

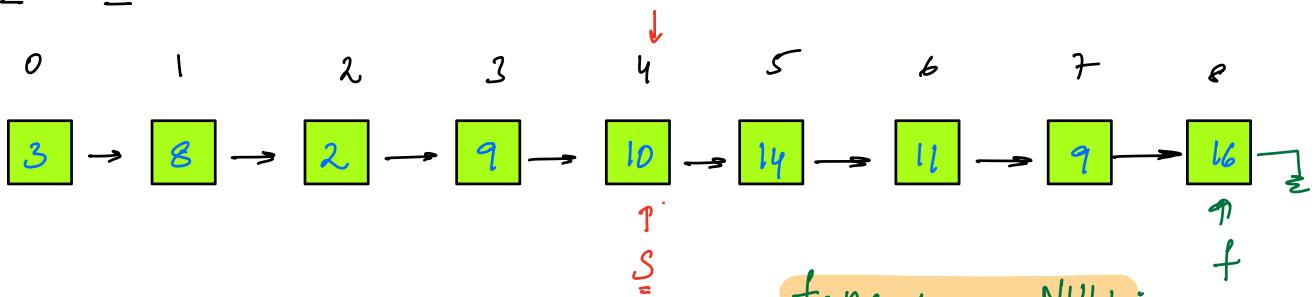
Today's Content:

- Find Middle ✓
- Merge 2 sorted arrays ✓ → using dummy node
- Merge Sort / Merge N Sorted Links → ✓
- Re-arrange → { TODO } → Assignment
- Cycle detection ✓
- Loop detection → { Proof in Doubts Session }

Find Middle

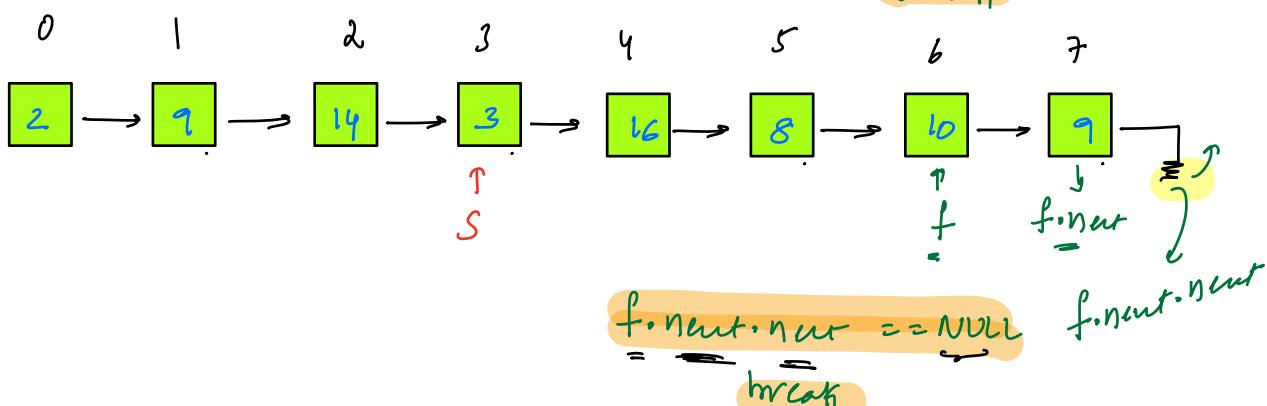
Fast point \rightarrow 2 steps

Slow point \rightarrow 1



f.next == NULL:

break



Sol1

1 Given linked list

if $N = \text{size}(\text{head})$, $N >= 1$

1. If $\left\{ \begin{array}{l} \text{get } k^{\text{th}} \text{Elem}(\text{head}, \frac{N}{2}) \\ \text{get } k^{\text{th}} \text{Elem}(\text{head}, \frac{N-1}{2}) \end{array} \right\} \Rightarrow c_2$

2 Iterations

Q) If odd get center

If even get c_1 center

Note: In a single iteration

Idea

$\left\{ \begin{array}{l} \text{if: } n \\ \text{if: } 2n \end{array} \right\} : d$

Node center(Node h) {

 if (h == NULL) { return h; }

 Node f = h;

 Node s = h;

 while (f.next != NULL || f.next.next != NULL) {

 s = s.next;

 f = f.next.next;

 return s;

Edge or

Case
working

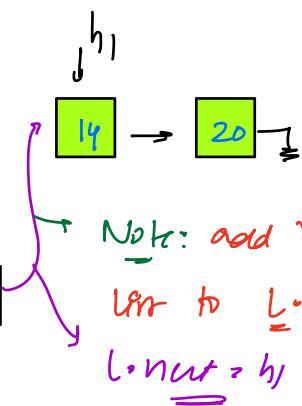
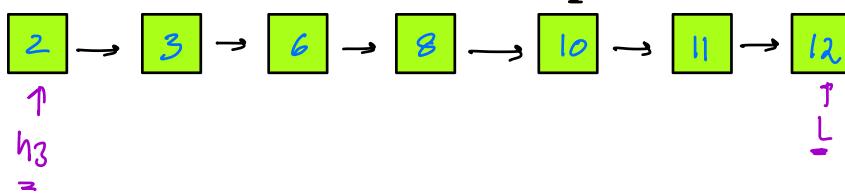
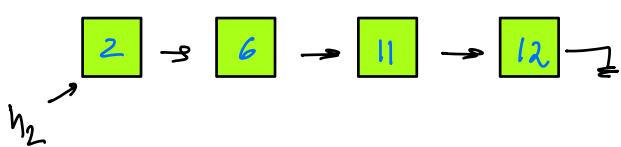
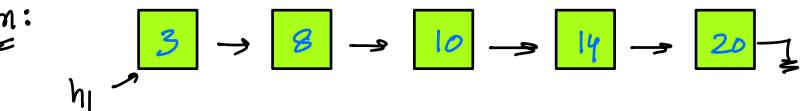
$h \rightarrow \boxed{\quad} \rightarrow \dots$

$h \rightarrow \boxed{\quad} \rightarrow \boxed{\quad} \rightarrow \dots$

Merge 2 Sorted Linked Lists

} return a single sorted linked list
 No Extra Space, only re-arrangement

Ex:



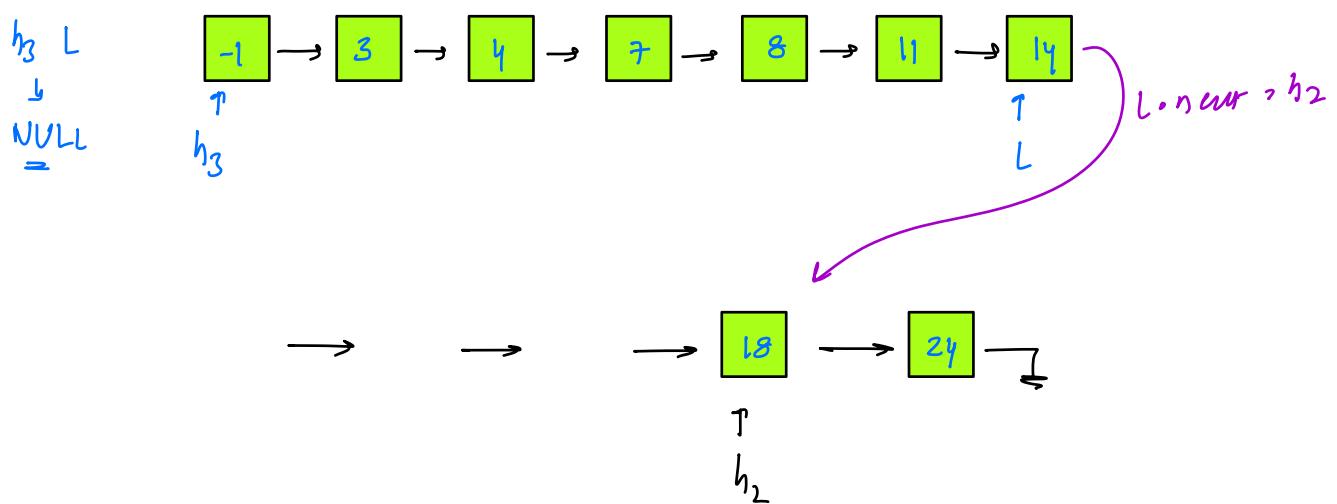
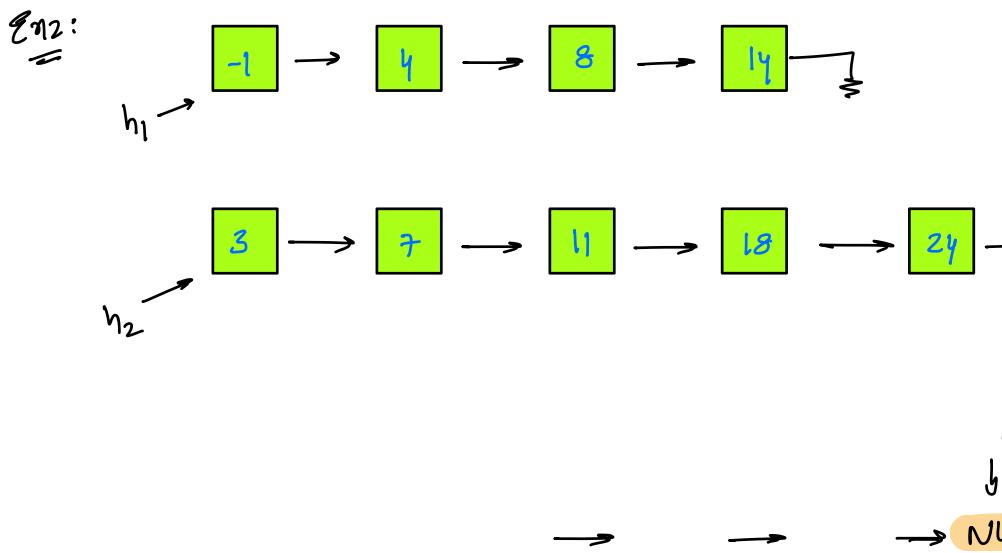
Note: add remaining
 list to L
 $L \leftarrow L \cup h_1$



if ($h_1.data < h_2.data$) { on ?

Add h_1 at back
 $L.next = h_1$
 $h_1 = h_1.next$
 $L = L.next$

Add h_2 at back
 $L.next = h_2$
 $h_2 = h_2.next$
 $L = L.next$



Note: Avoid usage of dummy node.

{ Even tho it's a single node, if we run
 same function N Times it will create
 N dummy nodes }

Merge (Node h₁, Node h₂) {

If (h₁ == NULL) { return h₂ } Edge Case

If (h₂ == NULL) { return h₁ }

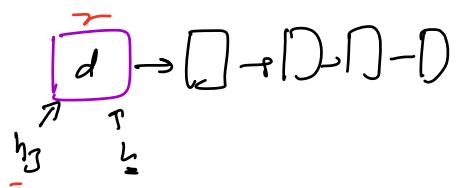
{ Node h₃ = NULL, L = NULL }

If (h₁.data < h₂.data) { h₃ = h₁, L = h₁, h₁ = h₁.next }

else { h₃ = h₂, L = h₂, h₂ = h₂.next }

or

Node h₃ = new Node (-1);
L = h₃



while (h₁ != NULL && h₂ != NULL) {

If (h₁.data < h₂.data) { Add h₁ at back }

else { Add h₂ at back }

// Adding remaining part

If (h₂ != NULL) { L.next = h₂ }

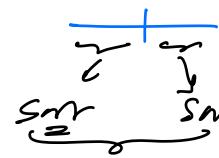
else { L.next = h₁ }

// return head of sorted linked list

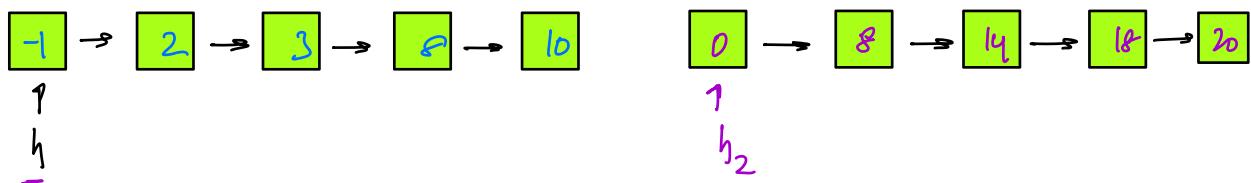
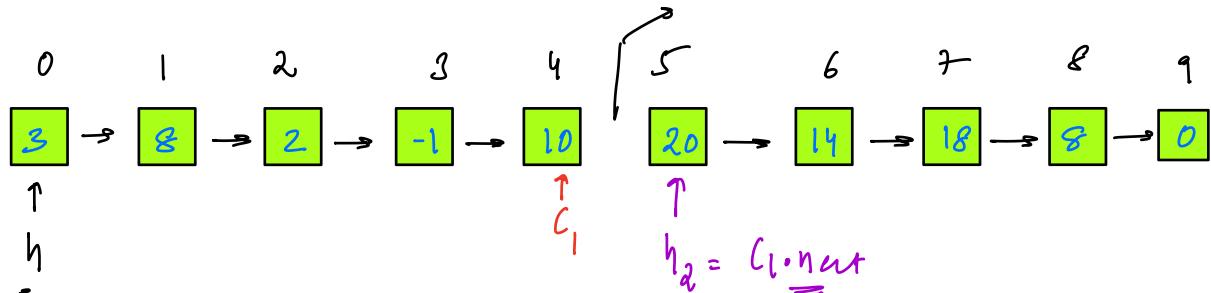
return h₃ // if we are using dummy node

return h₃.next

Merge Sort



Sort \Rightarrow Sort \Rightarrow merge break $c_1.\text{next} = \text{NULL}$



```
Node    mergeSort(Node h) {   SC = O(1) ↳ O(1)
```

if ($h == \text{NULL}$) { return h }

if ($h.\text{next} == \text{NULL}$) { return h }

Node $c_1 = \text{centre}(h);$

Node $h_2 = c_1.\text{next}$

$c_1.\text{next} = \text{NULL}$

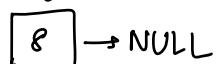
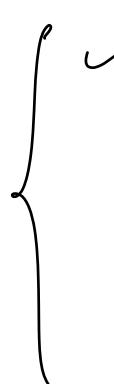
$h = \text{mergeSort}(h)$

$h_2 = \text{mergeSort}(h_2)$

return $\text{merge}(h, h_2)$

Leave Recursion stack
linked list edge case
No Element, 1 Element, 2 Elements
loop overflow
stack overflow

1) No Element, 1 Element, 2 Elements



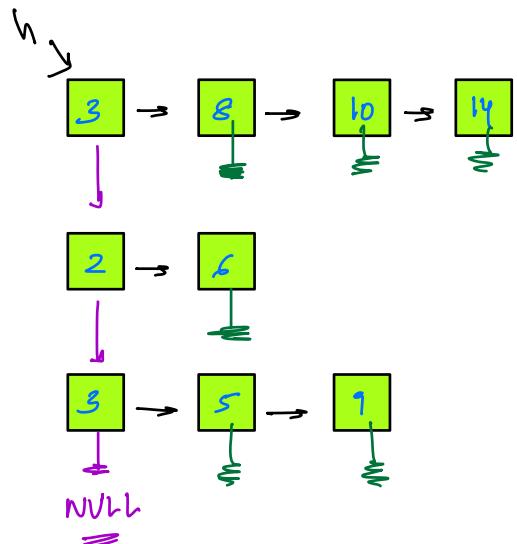
$h =$ c $h_2 = \text{NULL}$

$\text{mergeSort}(h) \rightarrow [8] \rightarrow \text{NULL}$

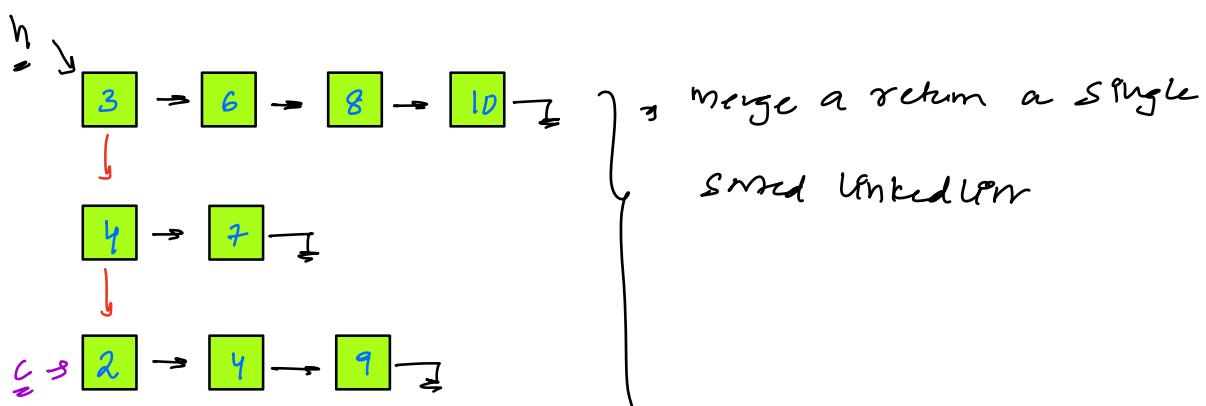
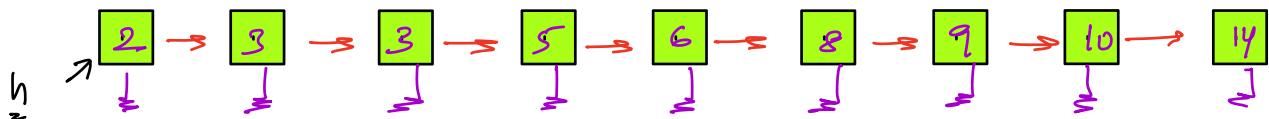
$\text{mergeSort}(h_2) \rightarrow \text{NULL}$

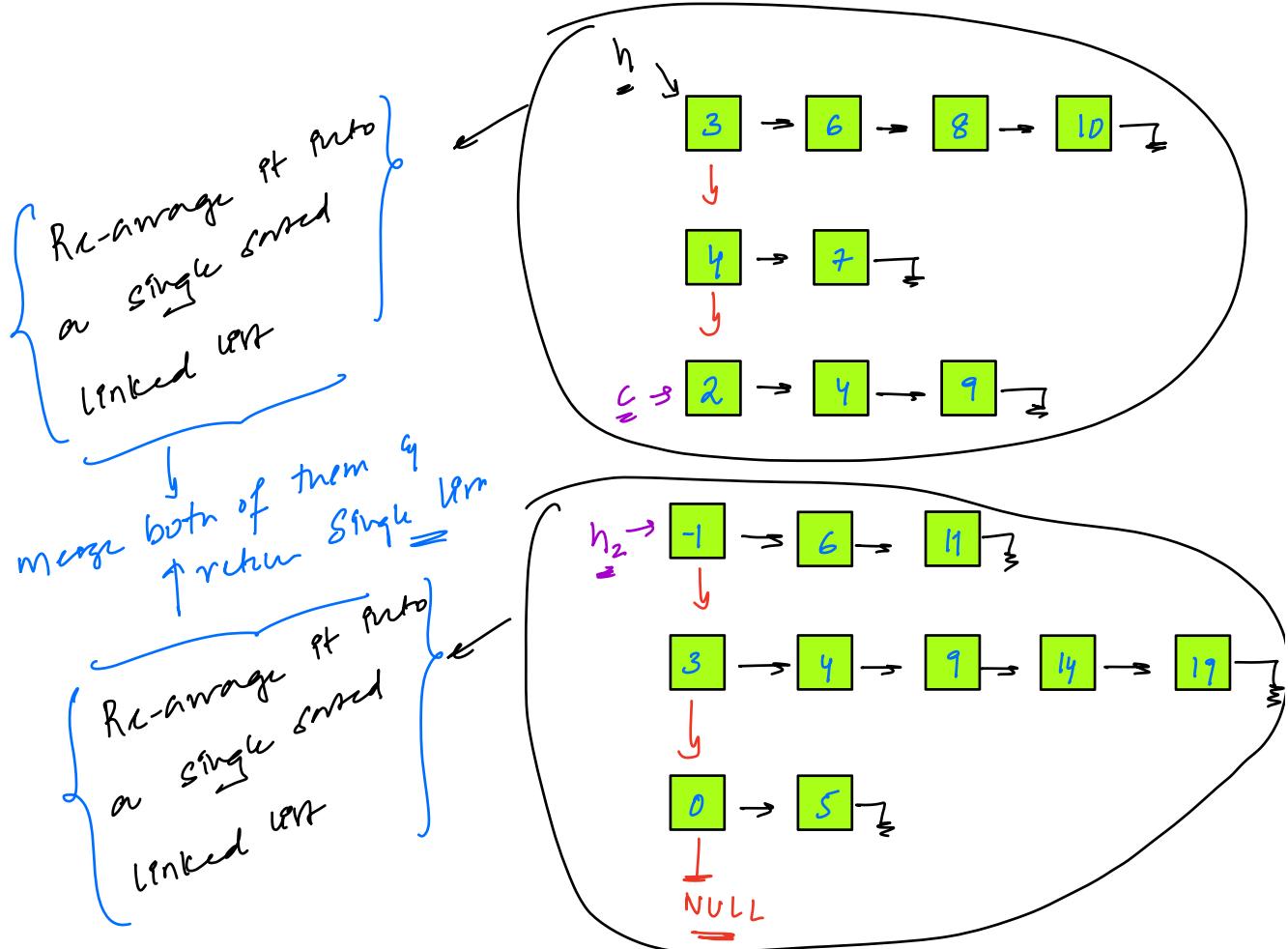
Q8 Given N Sorted Linked Lists merge all of Them.

```
class Node {
    int data;
    Node right;
    Node down;
    Node(int n) {
        data = n;
        right = down = null;
    }
}
```



Sol: → Flatten Sorted Linked List





```

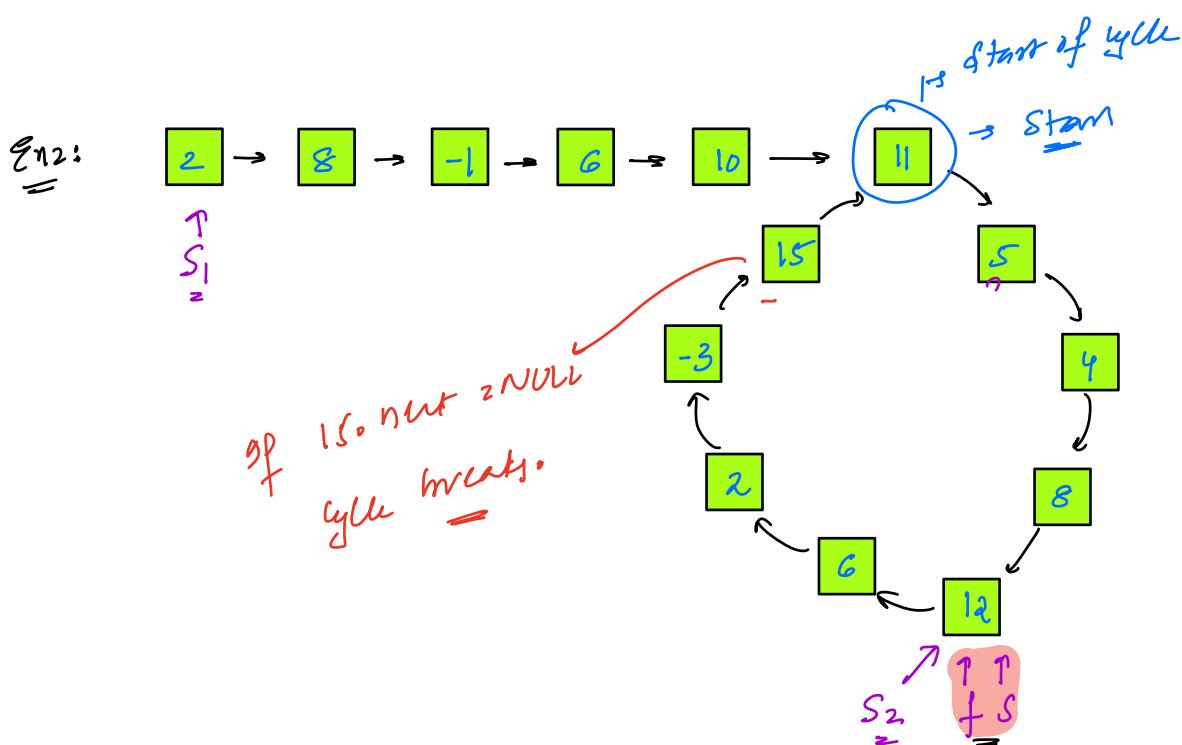
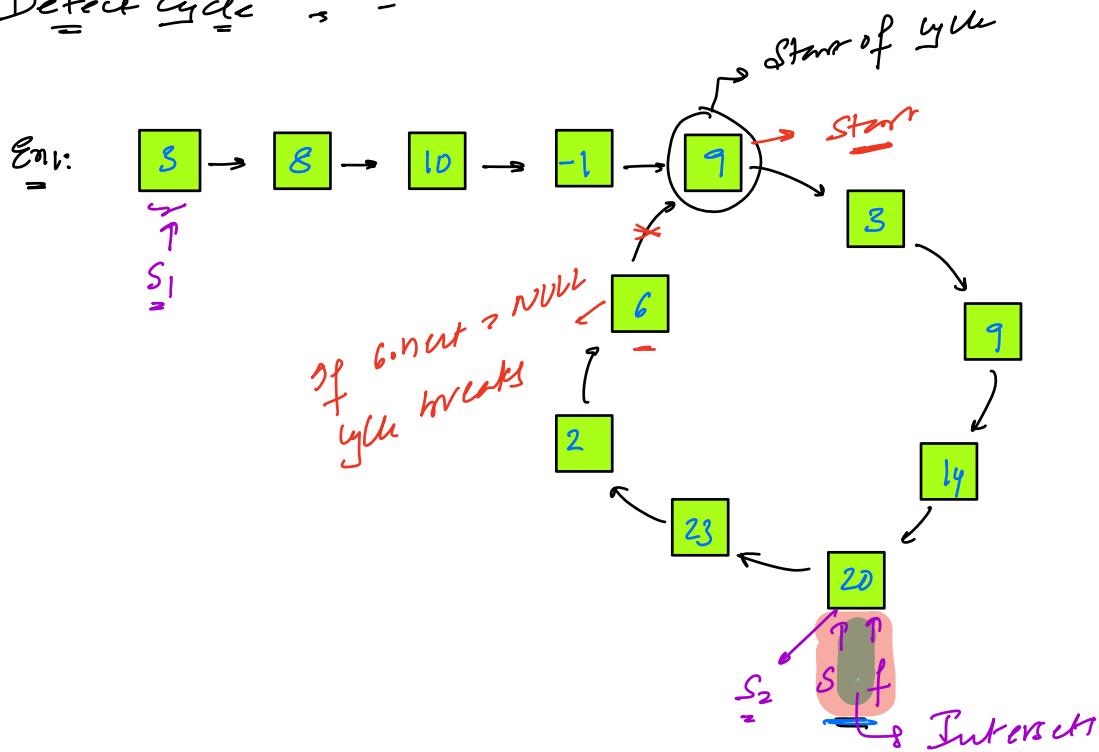
// Merge N Srt( Node h) {
  if (h == NULL || h.down == NULL) { return h }

  Node c = center(h)           using down reference

  Node h2 = c.down
  c.down = NULL
  h = mergeNSrt(h)
}

h2 = mergeNSrt(h2)             using right reference
return merge(h, h2)
  
```

Detect Cycle \Rightarrow -



Approach 1: Store all references in hashset?

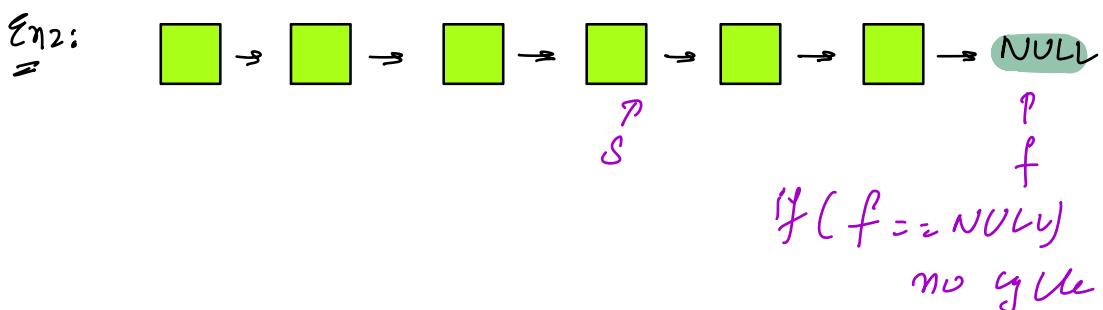
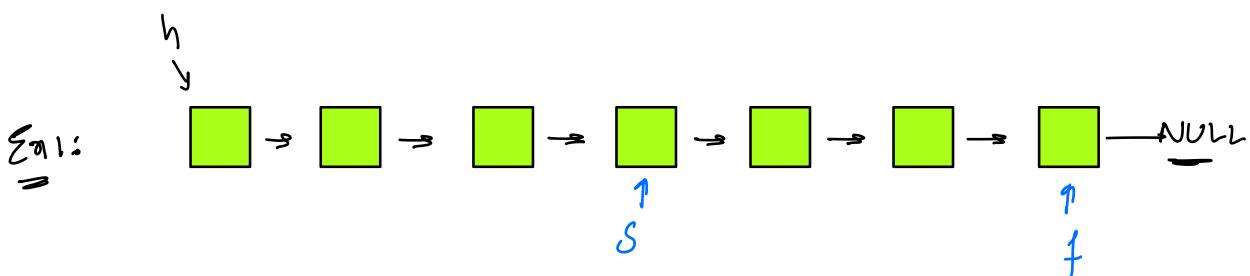
TC: $O(N)$ SC: $O(N)$

↓ {
 ⇒ If we insert same address 2 times?
 ⇒ Cycle is present
 { If we incur **temp = NULL**
 Cycle is not present
 }
 }
 } Hashset & Node
 } How to store Node
 reference in your
 language of choice?

Approach 2: $s = h, f = h$

If there is a cycle **$s == f$**

If **$f == NULL \wedge f.next == NULL$** : no cycle



Detect Cycle (Node h) {

// TODO

→ check cycle there or not? ✓

→ If cycle is there ✓

⇒ You have to get start of cycle ?

→ $S_1 = h$, $S_2 = (\text{keep at intersection})$

update both slow pointer till they are same

They will meet at start of cycle

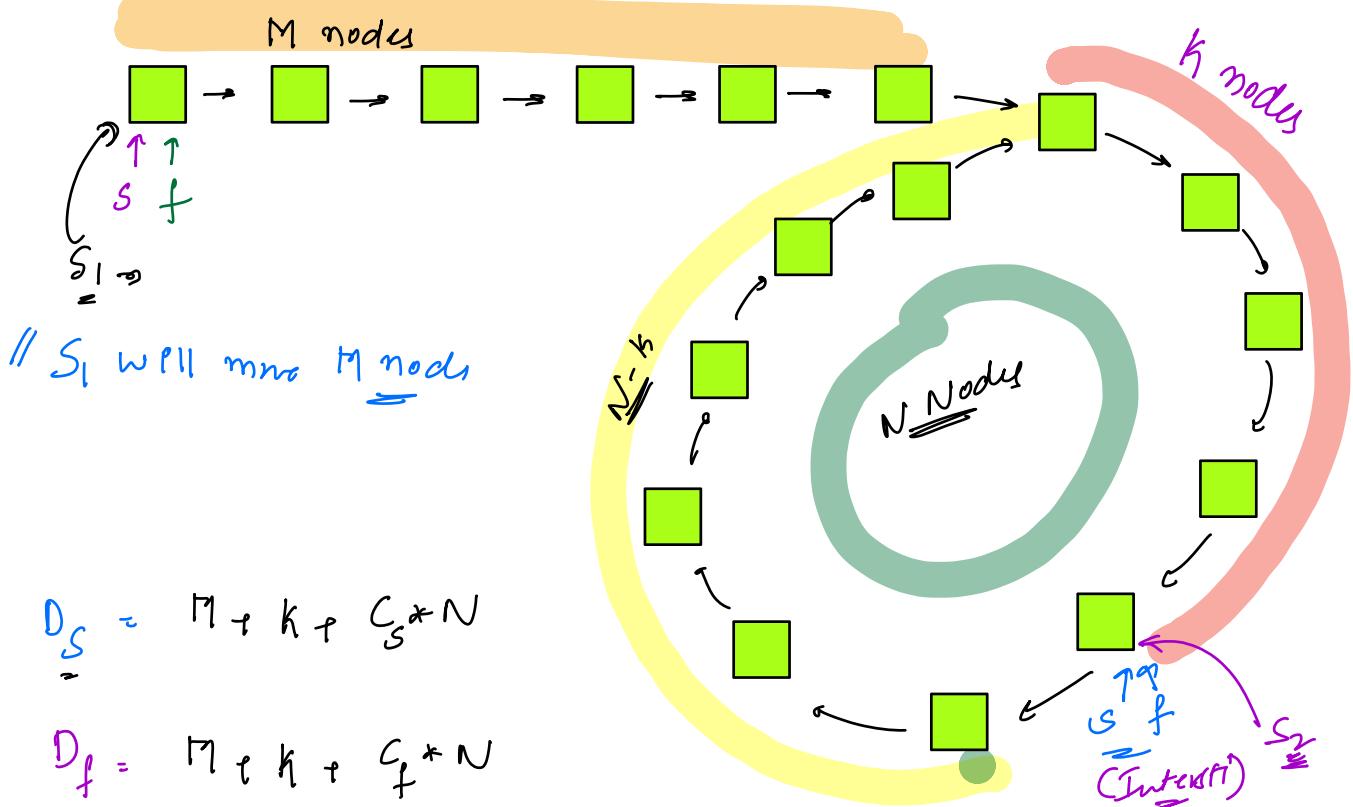
→ You need to remove the cycle?

Pivote & get node whom

node.next = Start of cycle

{
node.next = NULL to
remove cycle

Proof of Concept \Rightarrow Explain from Starky



$$D_S = M + k + C_S \cdot N$$

$$D_f = M + k + C_f \cdot N$$

$$D_f = 2 D_S$$

$$(M + k + C_f \cdot N) = 2(M + k + C_S \cdot N)$$

$$\cancel{M} + \cancel{k} + \cancel{C_f N} = \cancel{2M} + \cancel{2k} + 2C_S N$$

$$C_f N - 2C_S N - k = M$$

$$(N)(C_f - 2C_S) - k = M$$

$$T_1 = (N)(C_f) - k$$

$$M = (C_f - 2C_S) + (N - k)$$

S_2 is at inflection + $(N - k)$

' finally both S_1 & S_2 are meeting at start