

$$10 \quad 20(a) \quad y[n-1] + 2y[n] = x[n]$$

$$z^{-1} + 2 = 0 \quad z = -\frac{1}{2}$$

$$\therefore y[n] = A(-\frac{1}{2})^n$$

$$\text{代入 } y[-1] = A(-\frac{1}{2})^{-1} = -2A = 2$$

$$\wedge A = 1 \quad \therefore y[n] = -(-\frac{1}{2})^n$$

$$(b) \quad x[n] = (\frac{1}{4})^n u[n] \xleftrightarrow{z} \frac{1}{1 - \frac{1}{4}z^{-1}}$$

$$z\text{变换} \quad z^{-1}Y(z) + Y(z) + 2Y(z) = X(z)$$

$$(z^{-1} + 2)Y(z) = X(z)$$

$$Y(z) = \frac{\frac{1}{1 - \frac{1}{4}z^{-1}}}{z^{-1} + 2} = \frac{2}{z^{-1} + 2}$$

$$= \frac{1}{2} \frac{1}{(1 - \frac{1}{4}z^{-1})(1 + \frac{1}{2}z^{-1})}$$

$$= \frac{1}{2} \left( \frac{\frac{1}{3}}{1 - \frac{1}{4}z^{-1}} + \frac{\frac{2}{3}}{1 + \frac{1}{2}z^{-1}} \right)$$

$$y_{zs} = \frac{1}{6} (\frac{1}{4})^n u[n] + \frac{1}{3} (-\frac{1}{2})^n u[n]$$

$$(c) \quad y[n] = y_{z1}[n] + y_{z2}[n]$$

$$= \frac{1}{6} (\frac{1}{4})^n u[n] - \frac{2}{3} (-\frac{1}{2})^n u[n]$$

$$10.27 \quad X(z) = \frac{3z^{-10} + z^{-7} - 5z^{-2} + 4z^{-1} + 1}{z^{-10} - 5z^{-7} + z^{-3}}$$

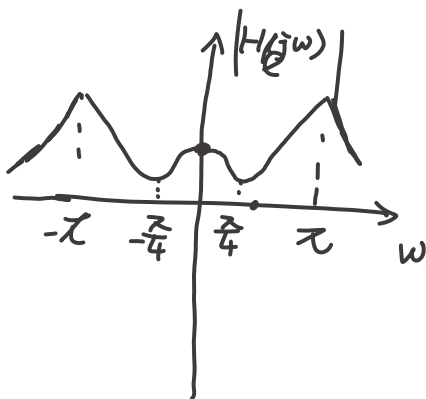
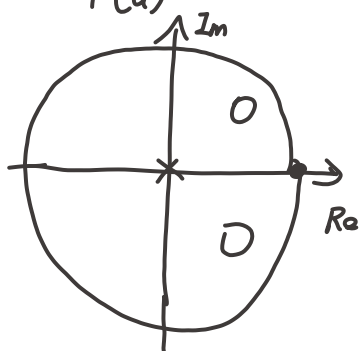
长除法:

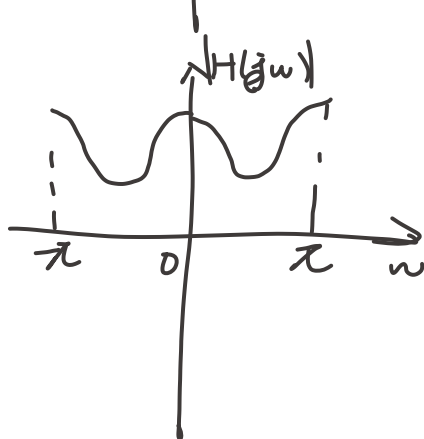
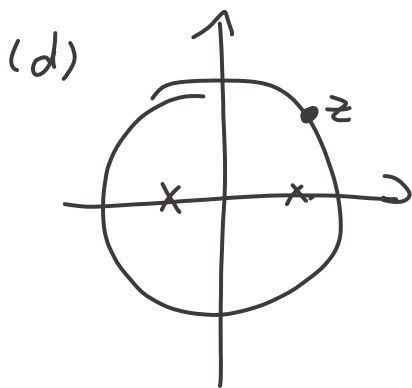
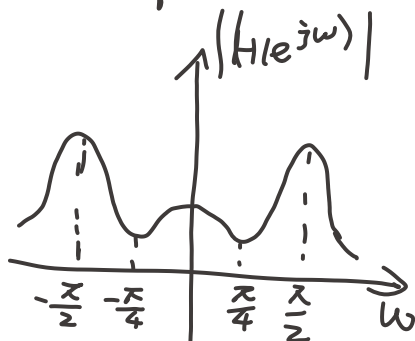
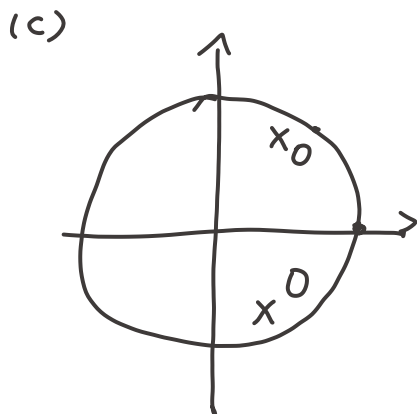
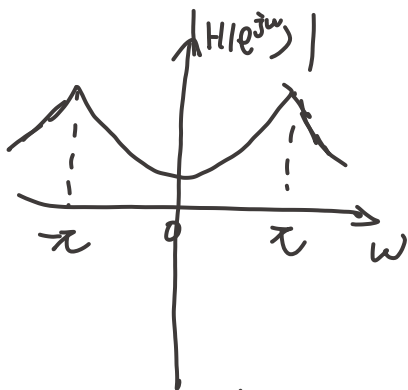
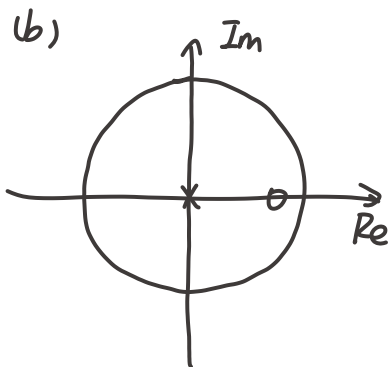
$$\begin{array}{r} z^3 + 4z^2 + 5z + 0 + 5z^{-1} + 20z^{-2} + \dots \\ z^{-3} - 5z^{-7} + z^{-10} \sqrt{\phantom{z^3 + 4z^2 + 5z + 0 + 5z^{-1} + 20z^{-2} + \dots}} \\ \underline{1 + 4z^{-1} - 5z^{-2} + z^{-7} + 3z^{-10}} \phantom{\dots} \\ 1 - 5z^{-4} + z^{-7} \\ \underline{\phantom{1 - 5z^{-4} + z^{-7}}} \\ 4z^{-1} - 5z^{-2} + 5z^{-4} + 3z^{-10} \\ \underline{4z^{-1} - 20z^{-5} + 4z^{-8}} \\ -5z^{-2} + 5z^{-4} + 20z^{-5} - 4z^{-8} + 3z^{-10} \\ \underline{-5z^{-2} + 25z^{-6} - 5z^{-9}} \\ 5z^{-4} + 20z^{-5} - 25z^{-6} - 4z^{-8} - 5z^{-9} + 3z^{-10} \\ \underline{5z^{-4} - 5z^{-8} + 5z^{-11}} \end{array}$$

$$\therefore X(z) = z^3 + 4z^2 - 5z + 0 + 5z^{-1} + 20z^{-2} + \dots$$

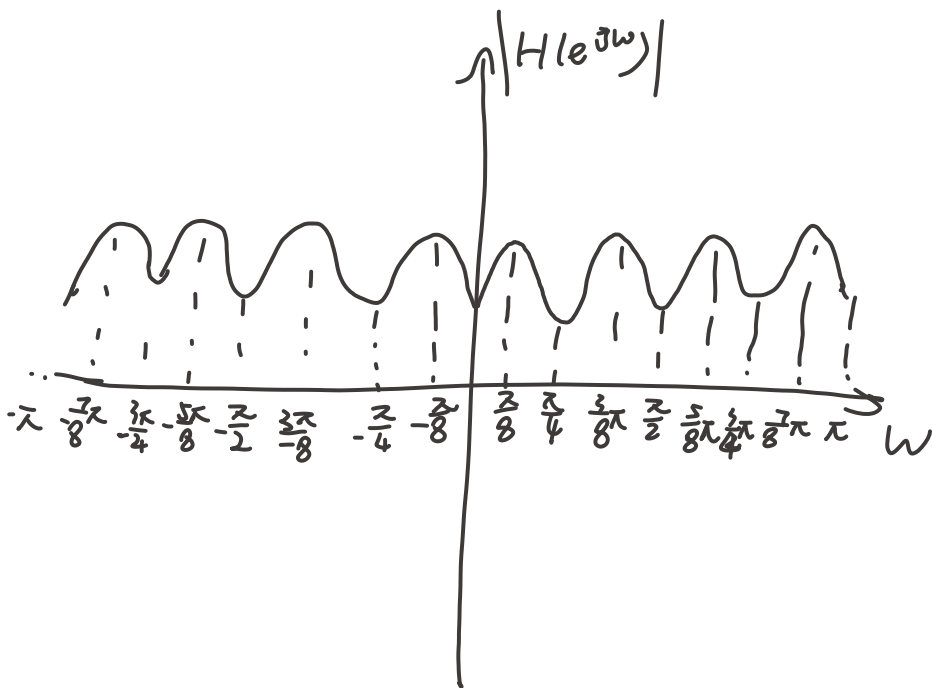
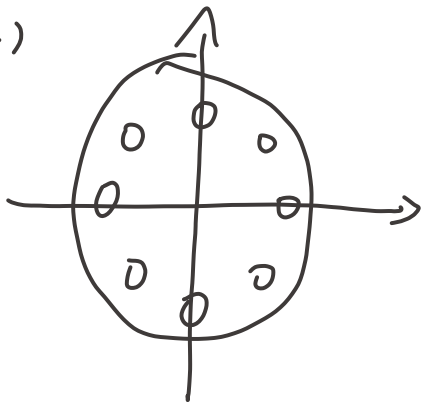
$$X[n] = \delta[n+3] + 4\delta[n+2] - 5\delta[n+1] + 5\delta[n-1] + 20\delta[n-2] + \dots$$

10.29 (a)





(c)



10 31  $x[n]$  实序列 由共轭对称

$$z_1 = \frac{1}{2} e^{j\pi/3} \quad z_2 = \frac{1}{2} e^{j(\pi/3)}$$

零点 2个 共轭对称

由右边序列.

$$\therefore \text{ROC: } |z| > \frac{1}{2}$$

$$\text{设 } H(z) = \frac{A z^2}{(z - \frac{1}{2} e^{j\pi/3})(z - \frac{1}{2} e^{-j\pi/3})}$$

$$\text{令 } z=1$$

$$H(1) = \frac{A}{(1 - \frac{1}{2} e^{j\pi/3})(1 - \frac{1}{2} e^{-j\pi/3})} = \frac{8}{3}$$

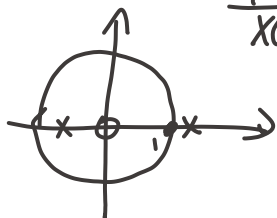
$$\therefore \frac{A}{1 - \frac{1}{4} - \frac{1}{2}(\frac{1}{2})} \quad A = \frac{10}{3}$$

10 34 (a)  $y[n] - y[n-1] - y[n-2] = x[n-1]$

$$Y(z) - z^{-1}Y(z) - z^{-2}Y(z) = z^{-1}X(z)$$

$$Y(z) (1 - z^{-1} - z^{-2}) = z^{-1}X(z)$$

$$\frac{Y(z)}{X(z)} = H(z) = \frac{z^{-1}}{1 - z^{-1} - z^{-2}} = \frac{z}{z^2 - z - 1}$$



$$\text{ROC: } |z| > \frac{1+\sqrt{5}}{2}$$

$$(b) \quad H(z) = \frac{z}{(z - \frac{1+\sqrt{5}}{2})(z - \frac{1-\sqrt{5}}{2})}$$

$$\frac{H(z)}{z} = \frac{1}{(z - \frac{1+\sqrt{5}}{2})(z - \frac{1-\sqrt{5}}{2})} = \frac{1}{\sqrt{5}} \left( \frac{-1}{z - \frac{1-\sqrt{5}}{2}} + \frac{1}{z - \frac{1+\sqrt{5}}{2}} \right)$$

$$h(z) = \frac{1}{\sqrt{5}} \left( \frac{-z}{z - \frac{1-\sqrt{5}}{2}} + \frac{z}{z - \frac{1+\sqrt{5}}{2}} \right)$$

$$\cdot h[n] = \frac{1}{\sqrt{5}} \left( \left(\frac{1-\sqrt{5}}{2}\right)^n u[n] \right) + \frac{1}{\sqrt{5}} \left( \left(\frac{1+\sqrt{5}}{2}\right)^n u[n] \right)$$

(c) ROC 未包含  $|z|=1$  是不稳定的

要求稳定 则可选一个双边信号

ROC:  $\frac{1+\sqrt{5}}{2} < |z| < \frac{1+\sqrt{5}}{2}$  其中  $\frac{1}{\sqrt{5}} \left(\frac{1+\sqrt{5}}{2}\right)^n u[-n-1]$  为左信号

$$\cdot h[n] = \frac{1}{\sqrt{5}} \left( \left(\frac{1-\sqrt{5}}{2}\right)^n u[n] \right) - \frac{1}{\sqrt{5}} \left( \left(\frac{1+\sqrt{5}}{2}\right)^n u[-n-1] \right)$$

10.46  $z$  变换  $X(z) = S(z) - e^{8\alpha} z^{-8} S(z)$

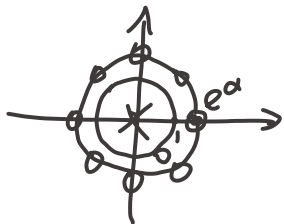
(a)

$$X(z) = S(z)(1 - e^{8\alpha} z^{-8})$$

$$H_1(z) = \frac{X(z)}{S(z)} = 1 - e^{8\alpha} z^{-8} = 1 - \frac{e^{8\alpha}}{z^8}$$

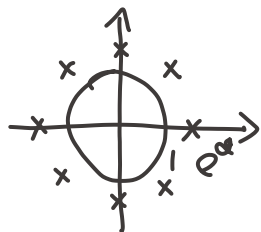
$$= \frac{z^8 - e^{8\alpha}}{z^8}$$

零点 8 个



ROC:  $|z| > 0$  为  $z = e^{\alpha} e^{j\frac{\pi}{4}k}$  ( $k=0,1,2,\dots$ )

$$(b) H_2(z) = \frac{Y(z)}{X(z)} = \frac{S(z)}{X(z)} = H_1(z)^{-1} = \frac{z^8}{z^8 - e^{8\alpha}}$$



极点:  $z = e^{\alpha} e^{j\frac{\pi}{4}k} (k=0,1,2,\dots)$

零点:  $z=0$

① 当  $|z| > e^{\alpha}$  因果但不稳定

② 当  $0 < |z| < e^{\alpha}$ , 稳定而非因果

(c) ① 因果情况  $H_2(z) = \frac{1}{1 - e^{8\alpha} z^{-8}}$

$$= \sum_{n=0}^{+\infty} e^{8\alpha n} z^{-8n}$$

$$h_2[n] = e^{8\alpha \frac{n}{8}} = e^{\alpha n} \quad n=0, 8, 16, \dots$$

$$h_2[n] = 0 \quad \text{其他}$$

② 非因果  $H_2(z) = \sum_{k=1}^{+\infty} (e^{-8\alpha} z^8)^k = \sum_{k=1}^{+\infty} e^{-8\alpha(k-1)} z^{8(k-1)}$

$$\therefore h_2[n] = e^{-\alpha|n|} \quad (n=0, -8, -16, \dots)$$

$$h_2[n] = 0 \quad (\text{其他})$$

1048 (a)  $\rightarrow$  (b): 相当于旋转  $180^\circ$  放缩极点  $\frac{2}{3}$ .

$$h_2[n] = A \left( \frac{2}{3} e^{j\pi} \right)^n u[n] \quad h_1[n]$$

$$= A \left( -\frac{2}{3} \right)^n u[n] \quad h_1[n]$$

$$\therefore \sum_0^{+\infty} |g[k]| = 3 \quad \therefore A \frac{1}{1 + \frac{2}{3}} = 3$$

$$\therefore A = 5$$

