

# Langevin Monte Carlo

Say we want to sample from  $p(w \mid D)$

Start from  $w^0$

For  $k = 1, \dots$

$$w^{k+1} = w^k + \varepsilon \nabla \log p(w^k \mid D) + \eta^k,$$

$$= w^k + \varepsilon \nabla \left( \underbrace{\log p(w^k)}_{\text{Weight decay}} + \sum_{i=1}^N \underbrace{\log p(y_i \mid x_i, w^k)}_{\text{Usual cross entropy}} \right) + \eta^k$$

Weight decay  $-C \|w^k\|^2$

Usual cross entropy

$$\eta^k \sim \mathcal{N}(0, 2\varepsilon I)$$