

EX. 6, POINT A

$$\int_0^1 \int_0^x c \frac{y}{x} dy dx = 1$$

$$\int_0^1 \frac{c}{x} \int_0^x y dy dx$$

$$\int_0^1 \frac{c}{x} \left[\frac{y^2}{2} \right]_0^x dx$$

$$\int_0^1 \frac{c}{x} \cdot \frac{x^2}{2} dx$$

$$c \int_0^1 \frac{x}{2} dx$$

$$\frac{c}{2} \int_0^1 x dx$$

$$\frac{c}{2} \left[\frac{x^2}{2} \right]_0^1$$

$$\frac{c}{2} \cdot \frac{1}{2} = 1$$

$$\frac{c}{4} = 1$$

$$c = 4$$

EX. 6 POINT B

$$4 \frac{y}{x} = \int_0^x 4 \frac{y}{x} dy \cdot \int_y^1 4 \frac{y}{x} dx$$

$$= \frac{4}{x} \left[\frac{y^2}{2} \right]_0^x \cdot 4y [\ln(x)]_y^1$$

$$= \frac{4x^2}{x} \cdot \frac{x^2}{2} \cdot 4y \cdot (-\ln(y))$$

$$= 2x \cdot (-4y \ln(y))$$

$$\uparrow$$

 $f_x(x)$

$$\uparrow$$

 $f_y(y)$