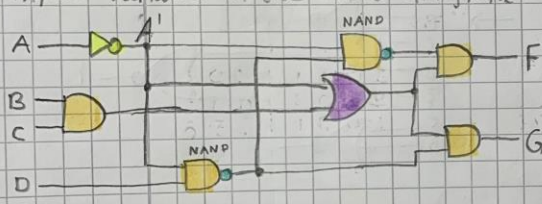


Darmassamitur 4

4.2 Obtain the simplified Boolean expression for output F and G in terms of the input variables in the circuit of Fig. 04.2



$$\begin{aligned} F &= (\overline{A+D})(\overline{A})(\overline{A+BC}) = (A+\overline{D})(\overline{A})(\overline{A+BC}) \\ &= (A+\overline{D})(\overline{A})(\overline{A}+\overline{BC}) \\ &= (A+\overline{D})(\overline{A})(\overline{A}+\overline{B}+\overline{C}) \\ &= (\overline{A}\overline{A} + \overline{A}\overline{B} + \overline{A}\overline{C} + \overline{D}\overline{A}\overline{B} + \overline{D}\overline{A}\overline{C}) \end{aligned}$$

$$G_1 = (\overline{A}D)(\overline{A} + B)$$

$$= (A + D)(\bar{A} + BC)$$

$$= \cancel{A}A + ABC + \bar{A}D + B\bar{C}D$$

$$= ABC + \bar{A}D + BCD$$

$$G_1 = \underline{\underline{ABC}}$$

$$= 0 + ABC + 0 + ABC\bar{D}$$

$$= ABC + ABC\bar{D}$$

1	1	1	%	1	1	1	0
---	---	---	---	---	---	---	---

Handwritten Karnaugh map for a 4-variable function with variables A, B, C, and D. The map is a 4x4 grid with rows labeled AB (00, 01, 11, 10) and columns labeled CD (00, 01, 11, 10). The cells contain 1s and 0s, with some cells highlighted by yellow and blue boxes.

AB \ CD	00	01	11	10
00	0	1	1	0
01	0	1	1	1
11	1	1	1	1
10	1	1	1	1

The yellow box highlights the cells (00,01), (01,01), (11,01), and (10,01). The blue box highlights the cells (01,11), (11,11), (01,10), and (11,10).

$$F = \bar{A}\bar{C}D + BC$$

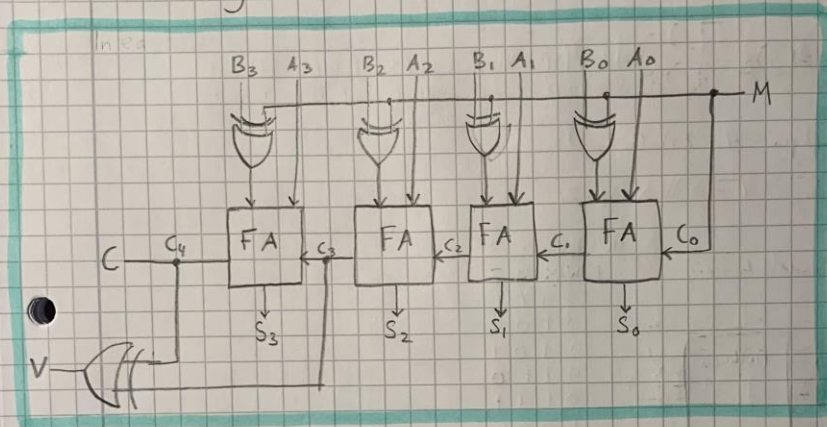
1B

00	01	11	10
00	01	11	10
01	01	11	10
11	11	11	11
10	10	10	10

4.13 The adder-subtractor circuit of Fig 4.13 has the following values for mode input M and data inputs A and B.

	M	A	B
a)	0	0111	0110
b)	0	1000	1001
c)	1	1100	1000
d)	1	0101	1010
e)	1	0000	0001

In each case, determine the values of the four SUM outputs, the carry C, and overflow V.



SUM(A ⊕ B)

NB = FA = Full-Adder

$S = A \oplus B$

$C = AB + \bar{A}B$

a)
$$\begin{array}{r} 0111 \\ + 0110 \\ \hline 1101 \end{array}$$
 C = 0
V = 1

$V_{MAX} = (8) 1000$

b)
$$\begin{array}{r} 1000 \\ + 1001 \\ \hline 10001 \end{array}$$
 C = 1
V = 0

$$\begin{array}{r} 0110001 \\ 06110101 \\ \hline 00611001 \\ 01001110 \end{array}$$
 C = 0
V = 0

c)
$$\begin{array}{r} 1100 \\ + 1000 \\ \hline 10100 \end{array}$$
 C = 1
V = 0

dec
53
+ 91
144

$$\begin{array}{r} 1111111 \\ 00110101 \\ 01011011 \\ \hline 10010000 \end{array}$$
 C = 0
V = 1

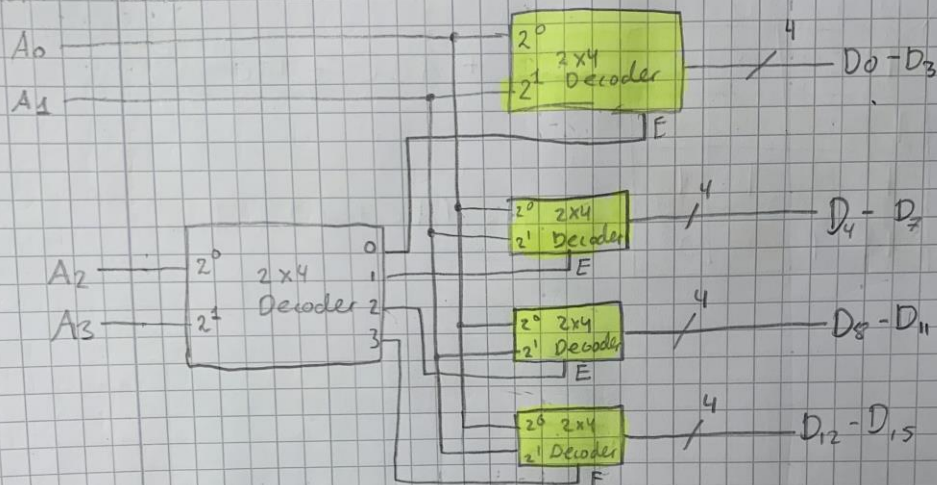
d)
$$\begin{array}{r} 0101 \\ + 1010 \\ \hline 1111 \end{array}$$
 C = 0
V = 1

$$\begin{array}{r} 11 \\ 0110 \\ + 0010 \\ \hline 1000 \end{array}$$

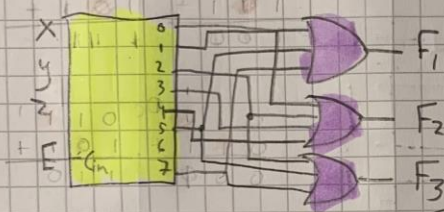
e)
$$\begin{array}{r} 0000 \\ + 0001 \\ \hline 0001 \end{array}$$
 C = 0
V = 0

Thinking signed we added two positive numbers.

4.26 Construct a 4-to-16-line decoder with 2-to-4-line decoders with enable.



4.28 b) $F_1 = (\bar{y} + x)z = \bar{y}z + xz = \bar{y}z(x + \bar{x}) + xz(y + \bar{y}) = \bar{x}\bar{y}z + \bar{x}y\bar{z} + x\bar{y}z + xy\bar{z} = \Sigma(0, 2, 3, 4, 6)$
 $F_2 = \bar{y}z + \bar{x}y + y\bar{z} = \Sigma(0, 2, 3, 4, 6) + \bar{x}y\bar{z} + x\bar{y}z = \Sigma(1, 5, 7)$
 $F_3 = (x + y)z = xz + yz = x(y + \bar{y})z + (\bar{x} + x)y\bar{z} = x\bar{y}z + xy\bar{z} + \bar{x}y\bar{z} + x\bar{y}z = \Sigma(2, 5, 7)$



4.28

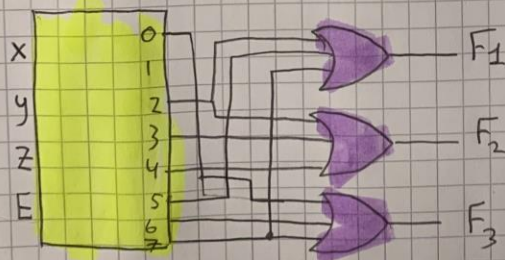
010 111

a) $F_1 = \bar{x}y\bar{z} + xz = \bar{x}y\bar{z} + x\bar{y}z = 010 + 111 = \Sigma(2, 5, 7)$

$F_2 = x\bar{y}z + xy = \bar{x}\bar{y}z + \bar{x}y\bar{z} = 010 + 101$

$F_2 = x\bar{y}z + \bar{x}y = \bar{x}\bar{y}z + \bar{x}y\bar{z} + \bar{x}y\bar{z} = \Sigma(2, 3, 4)$

$F_3 = \bar{x}\bar{y}\bar{z} + xy = \bar{x}\bar{y}\bar{z} + \bar{x}y\bar{z} + \bar{x}y\bar{z} = \Sigma(0, 6, 7)$



4. A1

	A	B	C	D	F
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	1
3	0	0	1	1	0
4	0	1	0	0	0
5	0	1	0	1	1
6	0	1	1	0	1
7	0	1	1	1	0
8	1	0	0	0	1
9	1	0	0	1	0
10	1	0	1	0	0
11	1	0	1	1	0
12	1	1	0	0	1
13	1	1	0	1	1
14	1	1	1	0	0
15	1	1	1	1	1

$$F = 1$$

$$F = \bar{D}$$

$$F = D$$

$$F = \bar{D}$$

$$F = \bar{D}$$

$$F = 0$$

$$F = 1$$

$$F = D$$

$$A = S_0$$

$$B = S_1$$

$$C = S_2$$

