1.1 $Y = AC + \overline{A} \, \overline{B} C$

$$\begin{array}{rcl} Y & = & AC + \overline{A}\,\overline{B}C \\ Y & = & C(A + \overline{A}\,\overline{B}) \\ Y & = & C(A + \overline{A}\,\overline{B}) \end{array}$$

Truth Table:

| A | B | C | AC | $\overline{A}\overline{B}C$ | Y |
|---|---|---|----|-----------------------------|---|
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 0 | 1 |

K-Map:

| | | | AB | | |
|------------|---|----|----|----|----|
| | | 00 | 01 | 11 | 10 |
| $^{\circ}$ | 0 | 0 | 0 | 0 | 0 |
| | 1 | 1 | 0 | 1 | 1 |

1.2 $Y = \overline{A}\overline{B} + \overline{A}B\overline{C} + \overline{(A + \overline{C})}$

$$Y = \overline{A} \, \overline{B} + \overline{A} B \overline{C} + \overline{(A + \overline{C})}$$

$$Y = \overline{A} \, \overline{B} + \overline{A} B \overline{C} + \overline{A} C$$

$$Y = \overline{A} (\overline{B} + B \overline{C} + C)$$

$$Y = \overline{A} (\overline{B} + \overline{B} \overline{\overline{C}} + C)$$

$$Y = \overline{A} (\overline{B} + \overline{B} + C + C)$$

$$Y = \overline{A}((\overline{B} + C) + (\overline{\overline{B} + C}))$$

$$Y \quad = \quad \overline{A}$$

Truth Table:

| A | B | C | $\overline{A}\overline{B}$ | $\overline{A}B\overline{C}$ | $\overline{(A+\overline{C})}$ | Y |
|---|---|---|----------------------------|-----------------------------|-------------------------------|---|
| 0 | 0 | 0 | 1 | 0 | 0 | 1 |
| 0 | 0 | 1 | 1 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 |

K-Map:

| | AB | | | | | | |
|---|----|----|----|----|----|--|--|
| | | 00 | 01 | 11 | 10 | | |
| С | 0 | 1 | 1 | 0 | 0 | | |
| | 1 | 1 | 1 | 0 | 0 | | |

2 Problem 2

2.1 Part 1

| A | B | C | Y | Minterm |
|---|---|---|---|--|
| 0 | 0 | 0 | 1 | $\overline{A}\overline{B}\overline{C}$ |
| 0 | 0 | 1 | 0 | - |
| 0 | 1 | 0 | 0 | _ |
| 0 | 1 | 1 | 0 | _ |
| 1 | 0 | 0 | 0 | _ |
| 1 | 0 | 1 | 0 | _ |
| 1 | 1 | 0 | 0 | - |
| 1 | 1 | 1 | 1 | ABC |
| | | | | |

 $Y = \overline{A}\,\overline{B}\,\overline{C} + ABC$

2.2 Part 2

| A | B | C | Y | Minterm |
|---|---|---|---|--|
| 0 | 0 | 0 | 1 | $\overline{A}\overline{B}\overline{C}$ |
| 0 | 0 | 1 | 0 | - |
| 0 | 1 | 0 | 1 | $\overline{A} B\overline{C}$ |
| 0 | 1 | 1 | 0 | - |
| 1 | 0 | 0 | 1 | $A \overline{B} \overline{C}$ |
| 1 | 0 | 1 | 0 | - |
| 1 | 1 | 0 | 1 | $AB\overline{C}$ |
| 1 | 1 | 1 | 0 | - |

 $Y = \overline{A} \overline{B} \overline{C} + \overline{A} B \overline{C} + A B \overline{C}$

3.1 Part 1

Already minimal

3.1.1 Part 2

K-Map:

| | AB | | | | | | |
|------------------|---------------------------|----|----|----|----|--|--|
| | | 00 | 01 | 11 | 10 | | |
| C | 0 | 1 | 1 | 1 | 1 | | |
| | 1 | 0 | 0 | 0 | 0 | | |
| $\overline{Y} =$ | $\overline{\overline{C}}$ | | | | | | |

4 Problem 4

f is true except when $x_1, \overline{x_2}$ and x_3 are all true (term 5), i.e. it is the negation of $x_1\overline{x_2}x_3$:

$$f(x_1, x_2, x_3) = \overline{x_1 \overline{x_2} x_3}$$

$$f(x_1, x_2, x_3) = \overline{x_1} + x_2 + \overline{x_3}$$

K-Map:

| | | | x_1x_2 | 2 | |
|-------|---|----|----------|----|----|
| | | 00 | 01 | 11 | 10 |
| x_3 | 0 | 1 | 1 | 1 | 1 |
| | 1 | 1 | 1 | 1 | 0 |

 $f(x_1, x_2, x_3) = \overline{x_1} + x_2 + \overline{x_3}$

5 Problem 5

5.1 Part 1

Sum of Products:

| x_1 | x_2 | x_3 | $f(x_1, x_2, x_3)$ | Minterm |
|-------|-------|-------|--------------------|--------------------------------------|
| 0 | 0 | 0 | 0 | - |
| 0 | 0 | 1 | 1 | $\overline{x_1} \overline{x_2} x_3$ |
| 0 | 1 | 0 | 0 | - |
| 0 | 1 | 1 | 0 | - |
| 1 | 0 | 0 | 1 | $x_1\overline{x_2}\overline{x_3}$ |
| 1 | 0 | 1 | 1 | $x_1\overline{x_2}x_3$ |
| 1 | 1 | 0 | 1 | $x_1x_2\overline{x_3}$ |
| 1 | 1 | 1 | 0 | - |

$$Y = \overline{x_1} \, \overline{x_2} x_3 + x_1 \overline{x_2} \, \overline{x_3} + x_1 \overline{x_2} x_3 + x_1 x_2 \overline{x_3}$$

K-Map:

| | x_1x_2 | | | | |
|-------|----------|----|----|----|----|
| | | 00 | 01 | 11 | 10 |
| x_3 | 0 | 0 | 0 | 1 | 1 |
| | 1 | 1 | 0 | 0 | 1 |

$$Y = x_1\overline{x_2} + x_1\overline{x_3} + \overline{x_2}x_3$$

Minimize:

 $\begin{array}{rcl} Y & = & \overline{x_1}\,\overline{x_2}x_3 + x_1\overline{x_2}\,\overline{x_3} + x_1\overline{x_2}x_3 + x_1x_2\overline{x_3} \\ Y & = & \overline{x_1}\,\overline{x_2}x_3 + x_1\overline{x_2}(\overline{x_3} + x_3) + x_1x_2\overline{x_3} \\ Y & = & \overline{x_1}\,\overline{x_2}x_3 + x_1\overline{x_2} + x_1x_2\overline{x_3} \end{array}$

 $Y = \overline{x_1} \overline{x_2} x_3 + x_1 \overline{x_2} + x_1 x_2 \overline{x_3}$ $Y = x_1 \overline{x_2} + \overline{x_1} \overline{x_2} x_3 + x_1 x_2 \overline{x_3}$ $Y = x_1 \overline{x_2} + \overline{x_1} \overline{x_2} x_3 + x_1 x_2 \overline{x_3}$

Product of sums:

| x_1 | x_2 | x_3 | $f(x_1, x_2, x_3)$ | Maxterms |
|-------|-------|-------|--------------------|--|
| 0 | 0 | 0 | 0 | $x_1 + x_2 + x_3$ |
| 0 | 0 | 1 | 1 | - |
| 0 | 1 | 0 | 0 | $x_1 + \overline{x_2} + x_3$ |
| 0 | 1 | 1 | 0 | $x_1 + \overline{x_2} + \overline{x_3}$ |
| 1 | 0 | 0 | 1 | - |
| 1 | 0 | 1 | 1 | - |
| 1 | 1 | 0 | 1 | - |
| 1 | 1 | 1 | 0 | $\overline{x_1} + \overline{x_2} + \overline{x_3}$ |

$$Y = (x_1 + x_2 + x_3)(x_1 + \overline{x_2} + x_3)(x_1 + \overline{x_2} + \overline{x_3})(\overline{x_1} + \overline{x_2} + \overline{x_3})$$

5.2 Part 2

Sum of Products:

| 111 OI 1 | | | | |
|----------|-------|-------|--------------------|--|
| x_1 | x_2 | x_3 | $f(x_1, x_2, x_3)$ | Minterm |
| 0 | 0 | 0 | 1 | $\overline{x_1} \overline{x_2} \overline{x_3}$ |
| 0 | 0 | 1 | x | - |
| 0 | 1 | 0 | 1 | $\overline{x_1}x_2x_3$ |
| 0 | 1 | 1 | 1 | $\overline{x_1}x_2x_3$ |
| 1 | 0 | 0 | 1 | $x_1\overline{x_2}\overline{x_3}$ |
| 1 | 0 | 1 | X | - |
| 1 | 1 | 0 | 0 | - |
| 1 | 1 | 1 | 0 | - |

 $Y = \overline{x_1} \, \overline{x_2} \, \overline{x_3} + \overline{x_1} x_2 x_3 + \overline{x_1} x_2 x_3 + \overline{x_1} x_2 \overline{x_3}$

K-Map:

| | x_1x_2 | | | | | | |
|-------|----------|----|----|----|----|--|--|
| | | 00 | 01 | 11 | 10 | | |
| x_3 | 0 | 1 | 1 | 0 | 1 | | |
| | 1 | X | 1 | 0 | X | | |

 $Y = \overline{x_1} + \overline{x_2}$

Truth Table

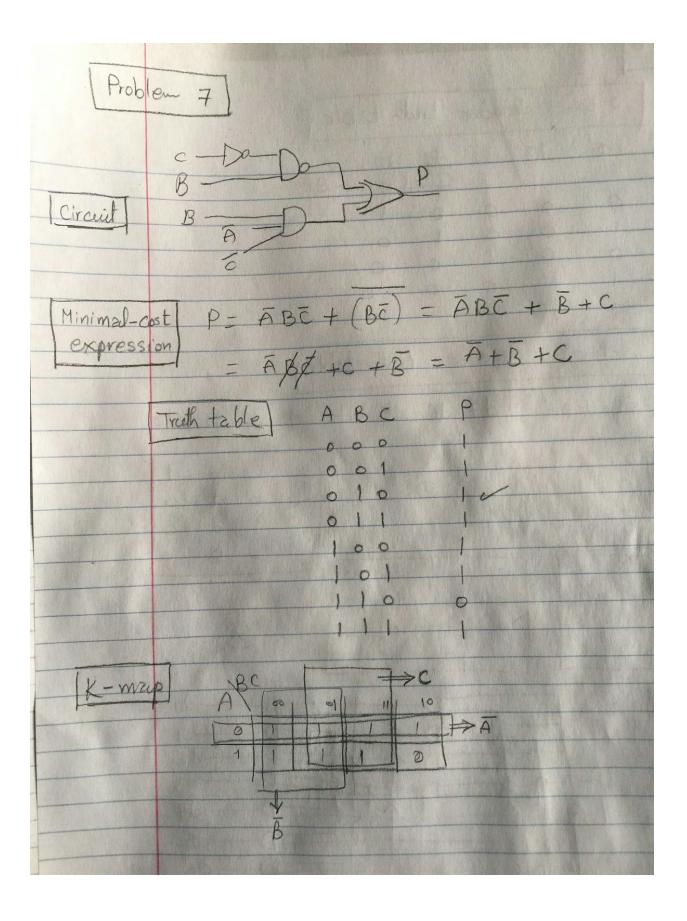
| u | u <u>th Table: </u> | | | | | | | |
|---|--|---|---|---|---|--|--|--|
| | A | В | С | D | Y | | | |
| | 0 | 0 | 0 | 0 | X | | | |
| Ī | 0 | 0 | 0 | 1 | x | | | |
| | 0 | 0 | 1 | 0 | x | | | |
| | 0 | 0 | 1 | 1 | 0 | | | |
| Ī | 0 | 1 | 0 | 0 | 0 | | | |
| Ī | 0 | 1 | 0 | 1 | x | | | |
| Ī | 0 | 1 | 1 | 0 | 0 | | | |
| Ī | 0 | 1 | 1 | 1 | x | | | |
| Ī | 1 | 0 | 0 | 0 | 1 | | | |
| Ī | 1 | 0 | 0 | 1 | 0 | | | |
| Ī | 1 | 0 | 1 | 0 | x | | | |
| Ī | 1 | 0 | 1 | 1 | 1 | | | |
| Ī | 1 | 1 | 0 | 0 | 1 | | | |
| | 1 | 1 | 0 | 1 | 1 | | | |
| Ī | 1 | 1 | 1 | 0 | X | | | |
| | 1 | 1 | 1 | 1 | 1 | | | |

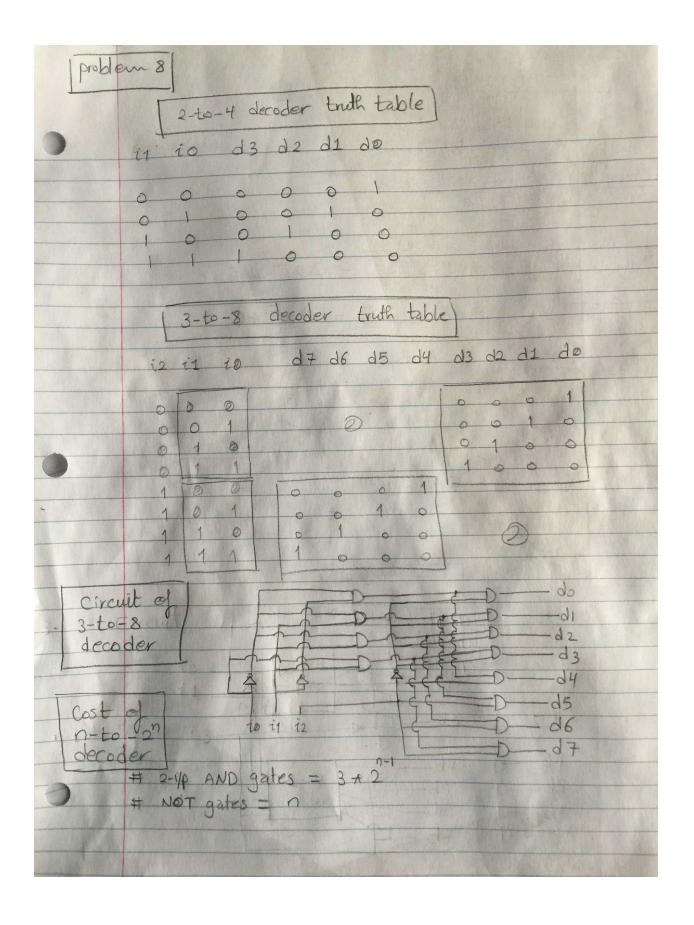
K-Map:

| ii iidp. | | | | | | | | |
|------------------|----|----|----|----|----|--|--|--|
| | AB | | | | | | | |
| | | 00 | 01 | 11 | 10 | | | |
| | 00 | X | 0 | 1 | 1 | | | |
| $^{\mathrm{CD}}$ | 01 | X | X | 1 | 0 | | | |
| | 11 | 0 | X | 1 | 1 | | | |
| | 10 | X | 0 | X | X | | | |

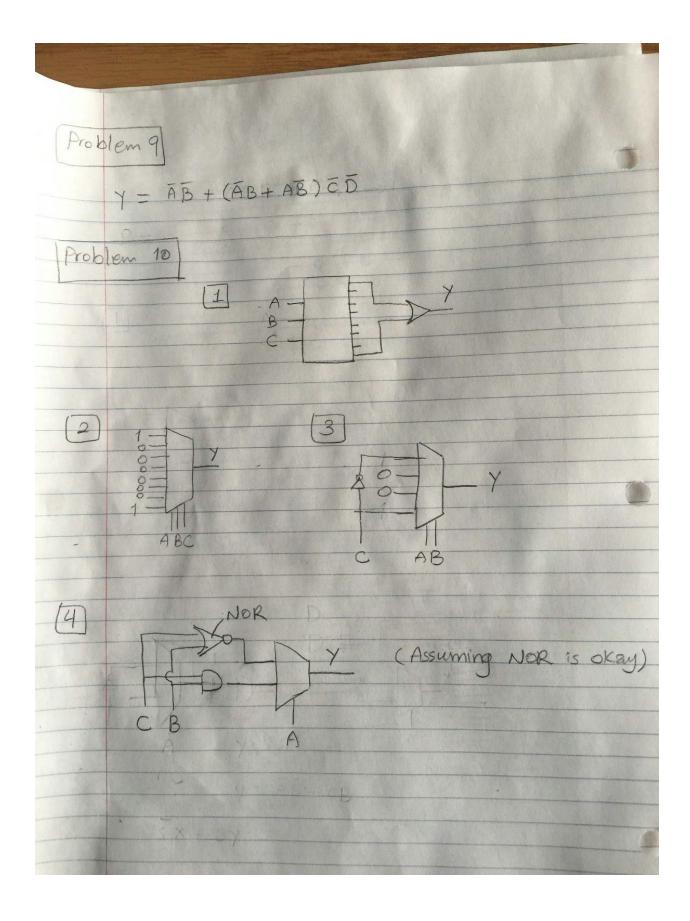
Minimal:

$$Y = AB + AC + BD$$

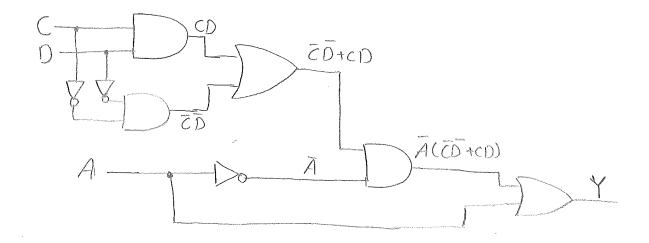


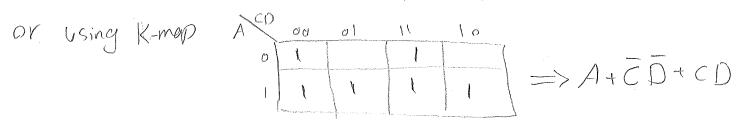


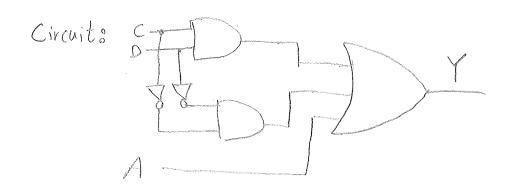
Problems 9 and 10



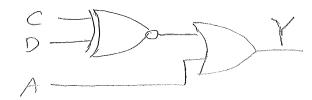
$$Y = A + \overline{A}(\overline{CD} + CD)$$

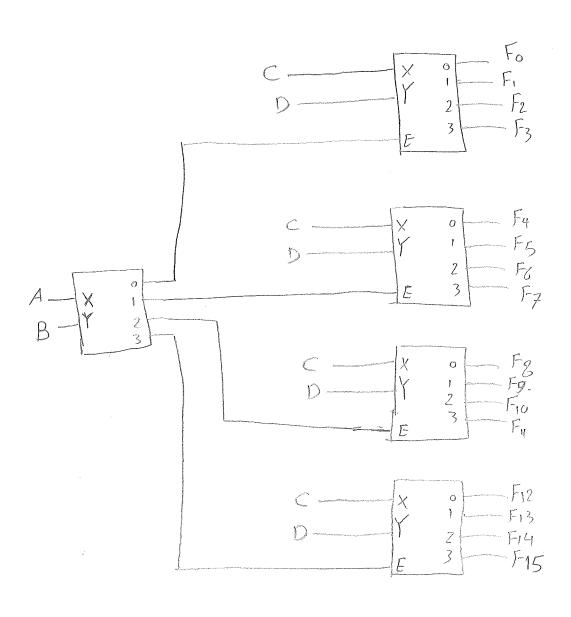


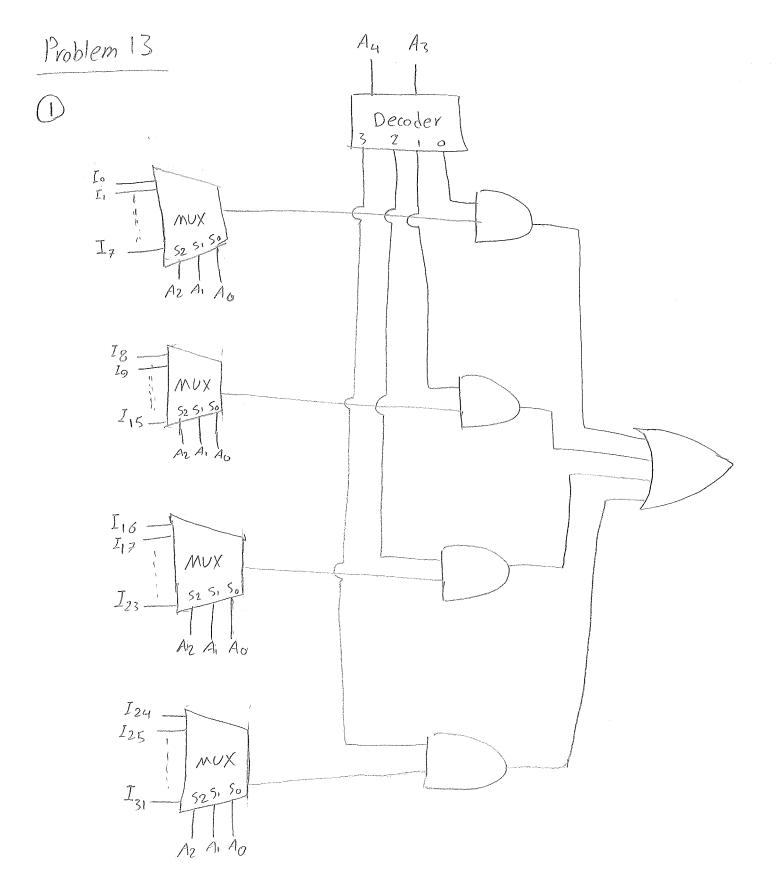


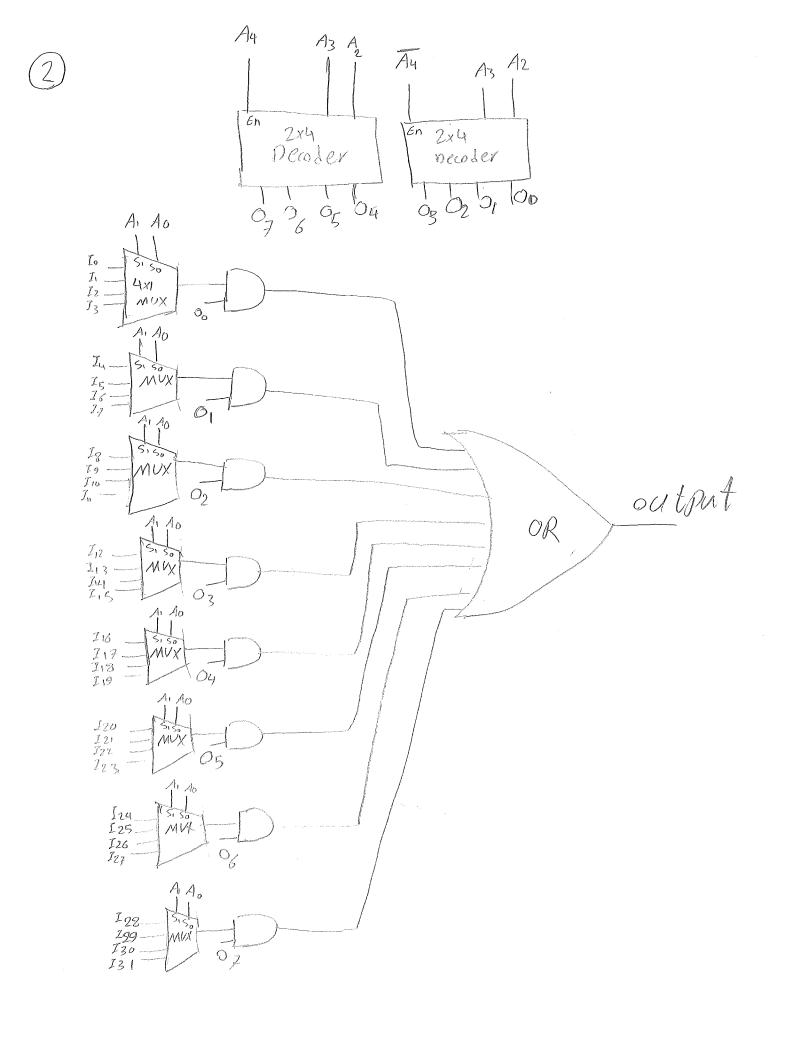


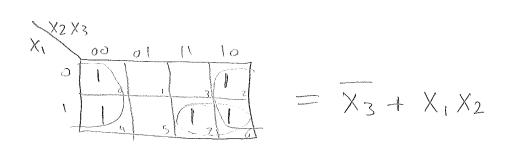
more simplification:
$$\overline{CD} + CD = \overline{CDD} \equiv \times NOR$$

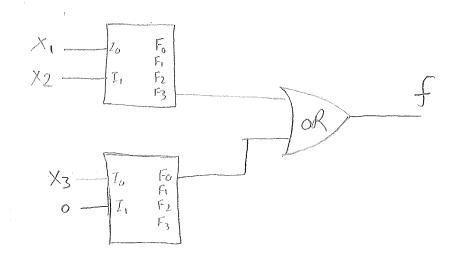




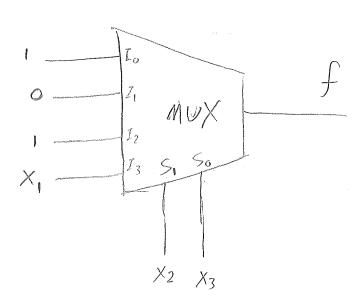








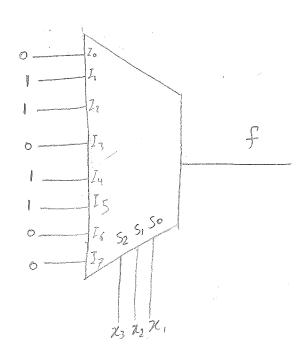
2



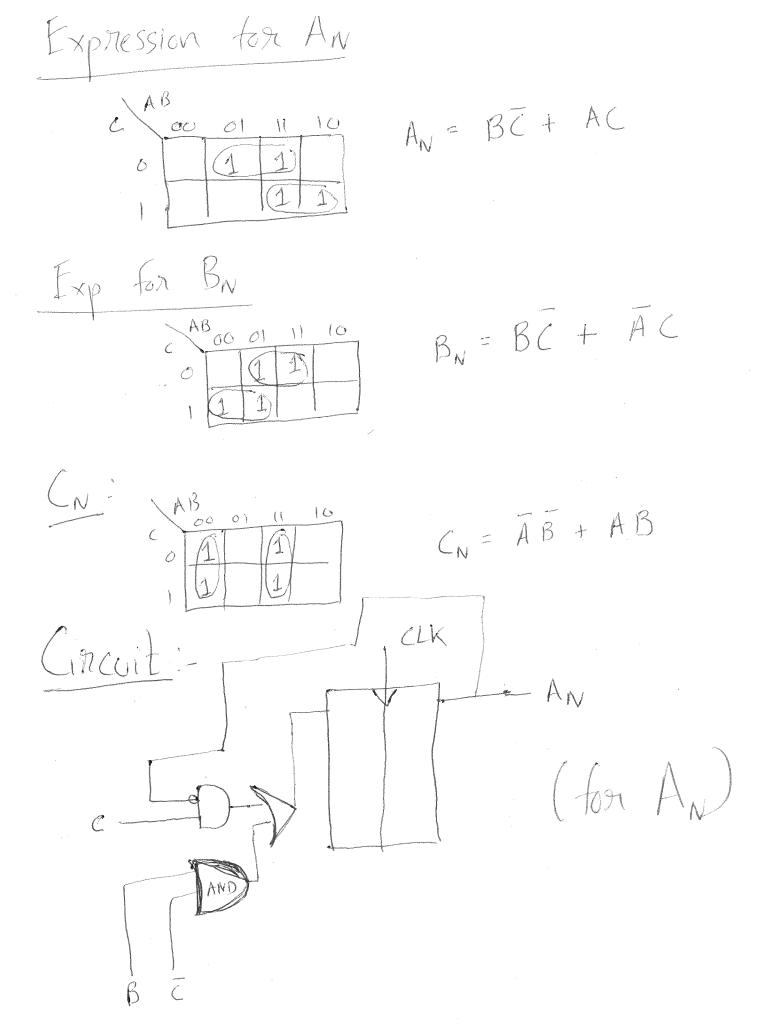
00 output

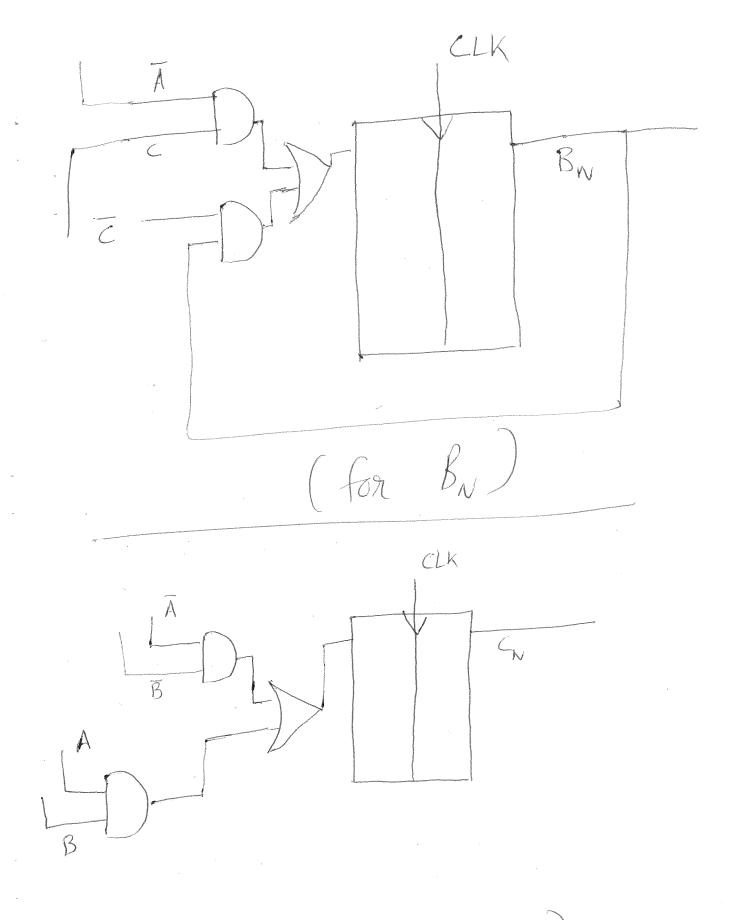
Problem 16: $f = \chi_{1} \chi_{2} + \chi_{1} \chi_{2} \chi_{3} + \chi_{1} \chi_{2} \chi_{3}$ $f = \chi_{1} \chi_{2} \chi_{3} + \chi_{1} \chi_{$

(2)



Problem 17 Need to maintain 3 bits. Say ABC. 8 states. Fo., ... I Fat where Fo is 000 F₈ is 100 and rest are in 9 nay sequence. Exposition ABC · to maintain state 13





(for (N)

Problem 18: Let's first draw the FSM: 1 $5_{6} = 0.0$ $5_{1} = 0.1$ 51/0 $S_2 = 10$ D = input Y = onthut 52/1 B_{N} AN B 0

