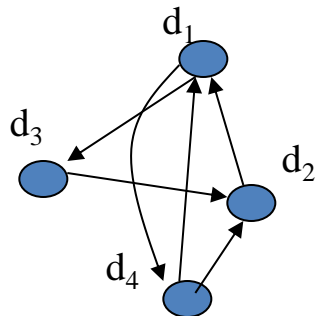


PageRank: Example



$$p(d_j) = \sum_{i=1}^N \left[\frac{1}{N} \alpha + (1 - \alpha) M_{ij} \right] p(d_i)$$

$$\vec{p} = (\alpha I + (1 - \alpha) M)^T \vec{p}$$

$$A = (1 - 0.2)M + 0.2I = 0.8 \times \begin{bmatrix} 0 & 0 & 1/2 & 1/2 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 1/2 & 1/2 & 0 & 0 \end{bmatrix} + 0.2 \times \begin{bmatrix} 1/4 & 1/4 & 1/4 & 1/4 \\ 1/4 & 1/4 & 1/4 & 1/4 \\ 1/4 & 1/4 & 1/4 & 1/4 \\ 1/4 & 1/4 & 1/4 & 1/4 \end{bmatrix}$$

$$\begin{bmatrix} p^{n+1}(d_1) \\ p^{n+1}(d_2) \\ p^{n+1}(d_3) \\ p^{n+1}(d_4) \end{bmatrix} = A^T \begin{bmatrix} p^n(d_1) \\ p^n(d_2) \\ p^n(d_3) \\ p^n(d_4) \end{bmatrix} = \begin{bmatrix} 0.05 & 0.85 & 0.05 & 0.45 \\ 0.05 & 0.05 & 0.85 & 0.45 \\ 0.45 & 0.05 & 0.05 & 0.05 \\ 0.45 & 0.05 & 0.05 & 0.05 \end{bmatrix} \times \begin{bmatrix} p^n(d_1) \\ p^n(d_2) \\ p^n(d_3) \\ p^n(d_4) \end{bmatrix}$$

$$p^{n+1}(d_1) = 0.05 * p^n(d_1) + 0.85 * p^n(d_2) + 0.05 * p^n(d_3) + 0.45 * p^n(d_4)$$

Initial value $p(d)=1/N$, iterate until converge

Do you see how scores are propagated over the graph?