

# BREAK EVEN AND MINIMUM COST ANALYSIS

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Often we have a choice b/w 2 alternatives whose one of them may be more economical under one set of conditions & the other may be more economical under another set of conditions.

By altering the value of some one variable in the situation holding all other points of difference b/w the two alternatives constant, it is often possible to find a value for the variable which may be makes the 2 alternatives equally economical. This value may be described as the Break Even Point.

When the cost of 2 alternatives is affected by a common variable. There may exist a value of the variable for which the two alternatives will have equal cost.

The cost of each alternative can be expressed as functions of the common independent variable & will be of the form  $T.C_1 = A_1(x)$  &  $T.C_2 = A_2(x)$

where,  $x$  - a common independent variable affecting both alt 1 & alt 2.

$T.C_1$  &  $T.C_2$  - are specified total costs for period of time for alt 1 & alt 2 respectively.

Solve for the value of  $x$  resulting in equal cost for alt 1 & alt 2 is accomplished by setting

the cost functions equal.  $T.C_1 = T.C_2$

$$\therefore A_1(x) = A_2(x)$$

which may be solved for  $x$  in detail.

The resulting value of  $x$  yields equal cost for the alternatives considered and is designated as the B.E.P.

(The Break Even Point) is that point of activity (Sales volume) where total revenues & total expenses are equal. It is the point of zero profit.

In other words, BEP is that specific level of activity or volume of sales where the firm break even, i.e. total cost equal total revenue. However, Break even point is the point where losses cease to occur while profits have not yet begun.

In cases the firm produces & sells less than the level of break even point, it would incur losses; while if it produces & sells more than the level of BEP it makes profits.

The BEP is also taken as the minimum level of production or sales which the company has to undertake in order to be economically viable.

It reveals the relationship b/w volume & cost of production on the one hand and revenues and total expenses/ profits obtained from the sales on the other hand.

It captures the relation of fixed costs, variable costs, the value of O/P, sales mix, prices etc. to the profitability of the company.

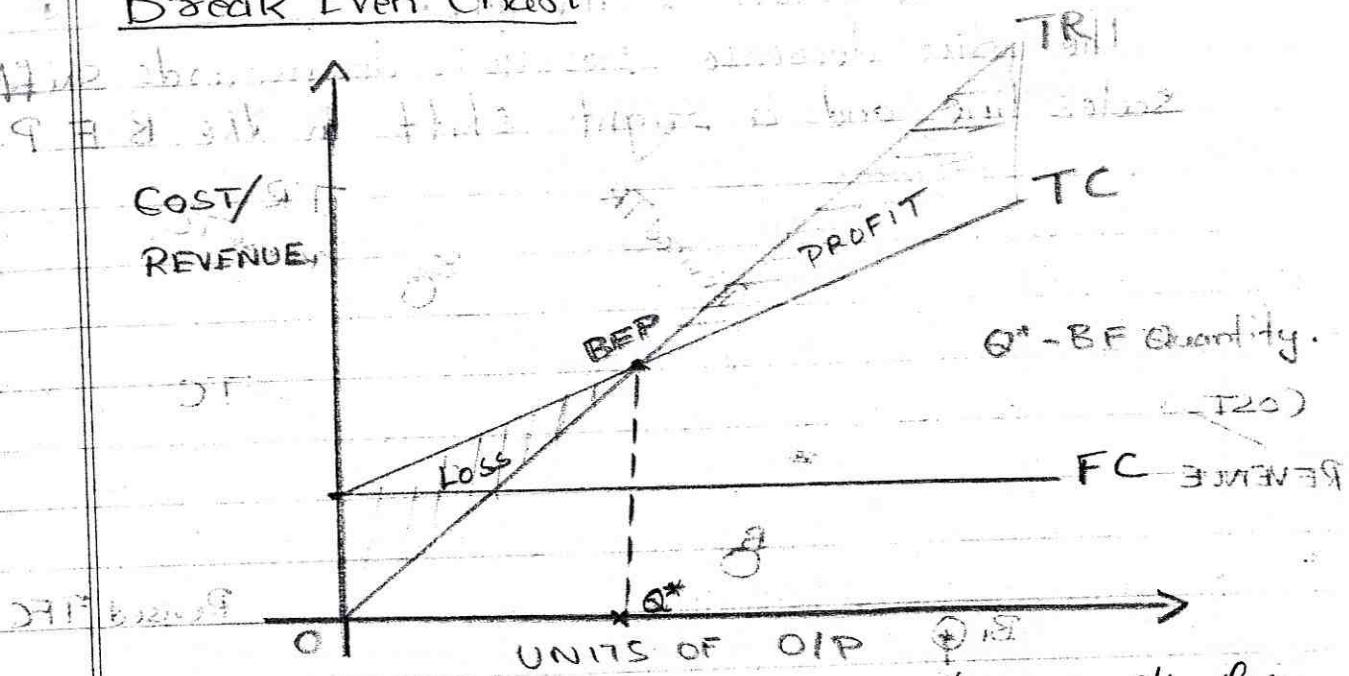
According to Mertz, Lucy & Frank "A BE Analysis indicates at what level costs & revenue are in equilibrium".

There are two approaches to representing a B.E.P.

i) Graphical Method - (Using B.E. Charts).

ii) The Algebraic Method:

## Break Even Chart



BE Charts are often used for determining the following,

- a. Break Even production volume
- b. Profit appropriation for a given level of output
- c. Choice of optimum level of o/p.
- d. Impact of rate of changes in sales on costs & profits.

NOTE - Preparation of BE chart is done using the income statement of the company.

Analytical Approach - Uses single Income statement

Statistical Approach - No. of income statements.]

## Changes in Costs & Price and B.E.P

The costs of a firm comprise either because of additional variable costs or increase in fixed costs. In both these cases the B.E.P will undergo a shift to the right.

On the other hand, decline in these cost could shift B.E.P towards the left.

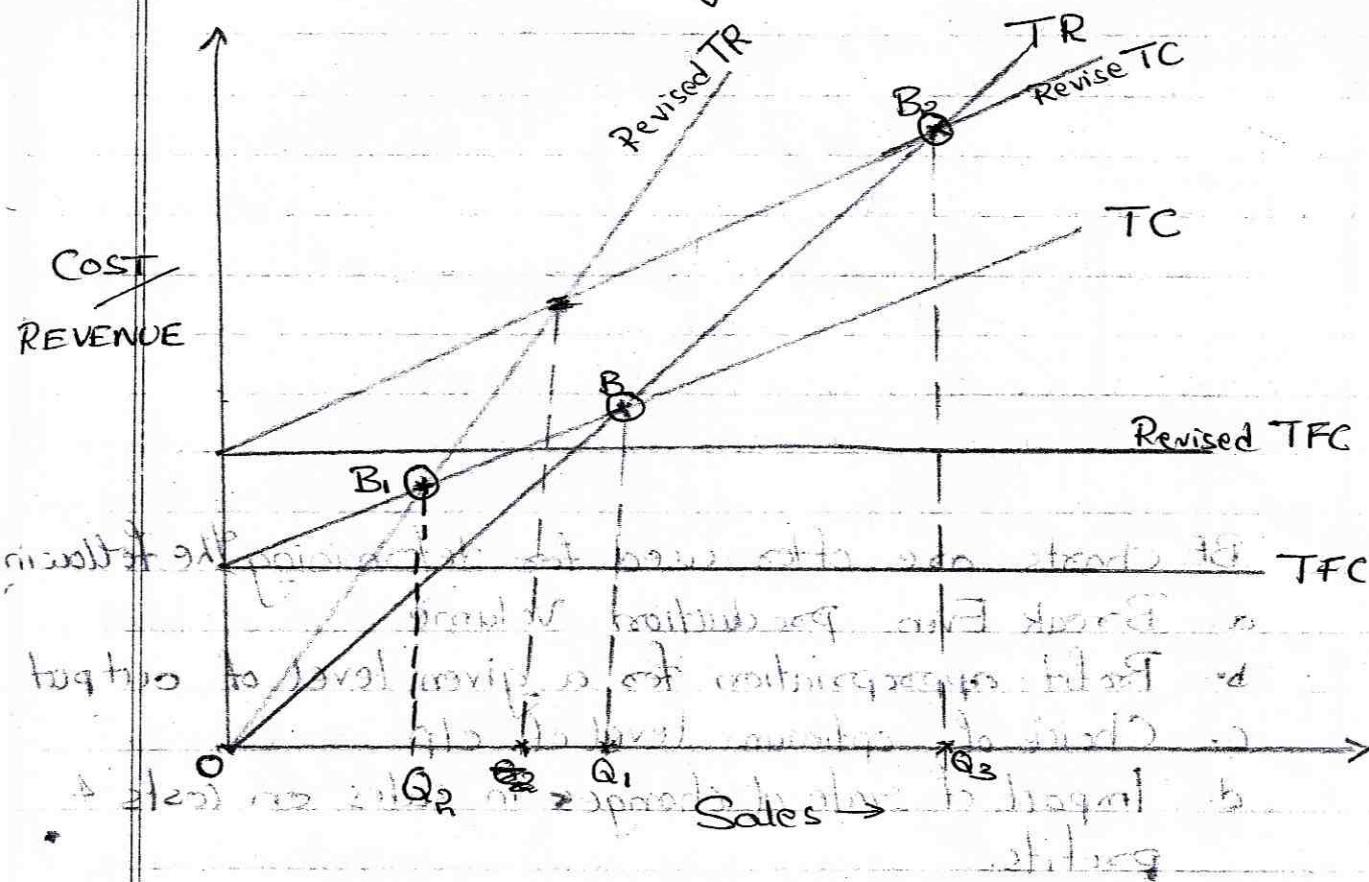
1) If Total sales line shifts due to changes in price.

A rise in price shifts the sales line upwards, & consequently

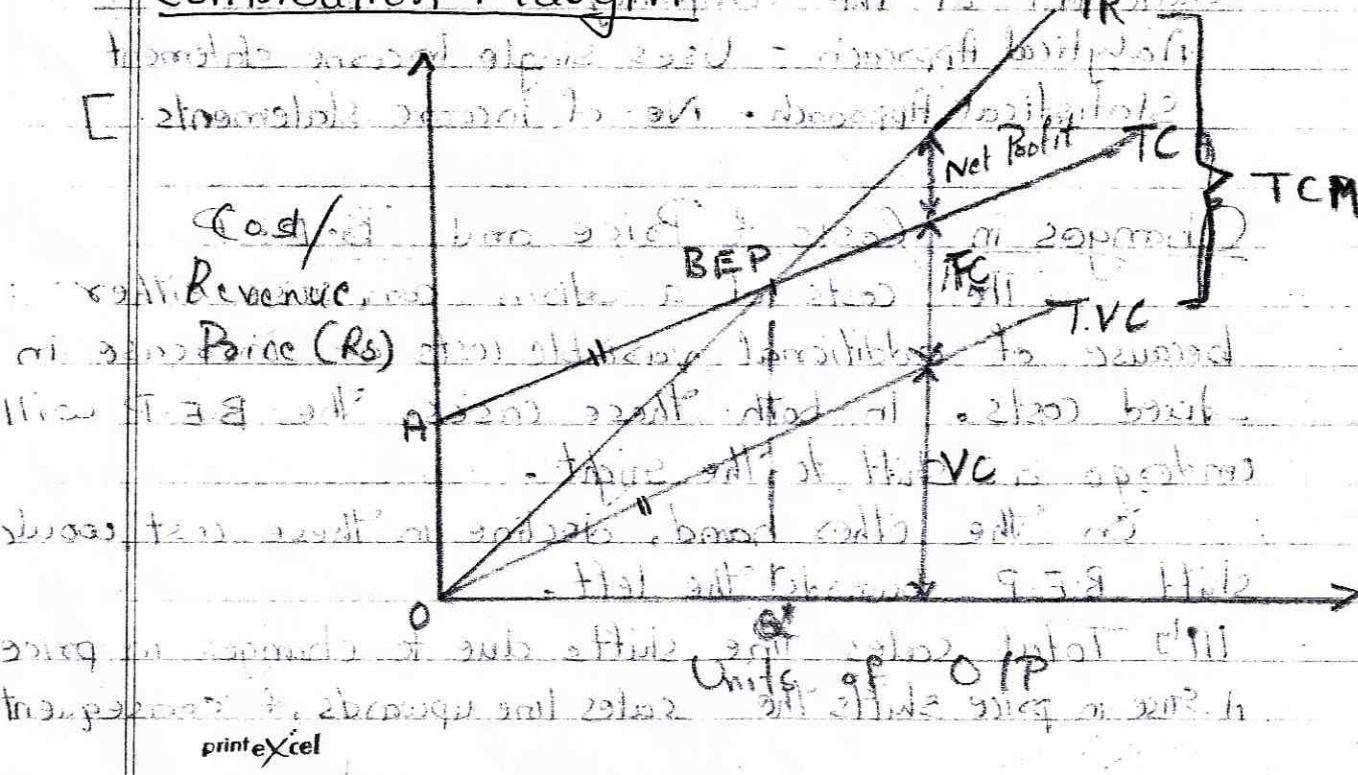
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B.E.P. would shift to the left.

The price decrease results in downwards shifts in sales line and a right shift in the B.E.P.



### Contribution Margin



Business managers don't usually think profit in the economic sense i.e. the difference b/w total revenue & total costs. Instead for short term, where a part of firm's investment is a sunk investment, they use a more appropriate concept known as contribution margin or contribution profit.

Contribution Margin: It is the difference b/w the total revenue (TR) & total variable cost (TVC).

$$\text{Total Contribution Margin} = TR - TVC \\ = \text{Net Profit} + \text{Fixed Costs.}$$

If the Total Net Profit = 0, then  $TCM = TFC$  and the firm achieves Break Even Point.

Average Contribution Margin (ACM) is the difference b/w unit price and avg. variable cost.

Break even occurs when avg. contribution margin (ACM) is equal to avg. fixed costs (AFC).

### Assumptions in B/E Analysis

The B/E A is based on a set of assumptions, some of which are quite restrictive.

The assumptions underlying the analysis are the following:

1. It assumes that costs can be classified into fixed & variable costs, thus ignoring semivariable costs.

2. Sale price of the product is assumed constant, thus giving linearity property to total revenue curve.

3. It assumes constant rate of increasing demand, thereby imparting linearity into the curves of total cost.

4. It assumes no improvement in technology & labour efficiency.

5. Changes in input prices are also ruled out.
6. Production & Sales are synchronised, in the sense there is no addition or subtraction from inventory.

### Uses

The main advantages of using BEA in managerial decision making can be the following:

1. It helps in determining the optimum level of O/P, below which it could not be profitable for a firm to produce.
2. It helps in determining the target capacity for a firm to get the benefit of minimum unit cost of production.
3. With the help of the B.E.A, the firm can determine the minimum cost for a given level of O/P.
4. It helps in deciding which products to be produced and which to be bought by the firm.
5. Plant expansion or contraction decisions are often based on the B.E.A of the perceived situation.
6. Impact of changes in price and costs on profits of the firm can also be analysed with the help of B.E technique.
7. Sometimes, a management has to take decisions regarding dropping or adding a product to the product line.
8. It evaluates the financial yield from a project.
9. It can be used in finding the S.P. which would prove most profitable for the firm.

From finding the B.E.P., the B.E.A helps in establishing the point wherefrom the firm can start payment of dividends to its shareholders.

## Limitations

1. Often we find that O/P prices, like material prices usage etc. undergo a change over time. Since B.F.A is based on past data, such data need to be adjusted for changes in O/P prices. These are avoided because of their complexity in analysis.
2. The B.F.A chart is one dimension basis of given product prices. In fact, the product prices change frequently. The non-inclusion of changes in product prices basically due to difficulty of precisely estimating the sales volume at various prices. But this non-inclusion of product prices imparts its share of unrealism to the results.
3. The B.F.A is static in nature, in the sense that it assumes a constant relationship of O/P to costs & revenues.
4. It is assumed in the analysis that the relative share of different products in the total O/P remains the same. In practical sense frequent changes in the composition of demand and product mix.
5. It is common knowledge that profits depend on various factors like technological improvements, managerial effectiveness etc and not only on level of O/P. The B.F.A by its assumptions only on O/P gives a partial view.
6. Since B.F.A is generally based on accounting data, it suffers from many limitations like omission of imputed costs, lack of scientifically determined depreciation etc.

7. The B.E.A ignores selling costs and only concentrates on the production costs.

8. It is not necessary that all in the particular period results in costs only during that period. Some costs, like maintenance, may partly be due to output in the earlier periods. While postponing the maintenance costs in the current period would result in ~~in~~ assigning the maintenance costs to the output of the subsequent periods, though these obviously do not ~~not~~ belong to output in that period.

### Determination of Break Even Point

~~At~~ Before we take up the B.E problems for solution,

let us define the following symbols.

$Q$  = Units of output (physical);  $Q_B$  - B.E quantity.

$P$  = Price per unit or Avg. Revenue (ass. constant)

$T.R = P \times Q$  = Total Revenue.

$\overline{TFC}$  = Total Fixed Cost or Revenue in  $R$

$\overline{TV C}$  = Total Variable Cost or  $TVC$

$\overline{TC} = \text{Total Cost} = [TFC + TVC \text{ or } TFC + Q(AVC)]$

$AFC$  = Avg. Fixed Cost

$ACM$  = Avg. Contribution Margin [ $= P - AVC$ ]

$TCP$  = Total Contribution Profit [ $= TR - TVC \text{ or } Q(ACM)$ ]

$TNP$  = Total Net Profit [ $= [(TR - TC)]$ ]

To determine B.E Point

To determine B.E Point what happens if  $Q = 0$ ?

$T.R = T.C$

which may be written as  $T.R = T.F.C + Q_B(A.V.C)$

$$Q_B (P - AVC) = TFC$$

∴ Break Even Quantity would be,

$$Q_B = \frac{TFC}{P - AVC} \quad \text{--- (1)}$$

(1) can be re-written in terms of contribution margin;

$$Q_B = \frac{TFC}{P - CM} \quad \text{--- (2)}$$

where,  $CM$  is contribution margin.

Eq. 2 can be is basic ie equation<sup>2</sup> and can be expressed in 3 ways,

- (1) As No. of units of goods sold
- (2) As a Rupee Volume of sales
- (3) As a Percentage of Plant capacity.

Each of these needs a different expression of the contribution margin.

For this we take an example

1. A costal ship can carry a maximum of 1,00,000 passengers per month at a fee of Rs 850. Variable cost per passenger is Rs 100. The fixed cost are Rs. 175,00,000 per month. Find The  
 (a) Break Even Point  
 (b) Sales Volume of Ship to break even  
 (c) Break Even Point in terms of quantity sold.

0.00	250000
250000	0.00

(a) In terms of BE Quantity: (Ans 10)

$$Q_B = \frac{TF.C}{P - AVC} = \frac{Rs. 75,00,000}{850 - 100}$$

$$= \underline{\underline{10,000 \text{ passengers}}}$$

(b) In terms of Rupee volume of sales,

(c) Contribution Margin as the fraction of price or revenue that contributes to payments of fixed cost + profit.

$$S_B = \frac{TF.C}{1 - (AVC/P)}$$

$$\text{where } S_B = \frac{TF.C}{1 - (IVC/TR)}$$

$$\text{Let us assume } 75,00,000 \text{ from part (a)}$$

$$1 - \left( \frac{100}{850} \right)$$

$$100,00,000 \text{ is revenue} = 85,00,000 \text{ is total H.C}$$

or 850 is 85% of 100000000

As % of Capacity may vary from station to station

Here we need to multiply Avg-contribution margin (ACM) by plant capacity. This will provide us Rupee value of sales that plant can contribute to fixed cost + profit.

Let us express Plant capacity as  $Q_{max}$

$$\%_B = \frac{TF.C}{(P - AVC) Q_{max}} \times 100$$

Also we can express as,

$$\%_B = \frac{Q_B}{Q_{max}} \times 100$$

$$\frac{75,00,000}{(850 - 100)} \times 100 = 1,00,000$$

$$\frac{7500000}{750 \times 100000} \times 100 = 10\%$$

2 A retailer plans to sell a baby elephant toy at a local fair. This purchase price of the toy is Rs 7/- per piece with a privilege of returning the unsold toys. The booth rent at the fair is Rs 250/- payable in advance. S.P. of the toy is Rs 12/-/piece. Find out the no. of toys which must be sold to break even & also the B.E sales value.

$$TFC = 2500 \text{ Rs} \quad (i) \quad Q_B = \frac{TFC}{P - AVC}$$

AVC is Rs 7/- breaking point P = AVC + Rent  $\Rightarrow P = 7 + 2500 = 2507$   
 and S.P. = Rs 12/- At sales point  $\Rightarrow 12 = 7 + \frac{2500}{Q_B} \Rightarrow Q_B = \frac{2500}{12 - 7} = 500 \text{ units}$   
 (break even point)

- Find (ii) Break Even Sales Value

$$\text{Ans} (i) \quad Q_B = \frac{TFC}{P - AVC}$$

$$S_B = Q_B \times SP \Rightarrow 500 \times 12 = 6000 \text{ Rs}$$

3 The following data is regarding a company. Find the B.E.P in terms of sales volume & unit cost.

Sales : Rs 1,00,000

(i) If Fixed Cost is Rs 2,00,000 then find B.E.P

(ii) If Variable Cost : Rs 50,000

(iii) Wkt. At B.E

$$TR = TFC + Profit$$

$$Q_B = \frac{TFC}{P - AVC}$$

$$Q_B \times P = \frac{TFC}{1 - AVC} \quad \left[ \begin{array}{l} TVC = \frac{AVC \times Q}{Sales} \\ \Rightarrow \frac{AVC \times Q}{P} \end{array} \right]$$

$$\therefore S_B = \frac{TFC}{1 - AVC/P}$$

ie profit margin  $\approx$  R,00,000  
 profit after tax  $\approx$  -250,000  $\rightarrow$  loss  
 profit contributed to overheads  $\approx$  100,000  
 profit after overheads  $\approx$  R,00,000  $\rightarrow$  no profit  
 $\rightarrow$  selling price  $\approx$  0.52  $\rightarrow$  margin on selling  
 overhead  $\approx$  block  $\therefore S_B = \text{Rs. } 4,00,000/-$

A firm has purchased a plant to manufacture a new product, the cost data for which is given below

Estimated annual sales R4000 units

Estimated costs :

Material	Rs. 4/unit
D. Labour	Rs. 0.60/unit
Overhead	Rs. 24,000/year
Administrative expenses	Rs. 28,800/year
Selling expenses (Fixed)	15% of Sales

Calculate SP, if profit/unit is Rs. 1.0241

Find out the B.E.P. in terms of units of 1000

1000 units : 25102

i. Estimated cost of production for 24000 units.

Material @ 4/unit	3.8 H	136400
Ds. Labour @ 0.6/unit) T = 81		24000
	377	82

Estimated cost of production for 24000 units	
Material @ 4/-/unit	96000
Direct Labour @ 0.06/unit	14400
Overhead @	24000
Administrative expenses	<u>Rs 28800</u>
	<u>Rs 1,63,200</u>

$$\therefore \text{Total Cost of Production} = \text{Rs } 163200$$

$$\text{Total Cost} = \text{Total Cost of Production} + \text{Total Selling Cost}$$

$$= \text{Rs } 163200 + 15\% \text{ of } \cancel{163200} \times$$

Profit on 24000 units (@ Rs 1.02 per unit)

$$= \text{Rs } 24000 \times 1.02 - \text{Rs } 24480$$

Let the Sales Volume = Rs  $X$

Then  $\text{Rs } X = \text{Total Cost} + \text{Profit}$

SVA 42

$$X = \left( 163200 + \frac{15}{100} X \right) + 24480$$

$$\text{Rs } X \left( 1 - \frac{15}{100} \right) = \text{Rs } 187680$$

$$\frac{85}{100} X = 187680$$

$$X = 187680 \times \frac{100}{85}$$

Ans) Total Sales Volume = 2192000

Required Profit = Total Sales Volume - Total Cost

= 2192000 - 163200

Thus total Sales Volume = Rs 2192000

Printed by Rs 104,800

29) If selling price of 192 units is Rs 104,800, then  
Total Sales Volume = Rs 104,800 / 1.02

(ii) At BEP, the units sold of the product should be such that their total cost is covered by total receipts from their sales. The BEP sales are where

$$\text{Total Sales Volume} = \frac{\text{Total Cost}}{\text{Selling Price per unit}}$$

~~$$200,000 \text{ units sold} \times \$10 = \text{Total Cost}$$~~

~~$$200,000 \times \$10 = \frac{\text{Total Cost}}{\text{Selling Price per unit}}$$~~

~~$$200,000 \times \$10 = \frac{\text{Total Cost}}{\$10 + 15\% \times \$10}$$~~

~~$$200,000 \times \$10 = 63,200 + 15\% \times 2,208,000$$~~

~~$$200,000 \times \$10 = 63,200 + 330,720$$~~

~~$$200,000 \times \$10 = \frac{393,920}{\$10}$$~~

~~$$200,000 \times \$10 = 39,392 \text{ units}$$~~

~~$$200,000 \times \$10 = 39,392 \text{ units}$$~~

$$\text{BEP Sales Volume} = \frac{\text{TCF} + \text{Total Selling expense}}{\text{SP} - \text{AVC}}$$

$$200,000 + \left( \frac{\$10 \times 0.05 \times 200,000}{\$10} \right) = \frac{(200,000 + 28,000)}{\$10} + 0.15 \times 2,208,000$$

$$200,000 = \frac{21,920 \times 4,60}{\$10}$$

$$200,000 = \frac{18,6279}{\$10} / \text{units}$$

$$200,000 = \frac{18,6279}{\$10} / \text{units}$$

5. A manufacturer sells his product at Rs 5/- each, Variable costs are Rs 2/- per unit & the FC amount of Rs 60,000/-

i. Calculate the BEP point in units

ii. What would be the profit if firm spends Rs 3000 unit on advertising.

iv. How much should the manufacturer sell to make profits of Rs 30,000/-

$$i. \text{ BEP, } Q_B = \frac{\text{TFC}}{S - \text{AVC}}$$

$$= \frac{60000}{5 - 2}$$

$$= 20000 \text{ units.}$$

$$ii. \text{ Profit} = \text{TR} - (\text{TC})_{\text{fixed}} + \text{E.P.}$$

$$= [5 \times 30000 - (60000 + 2 \times 30000)]$$

$$= 150000 - 120000$$

$$= \underline{\text{Rs. } 30000 \text{ per unit}}$$

$$iii. \text{ Q.B.E.P. in } \frac{\text{AVC}}{\text{S} - \text{AVC}} = \frac{60000 + 3000}{5 - 2}$$

$$= \frac{63000}{3} = \underline{\text{Rs. } 1000 \text{ units}}$$

$$iv. \text{ Target Sales Volume} = \frac{\text{FC} + \text{Target Profit}}{\text{S} - \text{AVC}}$$

$$= \frac{63000 + 30000}{5 - 2}$$

$$= \underline{\text{Rs. } 31000 \text{ units}}$$

6. ABC Company manufactures a toy which has a variable cost of Rs 10/-/unit & a SP of Rs 15/unit. Fixed costs are budgeted at Rs 60000. It
- Calculate the no. of toys needed to be sold in order to break even.

b. What is the B.E. (Break Even) volume?

- How many toys are to be sold to generate a profit of Rs. 15000/-.

Profit margin is 20% of selling price  
Profit margin of 20% is 1.2 times of

$$a \quad Q_B = \frac{TFC}{SP - AVC}$$

$$= \frac{40000}{15 - 10}$$

$\therefore = 8000$  toys.

b. BEP sales volume  $\Rightarrow 18000 \times 15$

$$\text{[Fixed costs + Profit]} = \text{Total Sales} - \text{Total Cost}$$

c. To generate a profit of - Rs 15000

$$\text{Sales} = \frac{\text{TFC} + \text{Profit}}{SP - AVC}$$

$$S = \frac{40000 + 10000}{15 - 10}$$

$$= \frac{50000}{5} \times 15$$

$\therefore 18000 \text{ toys} + 27150 \text{ more toys}$

$$= \frac{55000}{5} \times 15$$

$$= 165000 \text{ Rs}$$

### MARGIN OF SAFETY (MOS)

"It is the excess of budgeted or actual sales above the break even sales volume."

Mathematically,

$$\text{Margin of Safety} = \text{Actual Sales} - \text{Break Even Sales}$$

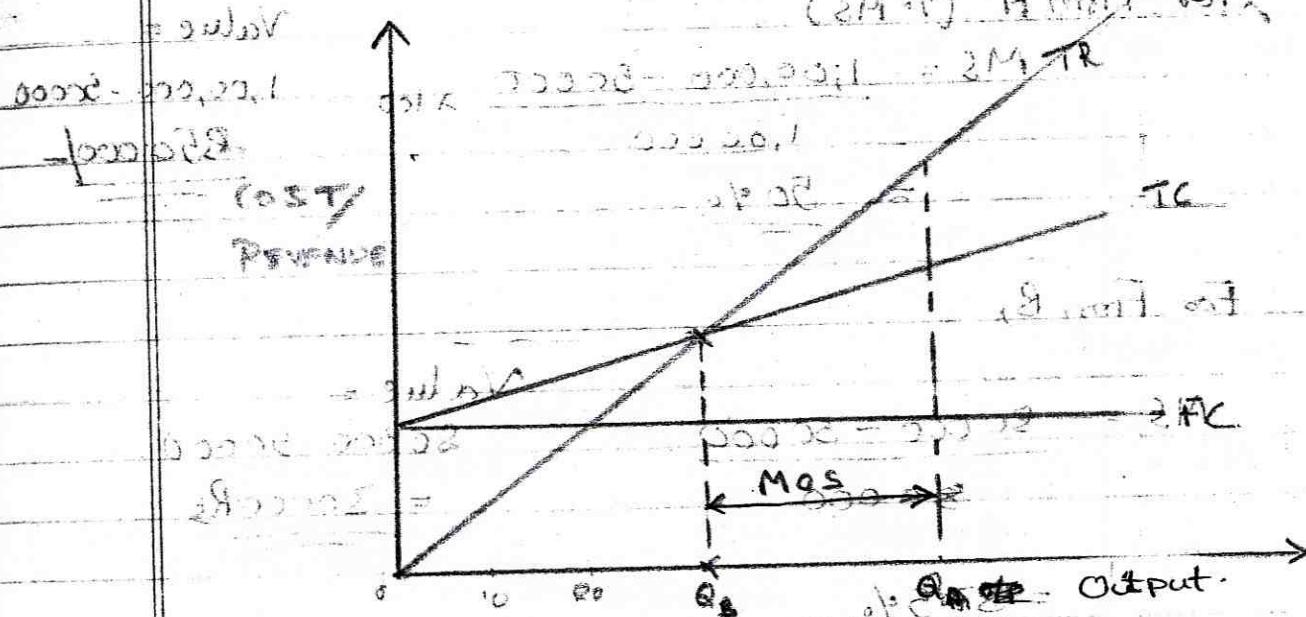
At the BEP, the firm is just able to cover the fixed costs, besides the variable cost.

In case the BEP actual sales is more than the BEP the firm is able to make profits.

In other words greater the safety margin, greater would be the profits.

It is important for a firm to have a reasonable safety margin. With a low safety margin the firm is running a risk. The risk of making losses during the phases of reduced business activity.

The low safety margin may be due to the lower actual sales or the fixed costs are very high.



$Q_B$  - Break Even Quantity

$Q_A$  - Actual Quantity

$$\text{Safety Margin} = Q_A - Q_B$$

Margin of Safety can be expressed as percentage of value also,

$$MS = \frac{Q_A - Q_B}{Q_A} \times 100 \%$$

Find the margin of safety of a firm A & B given the following data

Total revenue 2M 600 (or) 2M and costs 2M

For rated output firm A produces goods at 100 per unit

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• 8 months

Firm A

Firm B

Actual total Sales	1,00,000	Rs 60,000
Budgeted Sales	1,00,000	Rs 80,000
B.E. Sales	50,000	Rs 50,000

Which company is better placed w.r.t its MS & Why?

Based on Budgeted Sales

For Firm A (% MS)

$$\text{MS} = \frac{1,00,000 - 50,000}{1,00,000} \times 100 = \frac{50,000}{1,00,000} \times 100 = 50\%$$

Value = Rs 50,000/-

For Firm B,

$$\text{MS} = \frac{80,000 - 50,000}{80,000} \times 100 = \frac{30,000}{80,000} \times 100 = 37.5\%$$

Value = Rs 30,000/-

Based on Actual Sales

For Firm A,

$$\text{MS} = \frac{100,000 - 50,000}{50,000} \times 100 = \frac{50,000}{50,000} \times 100 = 100\%$$

Value = Rs 50,000/-

For Firm B,

$$\text{MS} = \frac{60,000 - 50,000}{60,000} \times 100 = \frac{10,000}{60,000} \times 100 = 16.7\%$$

Value = Rs 10,000/-

It is clear from MS (%) and MS value that,  
For the above analysis Firm A has a better safety margin  
than Firm B.

Ques 3. If the fixed cost of a company are Rs 6000/- & the variable cost is Re 10/- per unit of O/P, & the S.P. is Rs 20/- per unit. Find the B.E. point.

Ques 2. If the company sells 10,000 units of the product, find the safety margin of the company.

Ans: B.E.P. =  $\frac{\text{Fixed Cost}}{\text{S.P.} - \text{A.V.C.}}$

Given: Fixed cost = 60000  
S.P. = 20/-  
A.V.C. = 10/-

Now, B.E.P. =  $\frac{60000}{20 - 10} = 6000$  units.

Break even point = Total fixed cost / (S.P. - A.V.C.)

Break even point =  $\frac{60000}{20 - 10} = 6000$  units

Actual Q.S. =  $15000 \times 20 = 300000$  Rs.

Safety Margin =  $\frac{\text{Actual Sales} - \text{B.E.P. Sales}}{\text{Actual Sales}} \times 100$

Safety Margin =  $\frac{\text{Actual Sales} - \text{B.E.P. Sales}}{\text{Actual Sales}} \times 100$

$$\text{Safety Margin} = \frac{300000 - 120000}{300000} \times 100 \\ = 40\%$$

With 100% safety margin, Break even point = 120000

### Break Even Analysis - Comparison of Alternatives

With 100% safety margin, Break even point = 120000

1. A 50 HP motor is required to drive a pump to remove water from a funnel. The unit will be needed for a period of 4 years.

Two alternatives are under consideration.

Alternative 'A' calls for the construction of a power line & purchase of the electric motor. The total cost of \$4900. The salvage value of this equipment after 4 years is estimated to be \$700.

The cost of the current for the per hour of the operation is estimated to be \$2.94 per year and maintenance is estimated at \$420 per year.

Alternative B, calls for purchase of a diesel engine pump set at a cost of \$1925. It will have no salvage value at the end of 4 years period. The cost of diesel per hour of operation is estimated at \$1.47. maintenance is estimated at \$0.53 per hour of operation and the cost of the wages chargeable when the engine runs is \$2.8 per hour.

How many hours per year the two machines have to run so that the two alternatives incur equal costs. If the no. of hours of operation is estimated at 100 year which alternative is more economical. Take interest rate at 10% per year.

### Solution

Let  $X$  be the no. of hours of use of the operation per year.

Let  $TCA$  = Total equivalent annual cost of Alt. A

$TCA = \text{Capital Recovery} + \text{Maintenance Cost} + \text{Current Cost}$

$TCA = \frac{\text{Cost}}{\text{Life}} + \text{Maintenance Cost} + \text{Current Cost}$

$$\text{CR} = \frac{(P - R)}{(A/p, 10, 4)} + 700 + 1.47X$$

or \$1391.5000 add to last add

for 50% of bottomline 21 months  
100% extra 10 bottomline 21 months time

$$TC_A = 1395 + 420 + 2.94 \times x$$

$$\text{and } TC_B = 1815 + 2.94x \quad (1)$$

(Annual fixed) Maintenance  $\rightarrow$  per hr  $\rightarrow$  per day  
 Alt A  $TC_B = CR(i)_B + \left[ \begin{array}{l} \text{Cost of diesel +} \\ \text{Maintenance + wages} \end{array} \right] \times \text{No. of hours.}$

$$\text{function of } CR(i)_B = (P+R)(A/P, i, n) \text{ at } F.O.T.$$

$$(1925-0) \left( \frac{A}{P, 10\%, 4} \right) \times 0 \times i$$

Alt A cost  $\rightarrow$  \$607.28

$$\text{So Alt } TC_B = 607.28 + (1.47 + 0.53 + 2.8) \times x$$

$$TC_A = 607.28 + 4.8x \quad (2)$$

Now if we equate  $TC_A = TC_B$  i.e.  $(1) = (2)$ , then we will get 'x' is the value of no. of hours of operation of alt. A & B at which the costs are equal, i.e. BEP.

$$TC_A = TC_B$$

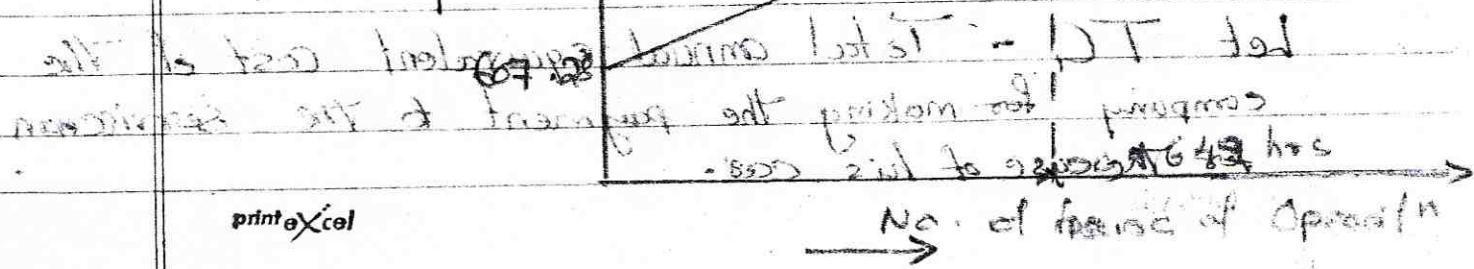
$$1815 + 2.94x = 607.28 + 4.8x$$

$$1207.72 = 1.86x$$

BEP marked on chart is 649 hrs

All pd. will start at 649 hrs

Alt B's costs to N & all others BEP is 649 hrs



From the chart it is very clear that if the actual no. of hours of operation is less than 649 hrs, At B is more economical (diesel engine). If the no. of hours of operations is greater than 649 hrs. Then At A is economical (electric motor).

When the no. of hrs (of operation) is 100 alternative B is economical.

~~100 hrs (0-25 P)~~

- Q. A company may furnish a car for use by a service man for transportation b/w its properties or the company may pay the service man for the use of his car at a rate of \$0.16/km for this purpose.

The following estimated data apply to company furnished cars. A car costs \$4000 and has a life of 4 years and a trade-in value of \$800 at the end of that time. Monthly storage costs for the car is \$20 and cost of fuel, main frame & tyres is \$0.06 per kilometer.

How many km the service man must travel annually by car for the cost of the two methods of providing transportation to be equal if the interest rate is 15% per year.

Let  $x$  be the no. of km travelled by the service man annually so that the costs of both alternatives are equal.

Let  $TG_1$  = Total annual equivalent cost of the company for making the payment to the service man for the use of his car.

$T C_2$  = Total annual equivalent cost of company to time furnishing its car to service man.

At BEP,  $x = 800$ ,  $T C_2 = 1481$  at  $x = 1000$

$$\Rightarrow \text{point } T C_1 = 0.16 \times x \quad \text{at } x = 1000 \quad (1)$$

$$T C_2 = CR(i) + \text{Annual Storage} + \text{Annual cost of fuel}$$

Cost of depreciation

Fees & maintenance.

$\downarrow$   $W_{13}$   $\downarrow$   $20$   $\downarrow$   $800$

$$CR(i) = (4000 - 800) (A/P, 15\%, 4) + 800 \times 0.15$$

constant

$$= 1241 + 20 \times 12 + 0.06 \times x$$

$$T C_2 = 1481 + 0.06 \times x \quad (2)$$

At BEP,  $1481 + 0.06x = 1241 + 20 \times 12$

$$0.06x = 14810$$

$$0.06x = 14810 \quad x = 247 \text{ km}$$

$$247 \text{ km} = (a, b, c, d) \text{ km}$$

$$(a, b, c, d) = 14810 \text{ km}$$

Alt 1 Alt 2

If  $x < 14810 \text{ km}$ , Alt 1 is

(a, b, c, d) recommended

else Alt 2

Alt 1

If  $x > 14810 \text{ km}$ , Alt 2 is recommended.

14810

$$FAD = (a, b, c, d) \text{ km}$$

Alt 2

BEP

0.16x

0.06x

14810

FAD = 14810 km

$1 - (i+1)$

$$FAD = 1.0 \times 1.0 =$$

$$1 - (i+1)$$

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3. M/c A costs Rs 3000/- has zero salvage value at any time & labour cost per unit of product on it is Rs 17/- . M/c B costs Rs 54,000 and has a zero salvage value at any time & labour cost per unit of production is Rs 12.50 . The interest rate is 10% p.a + 3% ad. CPT

If the annual output of production is 3000 units with how many years of service will the two m/c's break even in equivalent annual cost.

Solution

Let  $\overline{TC_A}$  - Total equivalent annual cost of m/c A

$\overline{TC_B}$  - " " " " " m/c B

$\Rightarrow 3000 \times 17 + 51000 \times i = 3000 \times 12.50 + 54000$  CPT

At an output of 3000 units per year

$$\begin{aligned} \overline{TC_A} &= 3000(A/P, 10, n) + 17 \times 3000 \\ &= 3000(A/P, 10, n) + 51000 \end{aligned}$$

$$\begin{aligned} \overline{TC_B} &= 54000(A/P, 10\%, n) + 12.50 \times 3000 \\ &= 54000(A/P, 10, n) + 37500 \end{aligned}$$

For the two m/c's to break even,

$$\overline{TC_A} = \overline{TC_B}$$

$$3000(A/P, 10\%, n) + 51000 = 54000(A/P, 10\%, n) + 37500$$

$$51000(A/P, 10\%, n) = 113500 \times 0.1211 \times 2.71$$

$$(A/P, 10\%, n) = 0.2647$$

$$\frac{i(1+i)^n}{(1+i)^n - 1} = 0.2647$$

$$\frac{0.1 \times 1.1^n}{1.1^n - 1} = 0.2647$$

get present value =  $0.2647$ . Then divide it by  
1.1% of 12 months. This gives us the monthly  
leasing payment to  $0.2647 \times 12 = 31.76$

$$2. \quad \$100 \times \frac{1}{1.1^{12}} = 0.1 \text{ initial cost} + 31.76$$

$$\text{24 years old} \Rightarrow \text{initial cost} = 0.2647 \times 12 \times 24 =$$

$$\text{\$6.2224}$$

Time 12, and  $1.1^{12} = 0.11^{12} = 0.62224$

Time 13, and  $1.1^{13} = 0.11^{13} = 0.2647$  to start over for

monthly lease cost for year 2 and the other 24 years

$$\text{monthly cost} = 31.76 \times 1.1^{12} = 1.6073$$

and any new  $\log 1.1 = \log 1.6073$  additional

cost at bank.  $n = 4.98 \text{ years} \approx 5 \text{ years}$

(ii)  $\rightarrow$  initial number of and time, same  
with costs will change and  $\text{TC}_A < \text{TC}_B$

$$3. \quad \text{If } n=6, \text{ then } \text{TC}_A \text{ and } \text{TC}_B$$

$$\text{TC}_A = \$1688 \text{ and } \text{TC}_B = \$1946$$

$$\text{and } \text{TC}_B = 49898 \text{, but } \text{TC}_A = 54534$$

and cost of just 2nd at bank is  $\approx 1.1^{12}$

If  $n < 5$  years then  $\text{TC}_A$  is more than  $\text{TC}_B$ .

is economical than bank when less than 5 years.

For values of  $\text{TC}_A$  and  $\text{TC}_B$  see page 229

If  $n > 5$  years then  $\text{TC}_B$  is more than  $\text{TC}_A$   
is economical.

the answer is  $\text{TC}_A$  because all  $n \geq 5$

these are similar to  $\text{TC}_B$  and  $\text{TC}_A$  is more than  $\text{TC}_B$

### Costs

Initial cost  $\uparrow$  to  $\text{TC}_A$   $\text{TC}_B$   $\text{TC}_C$   $\text{TC}_D$

BEP

sim best alternative to two hour fast food  $\text{TC}_A = \$1$

sim best  $\text{TC}_B = \$1$  " " " " "  $n=5 = \$1$

$\Rightarrow$  Year

printExcel

4. A sheet metal Company is considering the purchase of an automatic feed m/c for a certain phase of finishing process.

The m/c has initial cost of \$ 23,000, a salvage value of \$ 4000 & life of 10 yrs. If the m/c is purchased one operator is reqd. at the rate of (cost) \$ 12 per hour. The O/p with this m/c will be 8 tons/hr. Annual maintenance & operation cost of the m/c is expected to be \$ 3500.

Alternatively, the company can purchase a less sophisticated manual feed m/c for \$ 8000, which has no salvage value & life of 5 years. However with this alternative 3 workers will be required at a cost of \$ 8 per hour (each of the m/c will share) an annual maintenance and operating cost of \$ 1500. O/p is expected to be 6 tons per hour for this m/c. All ~~investment~~ capital return @ 10% per year.

- i. How much sheet metal must be finished per year in order to justify the purchase of the automatic feed m/c?

- ii. If the management anticipates a requirement to finish 2000 tons per year which m/c would be purchased?

Let  $x$  be the no. of tons of sheet metal produced/year.

$TC_1$  = Total equivalent annual cost of automatic feed m/c

$TC_2$  = " " " " " manual feed m/c.

$$TC_1 = CR(i) + \text{Annual maintenance} + \text{Annual labour cost}$$

+ operations cost

Annual Labour cost = 1 hr - 8 tons

$$\left(\frac{x}{8}\right) ? \text{ will be tons} < 10$$

$$\text{Labour cost} = \frac{x}{8} \times 10$$

$$= 1.25x \text{ Rs.}$$

$$TC_1 = [(23000 - 4000)(A/P, 10\%, 10) + 4000 \times 6.10]$$

$$+ 8000 + 1.25x$$

$$= 6992.25 + 1.25x$$

and cost of 12 tons maintenance labour cost is avoided

$$TC_2 = CR(i) + \text{Annual Maintenance} + \text{Annual labour costs}$$

$$\left(\frac{x}{6}\right) 3 \rightarrow x \text{ tons of waste labour cost}$$

and cost of 12 tons of waste labour cost is avoided

$$\text{Labour cost} = \frac{x}{6} \times (8 \times 3) + 4000$$

and cost of 12 tons of waste labour cost is avoided

and cost of 12 tons of waste labour cost is avoided

$$TC_2 = 8000(A/P, 10\%, 5) + 1000 + 4000$$

and cost of 12 tons of waste labour cost is avoided

$$= 3610.4 + 4x$$

and cost of 12 tons of waste labour cost is avoided

$$TC = TC_1 - 2000 \text{ or } TC_2 - 2000$$

$$= 6992.25 + 1.25x - 3610.4 + 4x$$

and cost of 12 tons of waste labour cost is avoided

$$= 3381.8 + 1.25x$$

and cost of 12 tons of waste labour cost is avoided

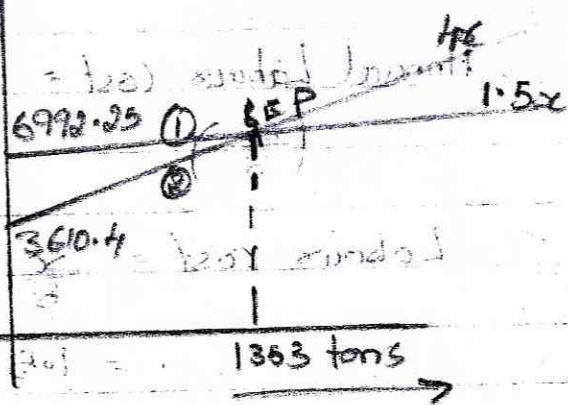
and cost of 12 tons of waste labour cost is avoided



If  $x < 1353$  tons  
manual feed mlc is  
recommended

If  $x > 1353$  tons Then  
auto feed mlc is recommended

If  $x = 2000$  tonnes auto feed  
mlc is recommended.



5. A contractor is offered his choice of either gasoline, diesel or butane engine to power a bulldozer he is to purchase.

The gasoline engine will cost \$2,000 & will have an estimated maintenance cost of \$200 per year and will consume 1.6 bushels of fuel per hour of operations.

The diesel engine will cost \$2800 and will have a cost of estimated \$240 per year to maintain and will consume \$3.30 worth of fuel per hour.

The butane engine will cost \$315 and will cost \$315 per year to maintain & will consume \$2.9 worth of fuel per hour of operation.

Since the salvage value of the engine is identical it can be neglected. All other costs associated with the 3 engines are equal and the interest rate is 15%. The service life of each engine is 5 years.

a) Plot the deflated annual cost of each engine as a function of no. of hours of operations/year.

b) Find the range of no. of hours of operation for which it would be most economical to specify the gasoline, diesel & butane engines.

Let  $x$  be the no. of hours of operations of each engine per year.

Let  $\overline{TC}_1$  = Total equivalent annual cost of gasoline engine

$\overline{TC}_2$  = " " " " " diesel engine

$\overline{TC}_3$  = " " " " " butane engine

$$\overline{TC}_1 = 2000 \left( A/P, 15\%, 5 \right) + 200 + 3.6x$$

$$= 796.64 + 3.6x \quad \text{①}$$

$$\overline{TC}_2 = 2800 \left( A/P, 15\%, 5 \right) + 240 + 3.3x$$

$$= 1075.3 + 3.3x \quad \text{②}$$

$$\overline{TC}_3 = 3300 \left( A/P, 15\%, 5 \right) + 315 + 2.9x$$

$$= 1299.5 + 2.9x \quad \text{③}$$

The B.E. b/w the alternatives can be found by equating the alternatives at a time in pairs.

$$\textcircled{1} + \textcircled{2} \quad \overline{TC}_1 = \overline{TC}_2$$

$$796.64 + 3.6x = 1075.3 + 3.3x$$

$$\therefore x = 928.86 = \underline{\underline{929 \text{ hrs}}}$$

$$\textcircled{2} + \textcircled{3} \quad \overline{TC}_2 = \overline{TC}_3$$

$$1075.3 + 3.3x = 1299.5 + 2.9x$$

$$\therefore x = 561 \text{ hrs} \quad \text{Equate } \textcircled{1}$$

$$\textcircled{3} + \textcircled{1} \quad \overline{TC}_3 = \overline{TC}_1$$

$$1299.5 + 2.9x = 796.64 + 3.6x$$

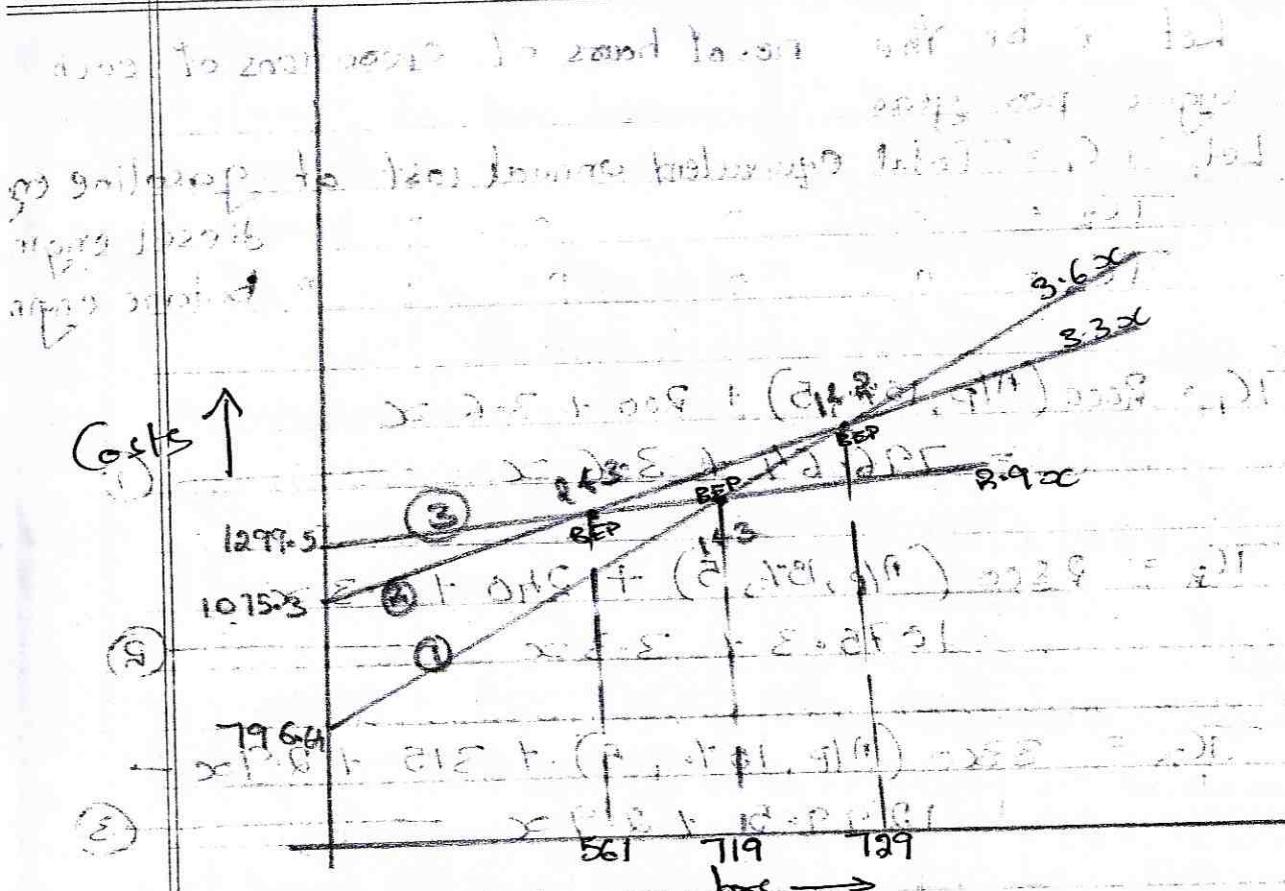
$$\therefore x = 719 \text{ hrs} \quad \text{Equate } \textcircled{2}$$

$$\text{Total Cost} = \frac{2000}{A/P, 15, 5} + 2800 \left( A/P, 15, 8 \right) + \frac{3300}{A/P, 15, 8}$$

$$= 2000 + 22400 + 3000 = 25400 \text{ Rs}$$

$$3.6x = 412 \Rightarrow 3.3x = 368.3 \text{ hrs} \rightarrow \text{match}$$

Total Cost



(d) Upto 719 hrs ; go for alt 1 w/ gasoline

2nd option is with a 12 combustion alt pump 2.

Upto Greatest than 719 hrs go for alt 3 - Butane engine

Don't go for diesel engine (alt 2).

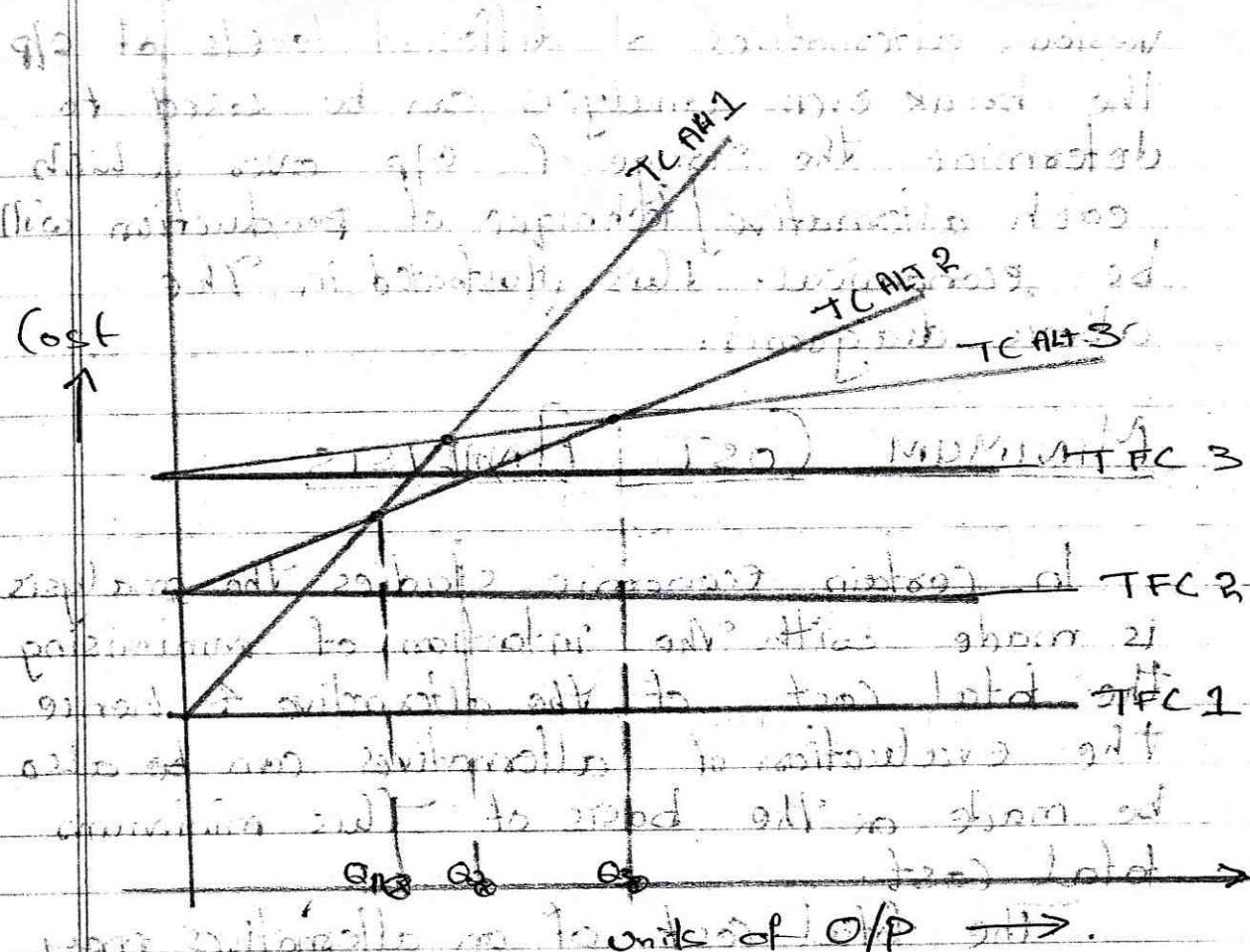
$$\text{2nd P.E.} = 22.2 \text{ P.F.}$$

## COMPARISON OF INVESTMENT ALTERNATIVES

$$\Sigma \text{ P.A.E. P.P.G.I.} = \Sigma \text{ E.S. + E.C.F.O.I.}$$

B.E. analysis can be used for comparing the different alternatives that are available for producing a particular product for achieving a decided objective.

Because ~~Break even~~ in practical practice there may be more than one technique available for producing a particular product. These techniques differ from each other in terms of the costs associated with them at different levels of O/P.



(a) At lower levels of O/P manual operated techniques may be profitable. Since they require minimum FC. With the result, the business B.E. 4 will make a profit at a lower level of O/P. These techniques will not be profitable at higher levels of O/P because of the higher VC.

On the other hand, at higher levels of O/P automation techniques will be more profitable because of the lower variable cost (VC). but they will not be profitable at lower levels of O/P, since they require higher FC. With the result, the business breaks even and makes a profit at a higher vol. of O/P as compared to manual operated MTC's. techniques.

So by solving the costs associated with the