more matplotlib, numpy matrices

more matplotlib

· plotting issues:

```
import matplotlib.pyplot as plt
plt.plot() # should pop up a figure window with axes
```

- figures not popping up in ipython?
 - turn on interactive mode by calling plt.ion()
 - permanently enable interactive mode in matplotlib settings file:
 - linux: ~/.config/matplotlib/matplotlibrc
 - mac + windows: ~/.matplotlib/matplotlibrc
 - uncomment #interactive: False line and set to True instead
- o figures in jupyter not automatically displaying inline?
 - type %matplotlib inline in a cell, all cells that follow will do inline plots
 - make this setting permanent in ~/.ipython/ipython_config.py file
 - uncomment #c.InteractiveShellApp.matplotlib = None line and set to 'inline'
 - for interactive plotting in jupyter, type %matplotlib notebook
 - make this setting permanent with c.InteractiveShellApp.matplotlib =
 'notebook' in ipython_config.py file
 - NOTE: this only works in more recent versions of matplotlib/jupyter?
 - quite a bit slower than interactive plots in ipython
- o missing toolbar?
 - Set toolbar : toolbar2 in matplotlibrc file
- the button for "edit axes/curve/image params" in figure window might be missing, not sure why
- MATLAB style vs. OOP style:
 - last week we learned the MATLAB "procedural" style of plotting:

```
import matplotlib.pyplot as plt
t = np.linspace(0, 4*np.pi, 100) # 100 evenly spaced timepoints, 2 cycles
s = np.sin(t) # calculate sine as a function of t
c = np.cos(t) # calculate cosine as a function of t
plt.plot(t, s) # plot points in t on x-axis vs. points in s on y-axis
plt.plot(t, c) # plot cosine as well
```

- MPL also has an alternative, more Pythonic, object-oriented (OOP) style, with very similar commands
- o first, you explicitly create a figure and an axes
- f, ax = plt.subplots() by default creates a new figure with one set of x-y axes, and returns objects representing them
 - notice the s in plt.subplots(), plt.subplot() is a slightly different MATLAB-style procedural command which you shouldn't need to use
- o now, we can do most of our plot commands as methods of this particular axes ax:
 - ax.plot(t, s)
 - common formatting commands in OOP style:
 - ax.set_xlim(), ax.set_ylim(), ax.set_xlabel(), ax.set_ylabel(), ax.set_title(), ax.legend()
 - compare with MATLAB style:
 - plt.xlim(), plt.ylim(), plt.xlabel(), plt.ylabel, plt.title(), plt.legend()
 - OOP style is slightly more wordy, but much more explicit, gives better control over multiple figures
 - one more useful figure property worth formatting is spines, only easily accessible through the OOP interface:
 - ax.spines['top'].set_visible(False)
 - ax.spines['right'].set_visible(False)
- with multiple figures and axes open, we can refer to them directly by name, no longer have to worry about which is the "current" figure:
- o f2, ax2 = plt.subplots()
- o ax2.hist(s) plot a histogram of sin(t) this time
- to clear a particular axes: ax.clear()

• subplots: create multiple axes in a single figure

```
o f, axs = plt.subplots(nrows=2, ncols=2)
```

- o axs is now a 2D array, choose your axes by indexing into axs with row and col indices:
 - axs[0, 1].plot(t, s) # plot s vs. t in axes in 1st row 2nd column
 - axs[1, 0].plot(t, c, color='r') # plot c vs. t in red in axes in 2nd row 1st column
- optional kwargs sharex, sharey

```
plt.close('all')
f1, ax1 = plt.subplots(2, 1, sharex=True, sharey=False) # ax1 is 1D array
ax1[0].plot(t, s) # plot s vs. t
ax1[1].plot(t, c, color='r') # plot c vs. t in red, shared x axis with sin plot
f2, ax2 = plt.subplots(2, 1, sharex=True, sharey=False) # ax2 is 1D array
ax2[0].hist(s) # plot hist of s
ax2[1].hist(c, color='r') # plot hist of c in red, shared x axis with sin hist
```

change the name of a figure, i.e. its window title bar and its default filename in the save dialog box:

```
f1.canvas.set_window_title( 'time series')
f2.canvas.set_window_title( 'histograms')
```

- · some other kinds of plots:
 - o scatterplots:
 - ax.scatter(x, y) very similar to ax.plot()
 - allows each point to be formatted differently (colour, marker, size)
 - defaults to not drawing a line between points
 - o errorbar plot
 - ax.errorbar(x, y, yerr=5, xerr=2) again similar to a.plot(), but with errorbars
 - bar charts
 - ax.bar(left, height) vertical bars, left and height are sequences
 - ax.bar(bottom, width) horizontal bars

matrices

- so far, we've (mostly) only dealt with 1D arrays, a.k.a. vectors
- numpy allows for N dimensional arrays, but most common are 2D arrays, a.k.a. matrices
- matrix is like an image: each entry has a (pixel) value stored at a row and column index
 - o can also think of it as a nested list, i.e. a list of lists
- plotting matrices as images is a great way to visualize them
- · initializing a 2D array is very similar to 1D arrays
 - o explicitly, using a list of lists, or a tuple of tuples, convert to array:

```
o a = np.array([[1, 2, 3], [4, 5, 6]]) Or a = np.array(((1, 2, 3), (4, 5, 6)))
```

- using np.arange(), and then reshaping:
- \circ a = np.arange(16).reshape((8, 2))
 - creates a 1D array, but then reshapes it to 2D
 - 2D array shape tuples are always (nrows, ncolumns)
 - check the shape of an array: a. shape
 - nrows * ncols of the reshaped array have to equal the number of elements in the 1D array
 - get the total number of elements in an array, whether 1D or 2D or ND: a.size
 - what happens if you do a.reshape((8, 3))?
 - what happens if you do a.reshape((4, 4))?
 - can also change the shape of an existing array by assigning to a shape = 8, 2

```
o a = np.zeros((8, 2))
o a = np.ones((8, 2))
o a = np.random.random((8, 2))
o a = np.tile([1, 2], 8)
```

```
    a.fill(7) fills the array with the number 7, but maintains its shape
    np.eye(5) - create 5x5 identity matrix
```

- to get number of rows: a.shape[0]
- to get number of columns: a.shape[1]
 - o for 1D arrays, len() gave number of elements in the array
 - o for 2D arrays, len() is a shortcut for a.shape[0], i.e. number of rows in a
- to convert 2D array to a 1D array, flatten it using a.ravel()
 - a.ravel() gives the same as np.arange(16)
 - flattening and asking for the length of the result: len(a.ravel()) gives same as a.size
- visualizing matrices:

```
f, ax = plt.subplots(figsize=(3, 3)) # set figure size in inches
im = ax.imshow(a) # returns an "image" object
f.canvas.set_window_title('imshow')
f.colorbar(im) # add a colorbar legend for the image
f.set_tight_layout(True) # make figure automatically resize contents
# resize the figure with the mouse
ax.set_xticks([]) # disable x ticks
ax.set_yticks([]) # disable y ticks
```

- use different colormaps to change how values in an array map to colours in displayed image:
 - default is called "viridis"
 - another popular one is "jet"
 - all colormaps listed using plt.colormaps()
 - im = ax.imshow(a, cmaps='jet') set during imshow call
 - im.set_cmap('viridis') modify existing image object
- scipy.ndimage and skimage are great for all kinds of image manipulation
 - loading different image types as arrays
 - o change contrast of an image
 - o manipulate colours
 - o thresholding, masking an image
 - image denoising/smoothing
 - o image segmentation
 - see recent local Python talk by Joe Donovan for lots of examples:
 - https://github.com/superpythontalks/image_analysis/blob/master/image%20processing.ipynb
- · 2D indexing and slicing

```
get element in 1st row, 1st column: a[0, 0]
get element in 3rd row, 2nd column: a[2, 1]
get element in last row, last column: a[-1, -1]
get element in 3rd row, 3rd column: a[2, 2] - IndexError!
get the first row, across all the columns: a[0, :], or just a[0] for short
get the first column, across all the rows: a[:, 0]
get first 3 rows: a[:3]
get every other row: a[::2]
flip matrix vertically by reversing order of rows: a[::-1]
flip matrix horizontally by reversing order of columns: a[:, ::-1]
rotate matrix in steps of 90 deg:

np.rot90(a) - counterclockwise
np.rot90(a, -1) - clockwise
```

- arithmetic operations on 2D arrays
 - matrix & scalar, same as for 1D arrays, works elementwise

- a + 2, a 2, a * 2, etc. does what you'd expect
- matrix & matrix also works elementwise, but both have to be the same shape:
 - \blacksquare b = np.random.random(16).reshape((8, 2))
 - a + b, a b, a * b, a / b etc.
 - what happens if you try b / a? divide by zero warning, results in np.inf at [0, 0]
- matrix a & vector x, bit more complex:
 - still elementwise, but the last dimension of a has to have same length as x
 - $\mathbf{x} = \text{np.arange(8)}$
 - a * x doesn't work, a.T * x does
 - called array "broadcasting"
- o can use many of the same methods as on 1D arrays:
 - a.max(), a.min(), a.sum(), a.mean(), a.std(), etc.
 - by default, these work on all elements in a 2D array, and return a single value
 - can be made to work across rows only, or columns only, by specifying the axis kwarg
 - a.max(axis=0) finds the max across the 1st dimension, i.e. across all rows, and returns one result per column
 - a.max(axis=1) finds the max across the 2nd dimension, i.e. across all colmuns, and returns one result per row
- · matrix operations:
 - o a.transpose() or its shortcut property a.T swaps rows with columns
 - o a.diagonal() returns the diagonal
 - o a.trace() returns sum along the diagonal
 - inner product, results in new matrix, whose entry at (i, j) is sum of elementwise product of row i of a and column j of b
 - np.dot(a, b) raises error, ncols of a must equal nrows of b
 - np.dot(a, b.T) works, and so does np.dot(a.T, b), but give different results
 - new matrix multiplication operator in Python 3.5 @ does the same as np.dot()
 - o outer product: take two vectors x and y, resulting matrix has (i, j)th entry that is x[i] * y[j]
 - $\mathbf{x} = \text{np.arange}(10)$
 - y = x.copy()
 - np.outer(x, y)
 - builds a multiplication table!
- concatenating arrays in 2D:
 - onp.concatenate() also has an axis kwarg which denotes which axis you want to lengthen
 - compare np.concatenate([a, b], axis=0) With np.concatenate([a, b], axis=1)
 - o np.stack(), np.hstack(), np.vstack()
- 3D arrays:
 - o can think of them as movies, i.e. a sequence of images

```
movie = np.random.random(80).reshape((5, 4, 4)) # 5 frames, each 4 x 4 pixels
for framei, image in enumerate(movie):
    f, ax = plt.subplots()
    ax.imshow(image, cmap='jet')
    f.canvas.set_window_title( 'frame %d' % framei)
```