

General form of Expectation Maximization

$$\begin{aligned}\log p(X \mid \theta) &= \sum_{i=1}^N \log p(x_i \mid \theta) \\&= \sum_{i=1}^N \log \sum_{c=1}^3 \frac{q(t_i = c)}{q(t_i = c)} p(x_i, t_i = c \mid \theta) \\&\geq \sum_{i=1}^N \sum_{c=1}^3 q(t_i = c) \log \frac{p(x_i, t_i = c \mid \theta)}{q(t_i = c)}\end{aligned}$$

Jensen's inequality

$$\log \left(\sum_c \alpha_c v_c \right) \geq \sum_c \alpha_c \log(v_c)$$