Collapsed Gibbs for LDA

Model

$$p(\theta_d) = \text{Dir}(\beta)$$
 $p(\phi_t) = \text{Dir}(\alpha)$ $p(z_{dn}|\theta_d) = \Theta_{dz_{dn}}$ $p(w_{dn}|z_{dn}, \Phi) = \Phi_{z_{dn}w_{dn}}$

$$p(Z \mid W) \sim \{Gibbs \ Sampling\}$$

$$p(\Phi|W) = \int p(\Phi|W, Z)p(Z|W)dZ$$
$$= \mathbb{E}_{p(Z|W)}p(\Phi|W, Z)$$