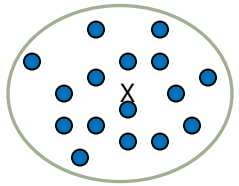
Measures of Cluster: Centroid, Radius and Diameter

- Centroid: $\vec{x}_0$
  - the "middle" of a cluster
  - n: number of points in a cluster
  - $\vec{x}_i$ is the *i*-th point in the cluster



$$\vec{x}_0 = \frac{\sum_i^n \vec{x}_i}{n}$$

- Radius: R
  - Average distance from member objects to the centroid
  - The square root of average distance from any point of the cluster to its centroid

$$R = \sqrt{\frac{\sum_i^n (\vec{x}_i - \vec{x}_0)^2}{n}}$$

- Diameter: D
  - Average pairwise distance within a cluster
  - The square root of average mean squared distance between all pairs of points in the cluster

$$D = \sqrt{\frac{\sum_i^n \sum_j^n (\vec{x}_i - \vec{x}_j)^2}{n(n-1)}}$$