Conditional Entropy: Complete Definition

$$\begin{split} & \boldsymbol{H}(\boldsymbol{X}_{meat} \, / \, \boldsymbol{X}_{eats} \,) = \sum_{\mathbf{u} \in \{0,1\}} [p(\boldsymbol{X}_{eats} = \mathbf{u}) \, \, \boldsymbol{H}(\boldsymbol{X}_{meat} \, | \, \boldsymbol{X}_{eats} = \mathbf{u})] \\ & = \sum_{\mathbf{u} \in \{0,1\}} [p(\boldsymbol{X}_{eats} = \mathbf{u}) \, \sum_{\mathbf{v} \in \{0,1\}} [-p(\boldsymbol{X}_{meat} = \mathbf{v} \, | \, \boldsymbol{X}_{eats} = \mathbf{u}) \log_2 p(\boldsymbol{X}_{meat} = \mathbf{v} \, | \, \boldsymbol{X}_{eats} = \mathbf{u})]] \end{split}$$

In general, for any discrete random variables X and Y, we have $H(X) \ge H(X|Y)$

What's the minimum possible value of H(X|Y)?