MetaNet Tutorial

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About

1.1 Install

MetaNet is a comprehensive network analysis package, especially in various omics.

the latest version can be found in https://github.com/Asa12138/MetaNet.

for some data manipulation, we recommend to use dplyr

```
remotes::install_github('Asa12138/pcutils')
remotes::install_github('Asa12138/MetaNet',dependencies=T)
library(MetaNet)
library(igraph)
#data manipulation
library(dplyr)
sessionInfo()
```

```
## R version 4.2.2 (2022-10-31)
## Platform: aarch64-apple-darwin20 (64-bit)
## Running under: macOS Ventura 13.0.1
##
## Matrix products: default
## BLAS: /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/c/en_US.UTF-8/en_US.UTF-8
##
## attached base packages:
## [1] stats graphics grDevices utils datasets methods base
```

```
##
## loaded via a namespace (and not attached):
                     digest_0.6.31
   [1] bookdown_0.32
                                      lifecycle_1.0.3 magrittr_2.0.3
   [5] evaluate_0.19
                      rlang_1.0.6
                                                     cli_3.6.0
                                      stringi_1.7.8
## [9] rstudioapi_0.14 vctrs_0.5.1
                                      rmarkdown_2.19 tools_4.2.2
                                      xfun_0.36
## [13] stringr_1.5.0 glue_1.6.2
                                                      yaml_2.3.6
## [17] fastmap_1.1.0
                     compiler_4.2.2 htmltools_0.5.4 knitr_1.41
```

Introduction

2.1 Network

In mathematics, "networks" are often referred to as "graphs", and the mathematical field of graph research is called "graph theory".

The basic elements in a network graph are nodes and edges. When constructing a network graph, the objects are called "nodes" (vertices or nodes), and they are usually drawn as points; the connections between nodes are called "edges" (edges). or links), and they are usually drawn as lines between points.

We Can be divide into directed and undirected networks, weighted and unweighted networks according to the edges.

2.2 Network in omics

Networks can represent various systems in the real world, and have many applications in biological research, especially in systems biology: gene expression regulatory networks, metabolic networks, ecosystem space networks, microbial co-occurrence networks, protein interaction networks, etc.

WGCNA

Co-occurrence networks

PPI

2.3 Software

- R: igraph (https://igraph.org/), network
- Python: networkx (https://pypi.org/project/networkx/)

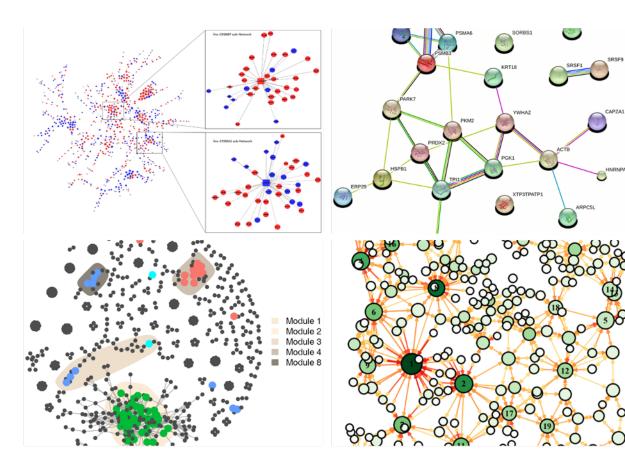


Figure 2.1: Applications of network in biology

2.4. METANET 9

- Pajek (http://vlado.fmf.uni-lj.si/pub/networks/pajek/)
- Cytoscape (https://cytoscape.org/)
- Gephi (https://gephi.org/)

2.4 MetaNet

MetaNet is a comprehensive network analysis package.

- Calculate correlation network quickly, accelerate lots of analysis by parallel computing.
- Support for multi-omics data, search sub-nets fluently.
- Handle bigger data, more than 10,000 nodes in each omics.
- Offer various layout method for multi-omics network and some interfaces to other software (Gephi, Cytoscape, ggplot), easy to visualize.
- Provide comprehensive topology indexes calculation including ecological network stability.

Construction

3.1 Pre-processing

The trans() function contains many normalization methods, suitable for preprocessing of different omics, some refer to vegan::decostand() (Oksanen et al. [2022]).

Table 3.1: Table 3.1: Normalization methods used in omics.

MethodDescription Counts per million minmax linear transfer to (min, max) Counts per million, then asinh transfer acpm log1log(n+1) transformat total divide by total divide by maximum \max frequencydivide by total and multiply by the number of non-zero items, so that the average of non-zero entries is one normalizemake margin sum of squares equal to one range standardize values into range 0 ... 1 (same to minmax(0,1)). If all values are constant, they will be transformed to 0. rank rank replaces abundance values by their increasing ranks leaving zeros unchanged rank replaces abundance values by their increasing ranks leaving rank, rrank zeros unchanged, and rrank is similar but uses relative ranks with maximum 1 scale x to presence/absence scale (0/1). pa standardizzale x to zero mean and unit variance hellinger square root of method = "total"

Table 3.1: Table 3.1: Normalization methods used in omics.

```
\begin{array}{ll} \log & \operatorname{logarithmic} \ \operatorname{transformation} \ \operatorname{as} \ \operatorname{suggested} \ \operatorname{by} \ \operatorname{Anderson} \ \operatorname{et} \ \operatorname{al.} \ (2006): \\ & \operatorname{logb}(\mathbf{x}) + 1 \ \operatorname{for} \ \mathbf{x} > 0, \ \operatorname{where} \ \operatorname{bb} \ \operatorname{is} \ \operatorname{the} \ \operatorname{base} \ \operatorname{of} \ \operatorname{the} \ \operatorname{logarithm}; \ \operatorname{zeros} \ \operatorname{are} \\ & \operatorname{left} \ \operatorname{as} \ \operatorname{zeros}. \\ & \operatorname{Additive} \ \operatorname{log} \ \operatorname{ratio} \ (\text{``alr''}) \ \operatorname{transformation} \ (\operatorname{Aitchison} \ 1986) \ \operatorname{reduces} \\ & \operatorname{data} \ \operatorname{skewness} \ \operatorname{and} \ \operatorname{compositionality} \ \operatorname{bias}. \\ & \operatorname{alr} = \left[ \log \frac{x_1}{x_D}, ..., \log \frac{x_{D-1}}{x_D} \right] \\ & \operatorname{clr} \quad \operatorname{centered} \ \operatorname{log} \ \operatorname{ratio} \ (\text{``clr''}) \ \operatorname{transformation} \ \operatorname{proposed} \ \operatorname{by} \ \operatorname{Aitchison} \\ & (1986) \ \operatorname{reduces} \ \operatorname{data} \ \operatorname{skewness} \ \operatorname{and} \ \operatorname{compositionality} \ \operatorname{bias}. \\ & \operatorname{clr} = \log \frac{x_r}{g(x_r)} \\ & \operatorname{robust} \ \operatorname{clr} \ (\text{``rclr''}) \ \operatorname{is} \ \operatorname{similar} \ \operatorname{to} \ \operatorname{regular} \ \operatorname{clr} \ (\operatorname{see} \ \operatorname{above}) \ \operatorname{but} \ \operatorname{allows} \ \operatorname{data} \\ & \operatorname{that} \ \operatorname{contains} \ \operatorname{zeroes}. \\ & \operatorname{rclr} = \log \frac{x_r}{g(x_r > 0)} \\ \end{array}
```

```
library(MetaNet)
data(otutab)
#trans(otutab, method="cpm")%>%head()
trans(otutab, method="log1")%>%head(4)
```

```
##
                                     NS1
                                              NS2
                                                       NS3
                                                                 NS4
                                                                          NS5
## s_un_f__Thermomonosporaceae 6.996681 7.560601 6.698268 7.211557 6.970730
## s__Pelomonas_puraquae
                                7.582229 7.118826 7.767687 7.712891 7.973844
## s__Rhizobacter_bergeniae
                                6.378426 6.129050 6.791221 6.804615 7.112327
## s Flavobacterium terrae
                                5.501258 5.459586 7.501634 6.513230 7.276556
##
                                     NS6
                                              WS1
                                                       WS2
                                                                 WS3
                                                                          WS4
## s_un_f_Thermomonosporaceae 6.976348 7.133296 7.376508 7.193686 6.848005
## s Pelomonas puraquae
                                7.512071 6.469250 6.206576 7.115582 7.158514
## s__Rhizobacter_bergeniae
                                6.749931 6.405228 6.154858 6.976348 6.936343
## s__Flavobacterium_terrae
                                6.198479 5.765191 7.563720 7.309212 6.903747
##
                                     WS5
                                              WS6
                                                       CS1
                                                                 CS2
## s_un_f_Thermomonosporaceae 7.118016 6.919684 7.746733 7.831617 7.444249
## s__Pelomonas_puraquae
                                6.860664 6.455199 7.174724 7.324490 6.739337
## s__Rhizobacter_bergeniae
                                6.741701 6.508769 6.937314 7.497207 6.910751
## s__Flavobacterium_terrae
                                6.359574 5.886104 6.985642 7.105786 6.626718
                                     CS4
                                              CS5
## s_un_f_Thermomonosporaceae 7.588830 7.266827 7.331715
## s__Pelomonas_puraquae
                                7.029088 7.302496 7.069023
## s__Rhizobacter_bergeniae
                                7.090910 7.085901 6.637258
## s__Flavobacterium_terrae
                                6.049733 6.940222 7.253470
```

guolv() and hebing() functions provide can help filter or aggregate the omics data.

3.2 Pairwise relationship

How to determine the pairwise relationship, because the experimental data is generally relatively rare, we mainly relying on statistical inference.

At present, there are mainly two ways, the first one is based on similarity or correlation Faust and Raes [2012]. for example: Spearman, Pearson, Bray-Curtis... based on abundance or incidence data, the similarity matrix between paired species can be calculated, and the randomized data can be used to repeatedly calculate the significance. Finally, meaningful similarities are retained in network.

The second way for networks is based on regression. Divide species into source and target, and use multiple regression to calculate the relationship between species.

Some tools use special methods to optimize the network construction, such as **SparCC**, etc.

3.2.1 Correlation

Correlation is a statistical term describing the degree to which two variables move in coordination with one-another.

Correlation calculation is the first step in all omics network analysis software, there are many method to get ρ and p-value. However, as the data size of omics grow larger and larger, many methods will become very time and computational resource consuming.

Here, we provide the c_net_cal() function for one single table or two tables to calculate correlation fastly (Figure 3.1), which will return a three elements list include ρ , p-value and p-adjust.

```
#single table
t(otutab) -> totu
c net cal(totu, method = "spearman", filename =F,p.adjust.method = NULL) -> corr
str(corr)
## List of 3
              : num [1:464, 1:464] 0 -0.2508 0.1847 0.0114 0.2095 ...
     ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s_Pelomonas_puraquae" "s_Rhizobacter_
    ....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s__Pelomonas_puraquae" "s__Rhizobacter_
##
    $ p.value : num [1:464, 1:464] 0 0.316 0.463 0.964 0.404 ...
##
     ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s_Pelomonas_puraquae" "s_Rhizobacter_
##
     ....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s__Pelomonas_puraquae" "s__Rhizobacter_
   $ p.adjust: num [1:464, 1:464] 0 0.316 0.463 0.964 0.404 ...
     ..- attr(*, "dimnames")=List of 2
```

```
....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s_Pelomonas_puraquae" "s_R
##
    ....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s_Pelomonas_puraquae" "s_R
#two tables
metadata[,3:10] -> env
c_net_cal(totu,env,method = "spearman", filename =F,p.adjust.method = NULL) -> corr2
str(corr2)
## List of 3
## $ r
             : num [1:464, 1:8] 0.356 -0.5253 0.0918 -0.0114 -0.0196 ...
    ..- attr(*, "dimnames")=List of 2
     ....$: chr [1:464] "s_un_f_Thermomonosporaceae" "s_Pelomonas_puraquae" "s_R
    ....$ : chr [1:8] "env1" "env2" "env3" "env4" ...
    $ p.value : num [1:464, 1:8] 0.147 0.0252 0.717 0.9643 0.9384 ...
##
    ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s_Pelomonas_puraquae" "s_R
##
    ....$ : chr [1:8] "env1" "env2" "env3" "env4" ...
## $ p.adjust: num [1:464, 1:8] 0.147 0.0252 0.717 0.9643 0.9384 ...
    ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:464] "s_un_f_Thermomonosporaceae" "s_Pelomonas_puraquae" "s_R
##
     ....$ : chr [1:8] "env1" "env2" "env3" "env4" ...
```

spearman based network of 1072 OTUs

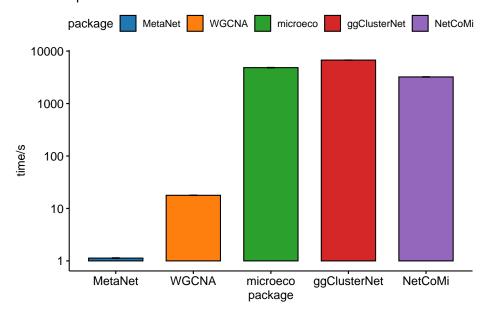


Figure 3.1: network build of packages comparison

3.2.2 Distance

you can use par_sim() to calculate various distance to get the pairwise similarity matrix.

3.2.3 SparCC

SparCC fits the Dirichlet distribution to the observed data, and iteratively calculates the proportion and correlation of species several times. The resulting correlation is the median of the distribution. p-values were calculated using the bootstrap method. This metric is said to be more useful with non-normal microbiome data.

$$D(x_i, x_j) = var(\log(\frac{x_i}{x_j}))$$

par_sparcc() is available for SparCC calculation.

3.2.4 Others

There are some other methods available for network construction in **NetCoMi**

3.3 Build network

3.3.1 Normally build

If you have done the c_net_cal(), you can get a network (igraph object) easily by c_net_build(). Some common attributes will be set automatically.

```
c_net_build(corr,r_thres = 0.6,p_thres = 0.05,del_single = T) -> co_net
co_net
## IGRAPH 4639c34 UNW- 462 1401 --
## + attr: n_{type} (g/c), name (v/c), v_{group} (v/c), v_{class} (v/c), size
## | (v/n), label (v/c), shape (v/c), color (v/c), id (e/n), from (e/c),
\#\# | to (e/c), weight (e/n), cor (e/n), p.adjust (e/n), p.value (e/n),
## | e_type (e/c), width (e/n), v_group_from (e/c), v_group_to (e/c),
## | e_class (e/c), color (e/c), lty (e/n)
## + edges from 4639c34 (vertex names):
## [1] s_un_f_Thermomonosporaceae--s_Actinocorallia_herbida
## [2] s_un_f__Thermomonosporaceae--s__Kribbella_catacumbae
## [3] s_un_f_Thermomonosporaceae--s_Kineosporia_rhamnosa
## [4] s_un_f_Thermomonosporaceae--s_un_f_Micromonosporaceae
## + ... omitted several edges
plot(co net)
c net build(corr2) -> co net2
plot(co_net2)
```

Co-occurrence network

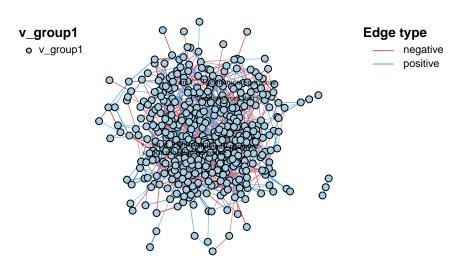
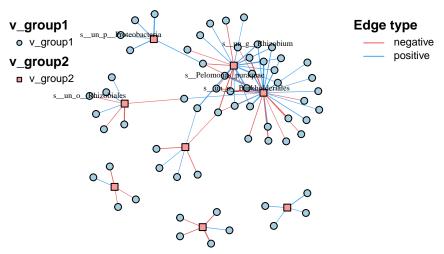


Figure 3.2: Simple co-occurrence network

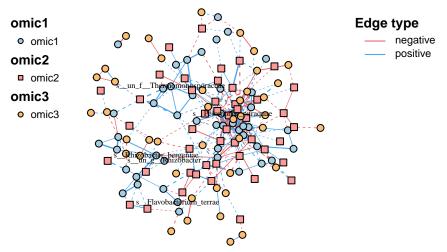
Bipartite network



Multi-tables When you have more than two tables for correlation network analysis, you can choose the multi_net_build() to calculate and build network. For subsequent multi-omics analysis, see Chapter 8.

```
data("multi_test")
#microbiome
dim(micro)
## [1] 18 50
#metabolome
dim(metab)
## [1] 18 50
#transcriptome
dim(transc)
## [1] 18 50
multi_net_build(micro,metab,transc,mode = "full",method = "spearman",filename = F)->multi1
plot(multi1)
```

Multi-omics network



Edgelist If you already get the pairwise relationship of data from other approaches (database), you can form it into a edgelist and use c_net_from_edgelist to build network. It is useful for following analysis.

```
load("../MetaNet/data/edgelist.rda")
dnet=c_net_from_edgelist(arc_count,direct = T)
plot(dnet)
```

Network

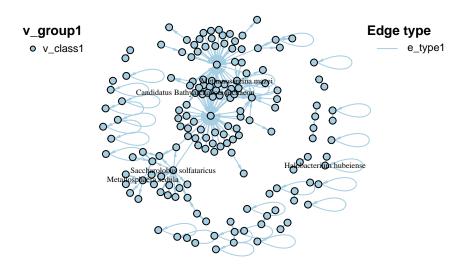


Figure 3.3: Simple directed network

3.4 RMT optimize

The correlation-based relevance network method is most commonly used largely due to its simple calculation procedure and noise tolerance. However, most studies involving relevance network analysis use arbitrary thresholds (usually, we use r>0.6, p<0.05), and thus the constructed networks are subjective rather than objective.

This problem has been solved by a random matrix theory (RMT)-based approach (Figure 3.4), which is able to automatically identify a threshold for cellular network construction from microarray data (Deng et al. [2012]).

use $\mathtt{RMT_threshold}()$, we can find the best $\mathtt{r_threshold}$ to make the network with smallest noise.

the bigger log_LE, less log_LW, less log_see, bigger p_ks_test indicate the better r_threshold for a meaningful network construction. You can change the threshold range to calculate more finely.

Random matrix theory

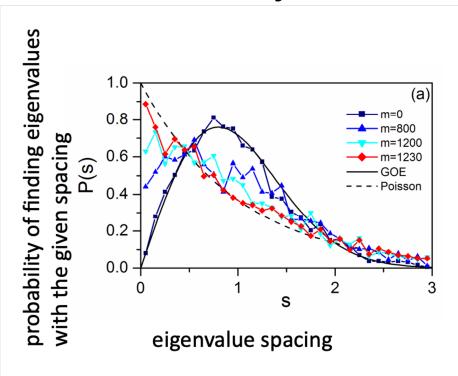


Figure 3.4: random matrix theory (RMT)-based approach

```
##
               ========Calculating6:
                                   threshold =0.6========
                      Calculating7:
                                   threshold =0.62===
                       Calculating8:
                                   threshold =0.64=
                       Calculating9:
                                   threshold =0.66=
                                   threshold =0.68=
                      Calculating10:
                                   threshold =0.7=
                       Calculating11:
                      Calculating12:
                                   threshold =0.72=
                     =Calculating13:
                                   threshold =0.74=====
                      Calculating14:
                                   threshold =0.76========
            =========Calculating15:
                                   threshold =0.78=========
                    ====Calculating16:
                                   threshold =0.8======
                                   threshold =0.82==========
       threshold =0.84==========
## ======Calculating19:
                                   threshold =0.86===========
## The Intermediate files saved in ./RMT_temp/ .
plot(rmt_res)
```

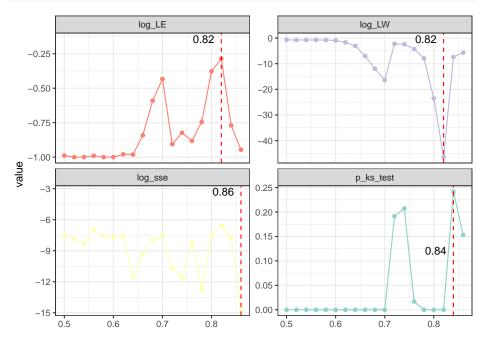


Figure 3.5: RMT_threshold result from 0.5 to 0.9

```
## [1] "recommend r_threshold: 0.835"
## [1] 0.835
```

You can set the gif=T in RMT_threshold and get a gif file to observe the distribution of eigenvalue spacing for different r-thresholds.

```
r if (knitr::is_html_output()) ' ![(\#fig:unnamed-chunk-13)the
```

distribution of eigenvalue spacing from 0.5 to 0.9](images/rmt_nnsd.gif)

Manipulation

4.1 Attributes

 $get_v get_e get_n$

4.2 Annotation

 $anno_vertex\ anno_edge$ summ2col

4.3 Filter (Sub-net)

 c_net_filter

4.4 Export

 c_net_save

Visualization

- 5.1 Basic plot
- 5.2 Layout
- 5.3 Other styles
- **5.3.1** ggplot
- 5.3.2 Gephi
- 5.3.3 Cytoscape

Topology

6.1 Complex network

The microbial co-occurrence network we study is a complex network, which generally has the following characteristics, scale-free, small-world attributes, modularity and hierarchy.

Table 6.1: Common characteristic

TernEmplagration

Scale-free It is a most notable characteristic in complex systems. It was free used to desibe the finding that most nodes in a network have few neighbors while few nodes have large amount of neighbors. In most cases, the connectivity distribution asymptotically follows a power law. It can be expressed in , where $P(k) \sim k^{-y} P(k)$ is the number of nodes with k degrees, k is connectivity/degrees and is a constant.

Small-mall-world It is a terminology in network analyses to depict the average worldistance between nodes in a network is short, usually logarithmically with the total number of nodes. It means the network nodes are always closely related with each other.

Table 6.1: Common characteristic

ModTharity dularity of a graph with respect to some division (or vertex types) measures how good the division is, or how separated are the different vertex types from each other. It defined as

$$Q = \frac{1}{2m} \sum_{i,j} (A_{ij} - \gamma \frac{k_i k_j}{2m}) \delta(c_i, c_j)$$

Vertex c_j per from each control $Q = \frac{1}{2m} \sum_{i,j} (A_{ij} - \gamma \frac{k_i k_j}{2m}) \delta(c_i, c_j)$ here mm is the number of edges, A_{ij} is the element of the A adjacency matrix in row i and column j, k_i is the degree of i, k_j is the degree of j, c_i is the type (or component) of i, c_j that of j, the sum goes over all i and jpairs of vertices, and $\delta(x,y)$ is 1 if x=y and 0 otherwise. The resolution parameter γ allows weighting the random null model, which might be useful when finding partitions with a high modularity. The original definition of modularity is retrieved when setting γ to 1.

Hieraticharchy It was used to depict the networks which could be arranged into a hierarchy of groups representing in a tree structure. Several studies demonstrated that metabolic networks are usually accompanied by a hierarchical modularity.

fit_power() is used to prove the scale-free. smallworldness() can calculate the smallworld index.

Topology indexes 6.2

Indexes Formula	Note	Description
Part I: net- work in- dexes for indi- vid- ual nodes Connectikity/ De- $\sum_{j\neq i} a_{ij}$ gree (cen- tral- ity)	is the connection strength between nodes i and j. when =1, ki is the unweighted degree	It is also called node degree. It is the most commonly used concept for describing the topological property of a node in a network.

Indexes	Formula	Note	Description
Between centrality	$\sum_{j,k} \frac{\sigma(i,j)}{\sigma(j,k)}$	(,,) is the number of hortest paths between nodes j and k that pass through node i. (,) is the total number of shortest paths between j and k.	It is used to describe the ratio of paths that pass through the ith node. High Betweenness node can serve as a broker similar to stress centrality.
Closenes cen- trality		The closeness centrality of a vertex is defined as the inverse of the sum of distances to all the other vertices in the graph. dij is the shortest distances from node i to j.	Closeness centrality measures how many steps is required to access every other vertex from a given vertex.
Eigenvector centrality	$\begin{array}{l} {\rm ct} & C_i = \\ \frac{1}{\lambda} \sum_{j \in M(i)} \end{array}$	M() is the set of nodes that, are connected to the ith node and is a constant eigenvalue.	It is used to describe the degree of a central node that it is connected to other central nodes.
Clusterin coeffi- cient	$\begin{array}{l} \text{agCo}_i = \\ \frac{2l_i}{k_i'(k_i'-1)} \end{array}$	li is the number of links between neighbors of node i and k i ' is the number of neighbors of node i.	It describe how well a node is connected with its neighbors. If it is fully connected to its neighbors, the clustering coefficient is 1. A value close to 0 means that there are hardly any connections with its neighbors. It was used to describe hierarchical properties of networks.
Eccentri		dij is the shortest if istance from node i to node j	The eccentricity of a vertex is its shortest path distance from the farthest other node in the graph.
Page.ran		i is the node whose pravalue needs to be calculated, and Bi is the set of all nodes pointing to node i. PRj is the pravalue of node j and lj is the number of links between neighbors of node j.	Calculates the Google PageRank for the specified vertices. PageRank, or webpage ranking, also known as webpage level, is an indicator to measure the importance of webpages.

Formula	Note	Description
$\begin{array}{l} \text{gfs}C = \\ \lambda_{AA^T} \\ AC = \\ \lambda_{A^TA} \end{array}$	vertices are defined as the principal eigenvector of AAT, the authority scores of the vertices are defined as the principal eigenvector of ATA. where A is the adjacency matrix of the	A node is an authority if it is linked to by hubs; it is a hub if it links to authorities.
	3 -1	
$\frac{\overline{k}}{\sum_{i=1}^{n} k_i}$	k i is degree of node i and n is the number of nodes.	Higher avgK means a more complex network.
$\begin{array}{l} L = \\ \sum_{i \neq j} d_{ij} \\ \overline{n(n-1)} \end{array}$	dij is the shortest path between node i and j.	A smaller GD means all the nodes in the network are closer.
$\frac{\sum_{i\neq j}^{j} 1/d_{ij}}{n(n-1)}$	all parameters shown above.	It is the opposite of GD. A higher E means that the nodes are closer.
	$\begin{array}{l} \overline{k}C = \\ \lambda_{AA^T} \\ AC = \\ \lambda_{A^TA} \end{array}$ $\begin{array}{l} \overline{k} = \\ \sum_{i=1}^n k_i \\ n \end{array}$ $\begin{array}{l} L = \\ \sum_{i \neq j} d_{ij} \\ n(n-1) \end{array}$ $E_a = $	$ \begin{array}{ll} \overline{k}C = & \text{The hub scores of the} \\ \lambda_{AA^T} & \text{vertices are defined as} \\ AC = & \text{the principal eigenvector} \\ \lambda_{A^TA} & \text{of AAT, the authority} \\ \text{scores of the vertices are} \\ \text{defined as the principal} \\ \text{eigenvector of ATA.} \\ \text{where A is the} \\ \text{adjacency matrix of the} \\ \text{graph.} \\ \\ \overline{k} = & \text{k i is degree of node i} \\ \text{and n is the number of nodes.} \\ \\ \overline{k} = & \text{dij is the shortest path} \\ \overline{k} = & dij is the$

$\operatorname{Indexes}$	Formula	Note	Description
Centrali of de- gree		max(k) is the maximal (k) is of all connectivity values and k i represents the connectivity of ith node. Finally this value is normalized by the theoretical maximum centralization score.	It is close to 1 for a network with star topology and in contrast close to 0 for a network where each node has the same connectivity.
Centrali of be- tween- ness	zet B n= $\sum_{i=1}^{n}(ext{ma}\ B_i)$	max(B) is the maximal xx(B)e-of all betweenness values and B i represents the betweenness of ith node. Finally this value is normalized by the theoretical maximum centralization score.	It is close to 0 for a network where each node has the same betweenness, and the bigger the more difference among all betweenness values.
Centrali of close- ness		max(C) is the maximal ax(Ci)e-of all closeness values and Ci represents the closeness of ith node. Finally this value is normalized by the theoretical maximum centralization score.	It is close to 0 for a network where each node has the same closeness, and the bigger the more difference among all closeness values.
Centrali of eigen- vector cen- trality		max(EC) is the maximal ax(EC) of all eigenvector centrality values and EC i represents the eigenvector centrality of ith node. Finally this value is normalized by the theoretical maximum centralization score.	It is close to 0 for a network where each node has the same eigenvector centrality, and the bigger the more difference among all eigenvector centrality values.
Density	$D = \frac{2l}{n(n-1)}$	l is the sum of total links.	The density of a graph is the ratio of the number of edges and the number of possible edges. It is closely related to the average connectivity.

Indexes Formula	Note	Description
Average $\overline{CCo} = \frac{\sum_{i=1}^{n} CCo_{i}}{\sum_{i=1}^{n} CCo_{i}}$ tering coefficient	oi is the clustering coefficient of node i.	It is used to measure the extent of module structure present in a network.
Transitiv IFy = $\frac{\sum_{i=1}^{n} 2i}{\sum_{i=1}^{n} (k'_i)(k_i)}$	li is the number of links i between neighbors of node i and k i ' is the number of neighbors of node i.	Sometimes it is also called the entire clustering coefficient. It has been shown to be a key structural property in social networks.
Natural $NC =$ con- nec- tivity	Where N is nodes $\prod_{i=1}^{N}$ in the network, represents the eigenvalue of the network adjacency matrix.	

Stability

It is very important to compare networks stability based on different groups. So MetaNet collects lots of methods to reflect the stability and complexity, these algorithms are coded using Parallel Computing which can be much faster.

7.1 Robustness tests

Robustness tests of networks were done with natural connectivity as it can reflect the stability of networks (WU Jun [2010]). Specifically, natural connectivity was calculated after removing the nodes (remove five nodes from a network at one time until 70% of nodes disappear), and the downtrend level of natural connectivity indicated the connectivity performance of the network after being damaged to a certain extent.

7.2 Community stability

Community stability can be characterized by various indexes, such as **robustness**, **vulnerability** and **cohesion**. Networks with higher robustness and lower vulnerability tend to be more stable (Yuan et al. [2021]). Also, community stability is commonly associated with negative interactions, and high percentage of negative correlations within communities is essential for maintaining a stable ecological system. ### Robustness The robustness was regarded as when 50% of nodes were randomly removed and results were based on 100 repetitions of the simulation.

7.2.1 Vulnerability

To evaluate the speed of disturbance spreading within a network, the global efficiency was regarded as the average of the efficiency over all pairs of nodes,

which was calculated by the number of edges in the shortest path between paired nodes. The vulnerability, which reflected the relative contribution of each node to the globe efficiency, was represented by the maximal vulnerability of nodes in the network.

7.2.2 Cohesion

Cohesion was calculated to quantify the connectivity of microbial communities in each group. Cohesion contains both positive and negative cohesion values, which indicate that associations between taxa attributed to positive and negative species interactions as well as similarities and differences in niches of microbial taxa11. Briefly, pairwise Pearson correlation matrix across taxa was calculated based on abundance-weighted matrix. After "taxa shuffle" null module-correcting with 200 simulations, average positive and negative correlations was calculated to get a connectedness matrix. Finally, positive and negative cohesions were calculated for each sample respectively by multiplying the abundance-weighted matrix and connectedness matrix. The absolute value of negative: positive cohesion is an important index for community stability. $cohesion = \sum_{i=1}^m abundance_i \times connectness_i$

multi-omics

8.1 Case study

In-depth multi-omic profiling was performed on each sample including plasma proteomics (targeted and untargeted), metabolomics (untargeted), lipidomics (semi-targeted), and gene expression (transcriptomics) from peripheral blood mononuclear cells (PBMCs).(Contrepois et al. [2020])

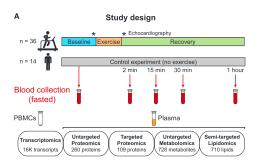


Figure 8.1: Overview of the study design including an acute bout of exercise

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