CS771: Machine Learning Assignment 1

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Part 1

For a single 32-bit PUF, we can guess the output by taking the sign of

$$\frac{1 + \operatorname{sign}(W^{\top}X + b)}{2}$$

where $X = [x_1, x_2, \dots, x_{32}]$ and $x_i = 1 - 2c_i$. (c_i denotes the input (0, 1) for multiplexer.)

For both PUFs, the output is given by:

$$\Delta = (((w_1)^T X + b_1) - ((w_1)^T X + b_2)),$$

Let's consider the following calculations:

$$W = w_1 - w_2$$
 and
$$b = b_1 - b_2$$

Output is decide by sign of $(W^TX+b)^2-\tau^2$ (as given in Question(squaring)) Including b in weight itself

Thus, increasing the dimension of X by 1.

 \therefore output is decided by the sign of $(W^TX)^2 - \tau^2$

$$(W^{T}X)^{2} - \tau^{2} \Rightarrow \sum_{i=0}^{32} (w_{i}x_{i})^{2} + \sum_{i=0}^{32} \sum_{j\neq i}^{32} w_{i}w_{j}x_{i}x_{j} - \tau^{2}$$

$$\therefore x_{i} = 1 \text{ or } -1 \Rightarrow x_{i}^{2} = 1$$

$$\therefore \sum_{i=0}^{32} (w_{i}x_{i})^{2} - \tau^{2} = \sum_{i=0}^{32} w_{i}^{2} - \tau^{2} = b,$$
also,
$$\sum_{i=0}^{32} \sum_{j\neq i}^{32} w_{i}w_{j}x_{i}x_{j} = (W')^{T}X'$$

$$W' = 2[w_0 \cdot w_1, w_1 \cdot w_2, \dots, w_{31} \cdot w_{32}]$$

$$X' = \phi(X) = [x_0 \cdot x_1, x_1 \cdot x_2, \dots, x_{31} \cdot x_{32}]$$

 \Rightarrow Here, X' is our feature vector of dimension:

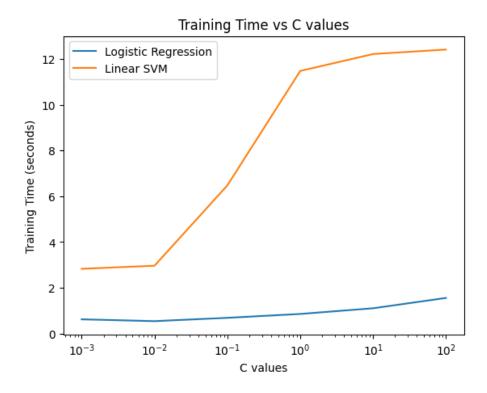
$$\binom{33}{2} = 528$$

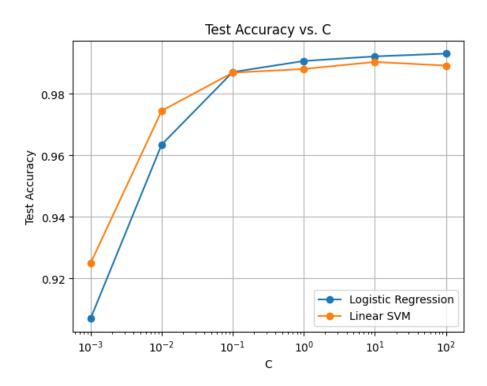
And our final output is decided by,

$$\frac{1 + \operatorname{sign}(W'^{\top}X' + b')}{2}$$

Part 3 - B

В





Part 3 - C

