to be relatively prime.
46 PII chinese_remainder_theorem(const VI &m, const VI &r) {
    PII ret = make_pair(r[0], m[0]);
    for (int i = 1; i < m.size(); i++) {</pre>
      ret = chinese_remainder_theorem(ret.second, ret.first, m[i],
     r[i]);
      if (ret.second == -1) break;
51
    return ret;
53
```

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6.4 C(n, r)

```
1 ll bin_pow(ll x, ll y) {
2    if (y == 0) return 1;
3
4    ll tmp = bin_pow(x, y / 2);
5    ll res = SQR(tmp) % MOD;
6    if (y & 1) res = (res x) % MOD;
7    return res;
8 }
9 ll fct[MAXN], rev[MAXN], fct_rev[MAXN];
10 void init(int n) {
11    fct[0] = 1;
12    for (int i = 1; i <= n; i ++)
13    fct[i] = (fct[i - 1] i) % MOD;
14
15    rev[0] = 1;
16    for (int i = 1; i <= n; i ++)
17    rev[i] = bin_pow(i, MOD - 2);
18</pre>
```

```
fct_rev[0] = 1;
for (int i = 1; i <= n; i ++)
    fct_rev[i] = (fct_rev[i - 1] rev[i]) % MOD;

int C(int n, int r) {
   return (((fct[n] fct_rev[r]) % MOD) fct_rev[n - r]) % MOD;
}</pre>
```

6.5 FFT

```
typedef long double DOUBLE;
typedef complex < DOUBLE > COMPLEX;
s typedef vector<DOUBLE> VD;
4 typedef vector<COMPLEX> VC;
5 struct FFT {
      VC A;
      int n, L;
      int ReverseBits(int k) {
9
          int ret = 0;
10
          for (int i = 0; i < L; i++) {
11
              ret = (ret << 1) | (k & 1);
              k >>= 1;
13
14
          return ret;
15
16
      void BitReverseCopy(VC a) {
17
          for (n = 1, L = 0; n < a.size(); n <<= 1, L++);
18
          A.resize(n);
19
          for (int k = 0; k < n; k++)
20
          A[ReverseBits(k)] = a[k];
21
22
      VC DFT(VC a, bool inverse) {
23
          BitReverseCopy(a);
24
          for (int s = 1; s <= L; s++) {
              int m = 1 << s;
26
              COMPLEX wm = exp(COMPLEX(0, 2.0))
                                                  M_PI / m);
27
              if (inverse) wm = COMPLEX(1, 0) / wm;
              for (int k = 0; k < n; k += m) {
29
                   COMPLEX w = 1;
                   for (int j = 0; j < m/2; j++) {
31
                       COMPLEX t = w A[k + j + m/2];
```

```
COMPLEX u = A[k + j];
                       A[k + j] = u + t;
                       A[k + j + m/2] = u - t;
                       w = w
                               wm;
          if (inverse) for (int i = 0; i < n; i++) A[i] /= n;
          return A;
41
42
      // c[k] = sum_{i=0}^k a[i] b[k-i]
43
      VD Convolution(VD a, VD b) {
44
          int L = 1;
          while ((1 << L) < a.size()) L++;</pre>
          while ((1 << L) < b.size()) L++;
          int n = 1 << (L+1);
          VC aa, bb;
          for (size_t i = 0; i < n; i++) aa.push_back(i < a.size()
     ? COMPLEX(a[i], 0) : 0);
          for (size_t i = 0; i < n; i++) bb.push_back(i < b.size()
51
     ? COMPLEX(b[i], 0) : 0);
          VC AA = DFT(aa, false);
          VC BB = DFT(bb, false);
53
          VC CC;
54
          for (size_t i = 0; i < AA.size(); i++) CC.push_back(AA[i]</pre>
         BB[i]);
          VC cc = DFT(CC, true);
          VD c;
          for (int i = 0; i < a.size() + b.size() - 1; i++) c.
58
      push_back(cc[i].real());
          return c;
59
60
61 };//aslesh akhareshe ke miad a ro to b zarb mikone ke do ta
      chanjomleian orderesh age n maximum darage bashe mishe O(nlgn)
```

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6.6 Gauss Jordan

```
// Gauss—Jordan elimination with full pivoting.
//
//
// Uses:
// (1) solving systems of linear equations (AX=B)
// (2) inverting matrices (AX=I)
```

```
(3) computing determinants of square matrices
7 //
8 // Running time: O(n<sup>3</sup>)
9 //
10 // INPUT:
               a[][] = an nxn matrix
               b[][] = an nxm matrix
11 //
12 //
13 // OUTPUT:
               Χ
                      = an nxm matrix (stored in b[][])
               A^{-1} = an nxn matrix (stored in a[][])
14 //
               returns determinant of a[][]
15 //
const double EPS = 1e-10;
typedef vector<int> VI;
18 typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
1 T GaussJordan(VVT &a, VVT &b) {
const int n = a.size();
   const int m = b[0].size();
   VI irow(n), icol(n), ipiv(n);
   T det = 1;
25
   for (int i = 0; i < n; i++) {
     int pj = -1, pk = -1;
     for (int j = 0; j < n; j++) if (!ipiv[j])
      for (int k = 0; k < n; k++) if (!ipiv[k])
      if (pj == -1 \mid | fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk}
30
      = k; 
      if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." <<</pre>
31
      endl; exit(0); }
      ipiv[pk]++;
32
      swap(a[pj], a[pk]);
33
      swap(b[pj], b[pk]);
34
      if (pj != pk) det = -1;
35
      irow[i] = pj;
36
      icol[i] = pk;
37
      T c = 1.0 / a[pk][pk];
38
      det = a[pk][pk];
39
      a[pk][pk] = 1.0;
40
      for (int p = 0; p < n; p++) a[pk][p] = c;
      for (int p = 0; p < m; p++) b[pk][p] = c;
      for (int p = 0; p < n; p++) if (p != pk) {
        c = a[p][pk];
44
```

```
a[p][pk] = 0;
        for (int q = 0; q < n; q++) a[p][q] -= a[pk][q]
                                                              С;
        for (int q = 0; q < m; q++) b[p][q] = b[pk][q]
                                                              С;
    for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
      for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p
     ]]);
    return det;
54
55 int main() {
    const int n = 4;
    const int m = 2;
    double A[n][n] = \{ \{1,2,3,4\}, \{1,0,1,0\}, \{5,3,2,4\}, \{6,1,4,6\} \};
    double B[n][m] = \{ \{1,2\}, \{4,3\}, \{5,6\}, \{8,7\} \};
    VVT a(n), b(n);
    for (int i = 0; i < n; i++) {
      a[i] = VT(A[i], A[i] + n);
      b[i] = VT(B[i], B[i] + m);
    double det = GaussJordan(a, b);
66 }// hale n moadele n majhool O(n ^ 3)
```

7 Other

7.1 Read Input

```
inline int read() {
   bool minus = false;
   int result = 0;
   char ch;
   ch = getchar();
   while (true) {
      if (ch == '-') break;
      if (ch >= '0' && ch <= '9') break;
      ch = getchar();
   }
   if (ch == '-') minus = true; else result = ch-'0';
   while (true) {
      ch = getchar();
   }
</pre>
```

```
if (ch < '0' || ch > '9') break;
result = result 10 + (ch - '0');
}
if (minus)
return -result;
else
return result;
}
```

7.2 LIS

```
int c[MAXN], a[MAXN];
1 int main() {
₃ int n;
    cin >> n;
   for (int i = 0; i < n; i ++) cin >> a[i];
   for (int i = 0; i \le n; i ++) c[i] = 1e9;
   int ans = 0;
   for (int i = 0; i < n; i ++) {
     int 1 = 0, r = i + 1;
      while (r - 1 > 1) {
       int mid = (1 + r) / 2;
        if (c[mid] <= a[i]) l = mid;</pre>
        else r = mid;
13
14
      ans = max(ans, 1 + 1);
15
      if (c[l + 1] > a[i]) c[l + 1] = a[i];
16
17
    cout << ans << endl;</pre>
18
19 }
```

7.3 Divide and Conquer Tree

```
#include <iostream>
#include <vector>
using namespace std;
const int N = 1000     100 + 5;
vector <int> adj[N];
int is_av[N], _sz[N]; //XXX initiate is_av to 1
void set_size(int v, int p) {
```

```
_sz[v] = 1;
    for(int u:adj[v])
      if(u != p && is_av[u]) {
        set_size(u, v);
        _sz[v] += _sz[u];
12
13
14
void divide(int v) {
    set_size(v, v);
    int S = _sz[v], p = v;
      sign:
        for(int u:adj[v])
          if(is_av[u] && u != p && _sz[u] > S / 2) {
            p = v;
            v = u;
            goto sign;
      // now v is the centroid of the tree
      // Enter your code here
    is_av[v] = 0;
    for(int u:adj[v])
      if(is_av[u])
        divide(u);
31
32 int main() {
    ios::sync_with_stdio(false);
    int n;
    cin >> n;
    for(int i = 1; i < n; ++i) {
     int a, b;
      cin >> a >> b;
     ——a, ——b;
      adj[a].push_back(b);
      adj[b].push_back(a);
41
42
    fill(is_av, is_av + N, 1);
    divide(0);
    return 0;
46 }// peyda kardan centroid o bazgashti fek konam O(nlgn)
```