

5.1

A	B	$(A \vee B)$	$\neg A$	$\neg A \rightarrow B$
0	0	0	1	0
0	1	1	1	1
1	0	1	0	1
1	1	1	0	1

$$(\neg A \rightarrow B) \equiv (A \vee B)$$

A	B	$(A \wedge B)$	$\neg B$	$A \rightarrow \neg B$	$\neg (A \rightarrow \neg B)$
0	0	0	1	1	0
0	1	0	0	1	0
1	0	0	1	0	1
1	1	1	0	1	0

$$\neg (A \rightarrow \neg B) \equiv (A \wedge B)$$

A	$\neg A$	$(A \rightarrow \neg A)$
0	1	1
1	0	0

$$(A \rightarrow \neg A) \equiv \neg A$$

$$6.2 \textcircled{a} \quad e(A, B) = (\neg A \vee \neg B) \wedge (\neg A \vee B) \wedge (A \wedge \neg B)$$

Representing (\neg) with $(-)$ bar, (\vee) with $+$, (\wedge) with (\cdot) .

$$(\bar{A} + \bar{B}) \cdot (\bar{A} + B) \cdot (A + \bar{B})$$

$$\bar{A} + (\bar{B} \cdot B) \cdot (A + \bar{B}) \quad (\text{distributivity})$$

$$\bar{A} + (0) \cdot (A + \bar{B}) \quad (\text{complementarity})$$

$$\bar{A} \cdot (A + \bar{B})$$

$$(\bar{A} \cdot A) + (\bar{A} \cdot \bar{B}) \quad (\text{distributivity})$$

$$0 + (\bar{A} \cdot \bar{B}) \quad (\text{complementarity})$$

$$(\bar{A} \cdot \bar{B}) = (\neg A \wedge \neg B)$$

$$(b) \quad F(A, B, C) = (A \wedge \neg B) \vee (A \wedge \neg B \wedge C)$$

$$(A \cdot \bar{B}) + (A \cdot \bar{B} \cdot C)$$

$$(\cancel{A} \cdot \bar{B}) \cdot (\bar{B})$$

$$(A \cdot \bar{B} + A \cdot \bar{B}) \cdot (A \cdot \bar{B} + C) \quad (\text{distributivity})$$

$$(A \cdot \bar{B}) \cdot (A \cdot \bar{B} + C) \quad (\text{? idempotence})$$

$$A \cdot \bar{B} \quad (\text{Absorption})$$

$$(A \wedge \neg B)$$

$$(c) \quad F(A, B, C, D) = (A \vee \neg(B \wedge A)) \wedge (C \vee (D \vee C))$$

$$(A + (\bar{B} + \bar{A})) \cdot (C + (D + C)) \quad (\text{De Morgan's})$$

$$(A + (\bar{A} + \bar{B})) \cdot (C + (C + D)) \quad (\text{commutativity})$$

$$((A + \bar{A}) + \bar{B}) \cdot ((C + C) + D) \quad (\text{associativity})$$

$$(1 + \bar{B}) \cdot (C + D)$$

(complementarity)

$$(1 + \bar{B}) \cdot (C + D)$$

(idempotence)

$$1 \cdot (C + D)$$

(identity)

$$(C + D) = (C \vee D)$$

(d) $\varphi(A, B, C) = (\neg(A \wedge B) \vee \neg C) \wedge (\neg A \vee B \vee \neg C)$

$$(\bar{A} + \bar{B}) + \bar{C} \cdot (\bar{A} + B + \bar{C}) \quad (\text{de Morgan's})$$

$$(\bar{A} + (\bar{B} + \bar{C})) \cdot (\bar{A} + B + \bar{C}) \quad (\text{associativity})$$

$$(\bar{A} + (\bar{C} + \bar{B})) \cdot (\bar{A} + B + \bar{C}) \quad (\text{commutativity})$$

$$((\bar{A} + \bar{C}) + \bar{B}) \cdot (\bar{A} + B + \bar{C}) \quad (\text{associativity})$$

$$(\bar{A} + \bar{C} + (\bar{B} \cdot B)) \quad (\text{distributivity})$$

$$(\bar{A} + \bar{C}) \quad (\text{complementarity})$$

$$(\neg A \vee \neg C)$$

(e) $\varphi(A, B) = (A \vee B) \wedge (\neg A \vee B) \wedge (A \vee \neg B) \wedge (A \vee \neg B)$

$$(A + B) \cdot (\bar{A} + B) \cdot (A + \bar{B}) \cdot (\bar{A} + \bar{B})$$

$$A + (B \cdot \bar{B}) \cdot (\bar{A} + B) \cdot (\bar{A} + \bar{B}) \quad (\text{distributivity})$$

$$A + (0) \cdot (\bar{A} + B) \cdot (\bar{A} + \bar{B}) \quad (\text{complementarity})$$

$$A \cdot \bar{A} + (B \cdot \bar{B})$$

(distributivity)

$$A \cdot \bar{A} + (0)$$

(complementarity)

$$0$$

(complementarity)

$$6.3 \quad \text{EL}(P, Q, R, S) = (\neg P \vee Q) \wedge (\neg Q \vee R) \wedge (\neg R \vee S) \wedge (\neg S \vee P)$$

Making a truth table

P	Q	R	S	ϕ
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

Therefore condition is satisfied in only 2 interpretation.

$$(b) (\neg P \wedge \neg Q \wedge \neg R \wedge \neg S) \vee (P \wedge Q \wedge R \wedge S)$$

(DNF) form .