

**MARWADI UNIVERSITY****Faculty of Technology**

Department of Information & Communication Technology

B.Tech**SEM: III****WINTER:2019****Subject: - Signals & Systems (01CT0302)****Date:- 12/10/2019****Total Marks:-100****Time: - 03:00 hours****Instructions:**

1. All Questions are Compulsory.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

Question: 1. (a) Answer the following: [10]

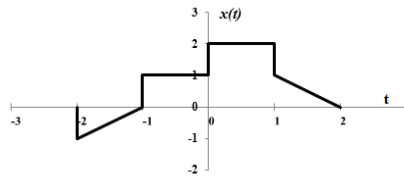
- (1) A system whose output depends upon future input is called
 (a) Static system (b) Causal system
 (c) Dynamic system (d) Non causal system
- (2) What is the rule $x(t)*h_1(t)+x(t)*h_2(t) = x(t)*[h_1(t)+h_2(t)]$ is called?
 (a) Commutative rule (b) Associative rule
 (c) Distributive rule (d) Transitive rule
- (4) Graphical representation of signal in frequency domain is called
 (a) Frequency Spectrum (b) Frequency
 (c) Wave form (d) None of the above
- (5) $Y(t) = x(t/3)$ is _____
 (a) Compressed signal (b) Expanded signal
 (c) Time shifted signal (d) Amplitude scaled signal by factor 1/3
- (6) An example of a discrete set of information/system is
 (a) The trajectory of the Sun (b) Data on a CD
 (c) Universe time scale (d) Movement of water through a pipe
- (7) $\delta(n) =$ _____
 (a) $u(n)+u(n-1)$ (b) $u(n)u(n-1)$
 (c) $u(n)-u(n-1)$ (d) $u(n-1)+u(n)$
- (8) Which of the following is an example of amplitude scaling?
 (a) Electronic amplifier (b) Electronic attenuator
 (c) Both amplifier and attenuator (d) Adder
- (9) A signal is power signal if
 (a) $E=0, P=0$ (b) $E= \text{infinite}, P=\text{Finite}$
 (c) $E= \text{finite}, P=0$ (d) $E= \text{finite}, P=\text{infinite}$
- (10) Which of the following method is not used for the inverse Z-transform.
 (a) Partial Fraction Expansion (b) Power series Expansion
 (c) Residue method (d) Slope over head method

(b) Attempt the following: (Two marks each) [10]

- (1) Examine whether the following signals are periodic or not?
 (a) $e^{j4\pi t}$ (b) $3 \sin 200\pi t + 4 \cos 100t$
- (2) Find even and odd component of following signal
 $x(t) = \sin 2t + \sin 2t \cos 2t + \cos 2t$
- (3) Find convolution of $x_1(n) = [1 \ 1 \ 2 \ 1]$ and $x_2(n) = [1 \ 4 \ 2 \ 3]$ using tabulation method.
- (4) State Commutative and Associative property for CT LTI system.
- (5) Describe benefits of Z- transform.

Question: 2.

- (a) Describe classification of systems in detail with example. [08]
- (b) Sketch the following signals:



- (i) $x(t-3)$ & $x(t/2)$ [02]
- (i) $-2r(t-2)$ [02]
- (iii) Check whether the signals are energy signal or power signal [04]
- (i) $(1/2)^n u(n)$ (ii) $x(t) = \begin{cases} t-2, & -2 \leq t \leq 0 \\ 2-t, & 0 \leq t \leq 2 \\ 0, & \text{otherwise} \end{cases}$

OR

- (b) For each of the following systems [08]
- (i) $y(n) = x(n) + nx(n-2)$
- (ii) $y(t) = tx(t)$
- Determine which of properties “Static/dynamic”, “time invariant/Variant”, “linear/Nonlinear”, “casual/Non causal” holds and justify your answer.

Question: 3.

- (a) State properties of LTI System. Prove a condition for a discrete time LTI system to be Causal and Stable. [08]
- (b) Prove that $x(n) * \delta(n-n_0) = x(n-n_0)$ [04]
- $x(n) \cdot \delta(n-n_0) = x(n_0)$
- (c) Find a linear convolution for $x(t) = e^{-at} u(t)$, $h(t) = u(t)$ [04]

OR

- (a) State and prove sampling theorem also draw frequency spectrum for $f_s \geq 2 f_m$, $f_s = 2 f_m$ and $f_s \leq 2 f_m$. [08]
- (b) Compute convolution for the following $x(n) = \{1, -2, 1\}$, and $h(n) = \{1, 1\}$. [04]
- (c) Find linear convolution using graphical method for $x(n) = \{1, 2\}$, $h(n) = \{1, 1, 2\}$ [04]

Question: 4.

- (a) Define ROC of Z- Transform. State and explain Properties of ROC. [08]
- (b) Find Z- Transform for the following also comment on ROC. [04]
- $x(n) = 2^n u[n] + 3^n u[-n-1]$
- (c) Find Z- transform of $x(n) = a^{|n|}$, $0 \leq a \leq 1$. Also comment on ROC. [04]

OR

- (a) State and Prove following properties of Z- Transform. [08]
- (i) Linearity (ii) Time Shifting (iii) Convolution (iv) Differentiation.
- (b) Find the z transform of signal $x(n) = \cos \omega_0 n u(n)$ [04]
- (c) Define Z-transform. State the relationship in between Z-transform and DTFT. [04]

Question: 5.

- (a) Using the partial fraction expansion technique find the inverse z transform of [08]

$$X(Z) = \frac{1-(1/2)Z^{-1}}{1+(3/4)Z^{-1}+(1/8)Z^{-2}} \quad \text{Find all possible } x(n)$$

- (b) Obtain Trigonometric Fourier series of the periodic rectangular waveform. [04]
 $f(t) = A, -T/4 \leq t \leq T/4$
 $= 0, \text{ otherwise}$
- (c) State and Prove Frequency Shifting Property of Fourier Transforms. [04]

OR

- (a) Find homogeneous solution of given differential equation [08]
 $y(n) - 3y(n-1) - 4y(n-2) = x(n)$
- (b) Find Fourier transform of a rectangular pulse 2 seconds long with a magnitude of 10 volts. [04]
- (c) State Dirichlet condition for Fourier Series representation. [04]

Question: 6.

- (a) Obtain Fourier transform of signal $x(t) = e^{-at}u(t) + e^{at}u(-t)$ for all t . [04]
- (b) A system is described by linear difference equation [04]
 $y(n) = 0.2x(n) - 0.5x(n-2) + 0.4x(n-3)$ given that the digital input sequence $\{-1, 1, 0, -1\}$ is applied to the system. Determine the corresponding output sequence.
- (c) Define Laplace transform. Explain mapping of S-Plane and Z-Plane. [04]

OR

- (a) Compute convolution for the CT-LTI system [08]
 $x(t) = 1, -1 \leq t \leq 1$
 $h(t) = 2, 0 \leq t \leq 2$
- (b) State application of signals and systems explain any one in detail. [04]
- (c) Define: The continuous time Fourier transforms. State and prove convolution properties of continuous time Fourier Transform [04]

---Best of Luck---