

# Kullback-Leibler (KL) Divergence Retrieval Model

Query Likelihood

$$f(q, d) = \sum_{\substack{w_i \in d \\ w_i \in q}} c(w, q) \left[ \log \frac{p_{\text{Seen}}(w_i | d)}{\alpha_d p(w_i | C)} \right] + n \log \alpha_d$$

KL-divergence  
(cross entropy)

$$f(q, d) = \sum_{w \in d, p(w|\theta_Q) > 0} [p(w | \hat{\theta}_Q) \log \frac{p_{\text{seen}}(w | d)}{\alpha_d p(w | C)}] + \log \alpha_d$$

Query LM

$$p(w | \hat{\theta}_Q) = \frac{c(w, Q)}{|Q|}$$

