Ordinal Logistic Regression: Rating Prediction

$$p(r \geq j \mid X) \geq 0.5 \Leftrightarrow \frac{e^{\alpha_j + \text{score}(X)}}{e^{\alpha_j + \text{score}(X)} + 1} \geq 0.5 \Leftrightarrow \text{score}(X) \geq -\alpha_j$$

$$\text{Rating} \qquad \text{score}(X) = \sum_{i=1}^{M} \beta_i X_i$$

$$k-1 \qquad \text{Classifier 1} \qquad -\alpha_k \qquad r=k$$

$$k-2 \qquad \text{Classifier 2} \qquad -\alpha_{k-1} \qquad r=k$$

$$\text{Classifier k-1} \qquad -\alpha_2 \qquad r=1$$

$$r=j \Leftrightarrow \text{score} \in [-\alpha_i, -\alpha_{i+1}), \text{ define } \alpha_1 = \infty, \alpha_{k+1} = -\infty$$