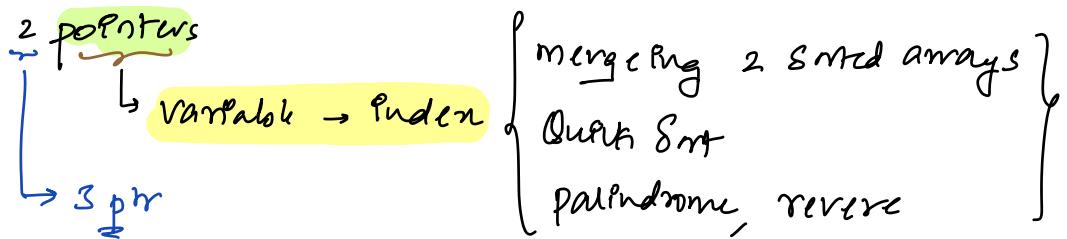


## Today's Content:



- Where to initialize
- How to update
- When to stop

18) Given  $N$  distinct sorted elements, Check if there exists a pair  $(i, j)$ ,  $\text{ar}[i] + \text{ar}[j] = k$ . Return T/F ( $i \neq j$ )

2 indices

Ex1:  $\text{ar}[5] \Rightarrow \{3, 7, 8, 12, 19\} \quad k = 15$

Ex2:  $\text{ar}[5] = \{2, 5, 8, 11, 15\} \quad k = 16$

$a=2$   
 $b=14 \times$

Solutions

1) Check all pairs

$T.C.: O(N^2) \quad S.C.: O(1)$

$\text{ar}[11] = \{ -3, 0, 1, 3, 6, 8, 11, 14, 18, 25 \} \quad k = 17$

$a = -3$

2) Using HashSet/Map

$T.C.: O(N) \quad S.C.: O(N)$

$P = 0; q < N; P++ \}$

$a = \text{ar}[P]$

$b = k - a;$

Apply RS get  $b$

$T.C.: O(N \log N) \quad S.C.: O(1)$

$P_1 \quad P_2 \quad \text{sum} = \text{ar}[P_1] + \text{ar}[P_2]$

$0 \quad 9 \quad 22 > 17 \quad \} \text{decrease sum, } P_2--$

$0 \quad 8 \quad 15 < 17 \quad \} \text{increase sum, } P_1++$

$1 \quad 8 \quad 18 > 17 \quad \} \text{dec, } P_2--$

$1 \quad 7 \quad 14 < 17 \quad \} \text{inc, } P_1++$

$2 \quad 7 \quad 15 < 17 \quad \} \text{inc, } P_1++$

$3 \quad 7 \quad 17 == 17 \quad \} (\text{return True})$

bool check(int arr[], int N, int k) {

    P<sub>1</sub> = 0, P<sub>2</sub> = N-1

    while (P<sub>1</sub> < P<sub>2</sub>) {

        if (arr[P<sub>1</sub>] + arr[P<sub>2</sub>] == k) {

            return True

        else if (arr[P<sub>1</sub>] + arr[P<sub>2</sub>] > k) {

            P<sub>2</sub> --

        else {

            P<sub>1</sub> ++

    return False

T: O(N) SC: O(1)

Ex:

arr[5] = 3 18 21 9 10



P<sub>1</sub>

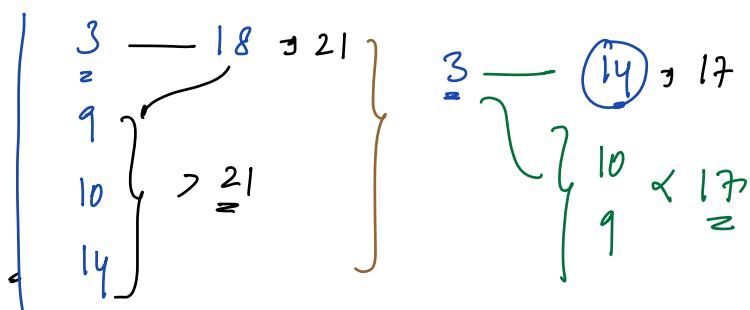
14 21 18

P<sub>2</sub>

k = 19

21 > 19, P<sub>2</sub> --

17 < 19, P<sub>1</sub> ++



28) Given  $N$  distinct sorted elements. Check if there exists a pair  $(i, j)$ , such that  $\text{ar}[j] - \text{ar}[i] = k$  &  $k > 0$  eq ( $i < j$ )

	0	1	2	3	4	5	6	7	8	9	$\} k=5$
$\text{ar}[N]$	-3	0	1	3	6	8	11	14	18	25	
$\downarrow$	=	=	=	=	=	=	=	=	=	=	
$N=10$											

Initialize pointers

$$\begin{array}{ccc} P_1 & \xrightarrow{\quad} & P_2 \\ 0 & & n-1 \\ \downarrow & & \downarrow \\ 0 & & 9 \end{array} \quad \text{Diff} = \text{ar}[P_2] - \text{ar}[P_1]$$

We cannot make  
a decrem

\* Incorrect

$$\begin{array}{c} P_2-- \\ \hline P_1++ : \text{diff decreas} \end{array}$$

$$\begin{array}{ccc} P_1 & \xrightarrow{\quad} & P_2 \\ 0 & & n/2 \\ \downarrow & & \downarrow \\ 0 & & 5 \end{array} \quad \text{Diff} = \text{ar}[P_2] - \text{ar}[P_1]$$

11 decre

$\left\{ \begin{array}{l} P_2-- \\ P_1++ \end{array} \right.$

$$\begin{array}{ccc} P_1 & \xrightarrow{\quad} & P_2 \\ n/2 & & n/2+1 \\ \downarrow & & \downarrow \\ 5 & & 6 \end{array} \quad \text{Diff} = \text{ar}[P_2] - \text{ar}[P_1] \quad k=5$$

$3 < 5$  Inc

$\left\{ \begin{array}{l} P_2++ \\ P_1-- \end{array} \right.$

Inc diff

$$\begin{array}{ccc} P_1 & \xrightarrow{\quad} & P_2 \\ N-2 & & N-1 \\ \downarrow & & \downarrow \\ \text{if } \text{ar}[P_2] - \text{ar}[P_1] < k \\ \text{increas diff} \\ P_1-- \\ \downarrow \\ \text{or if } \text{ar}[P_2] - \text{ar}[P_1] > k \\ \text{decreas diff} \\ P_2-- \end{array}$$

	0	1	2	3	4	5	6	7	8	9	$\sum k=5$
$ar[N]$	-3	0	1	3	6	8	11	14	18	25	

$P_1$        $P_2$

$$P_1 \quad P_2 \quad (ar[P_2] - ar[P_1])$$

0 1 :  $3 < 5$  : Inc  $\Rightarrow P_2++$

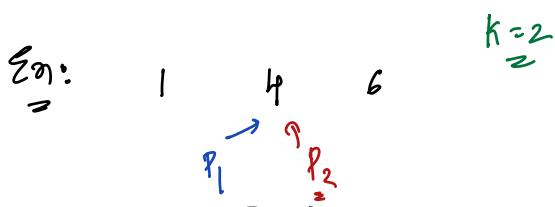
0 2 :  $4 < 5$  : Inc  $\Rightarrow P_2++$

0 3 :  $6 > 5$  : dec  $\Rightarrow P_1++$

1 3 :  $3 < 5$  : Inc  $\Rightarrow P_2++$

1 4 :  $6 < 5$  : dec  $\Rightarrow P_1++$

2 4 :  $5 \leq 5$  : return True



$P_1$	$P_2$	$ar[P_2] - ar[P_1]$
0	1	$3$ decrement, $P_1++$
1	1	$P_2++$
1	2	(return True)

Pseudocode  $\rightarrow$  Pseudocode :  $k \geq 0$   
 $k = \text{abs}(k)$

$$P_1 = 0, \quad P_2 = 1 \quad \text{nonced}$$

while ( $P_1 \leq N$  &&  $P_2 \leq N$ )

if ( $ar[P_2] - ar[P_1] \geq k$ ) {  
 |  
 | return True  
 |}  
 } un if ( $ar[P_2] - ar[P_1] > k$ ) {

$P_1++$   
 if ( $P_1 == P_2$ ) { $P_2++$ }  
 } else  
 |  
 |  
 |  
 | $P_2++$

TC:  $O(CN)$

SC:  $O(1)$

return False

$$\left. \begin{array}{l} 10 \quad 3 \Rightarrow 10 - 3 = 7 \\ \Rightarrow 3 - 10 = -7 \\ ar[f] - ar[g] = 15 \\ ar[p] - ar[j] = -15 \end{array} \right\} \begin{array}{l} 8 \\ -8 \end{array}$$

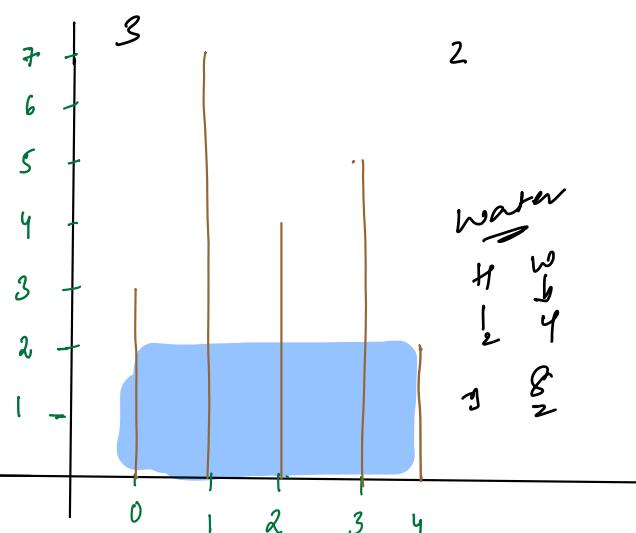
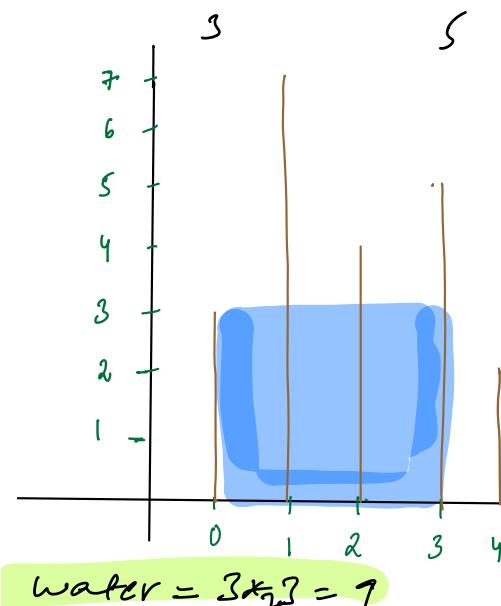
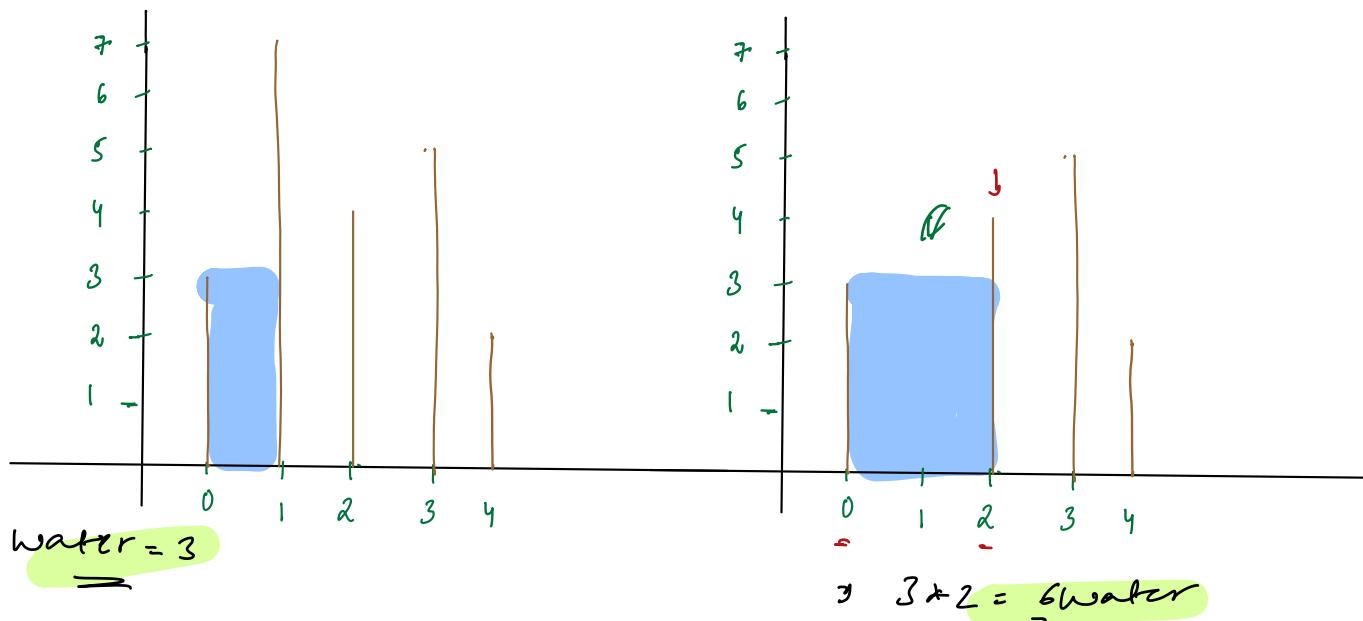
30) Given N array elements,

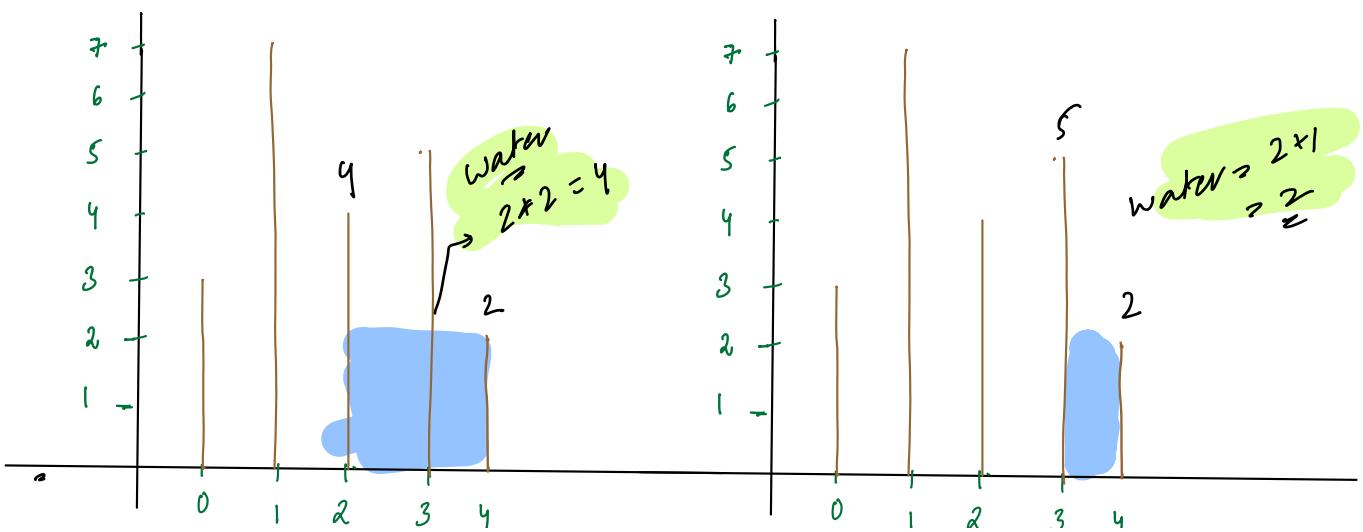
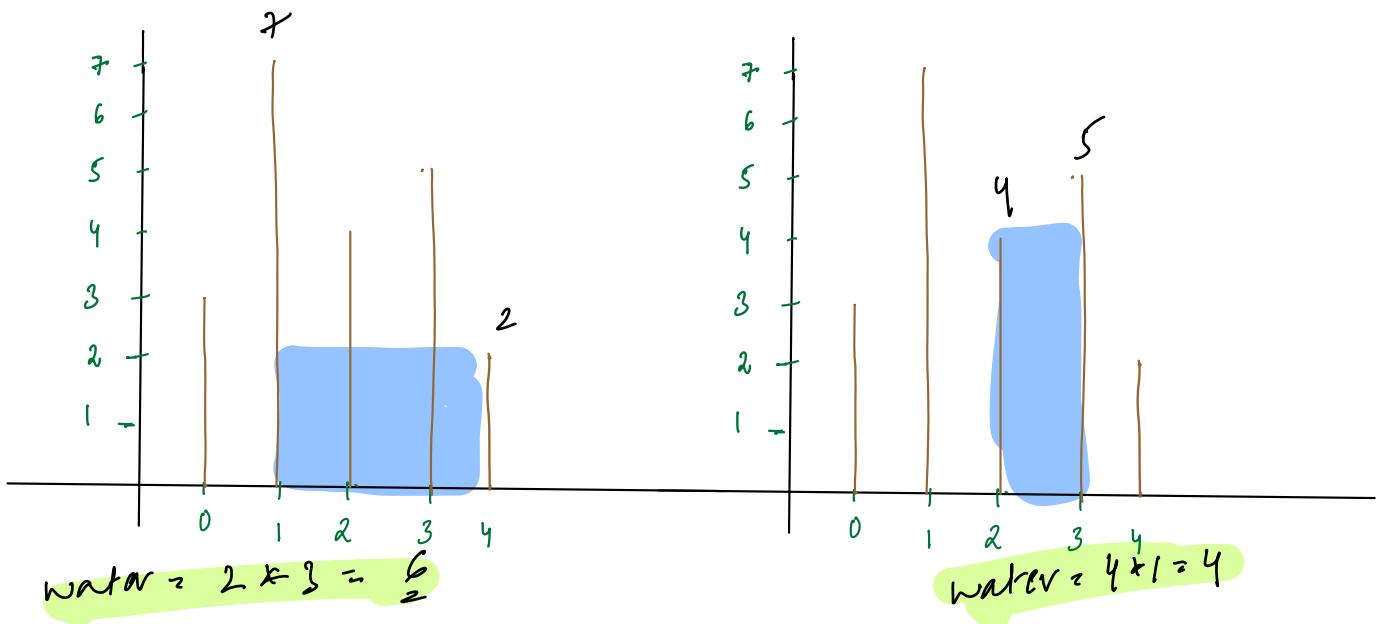
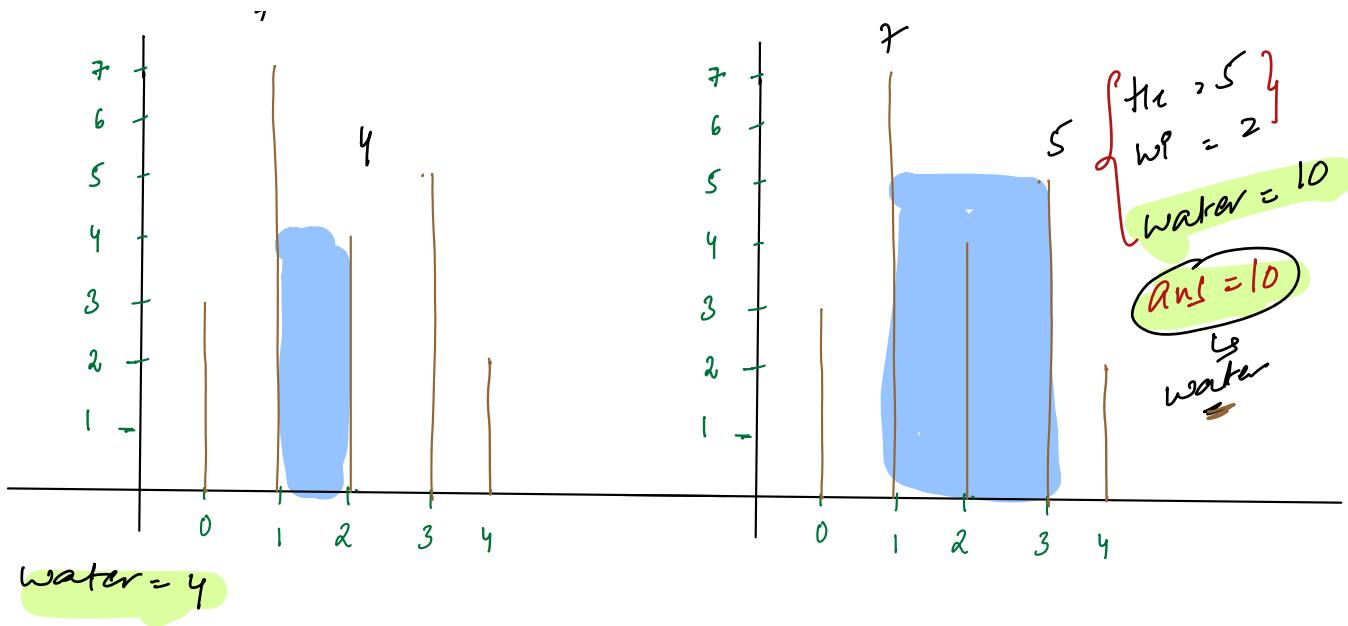
Where each  $arr[i]$  represents height of each wall

Pick any 2 walls such that max water is accumulated  
between them.

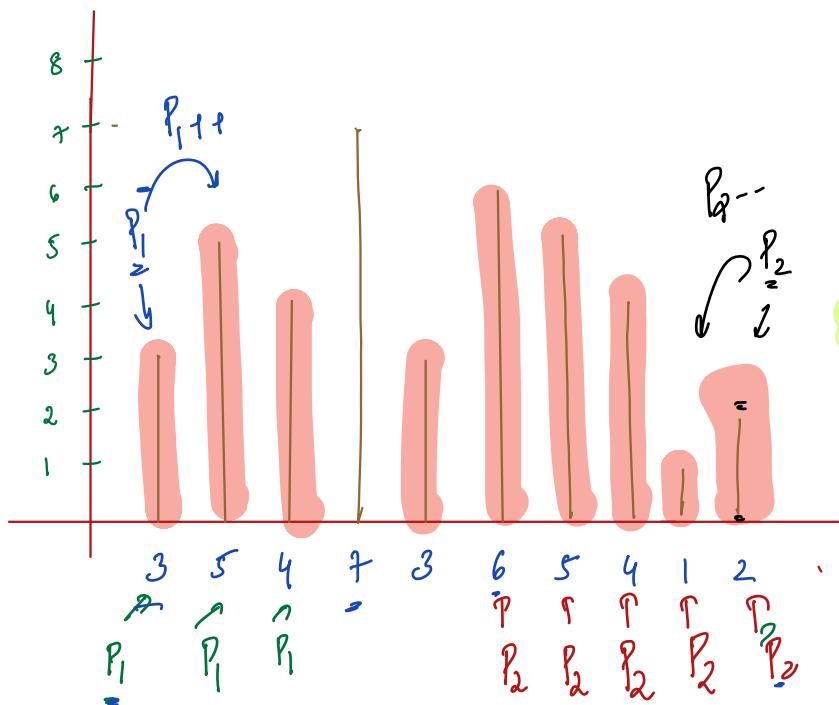
→ long streak

$$\text{Ex1: } \{ 3, 7, 4, 5, 2 \}$$





$$ar[10] = \{ 3, 5, 4, 7, 3, 6, 5, 4, 1, 2 \}$$



$\Rightarrow$  obs:

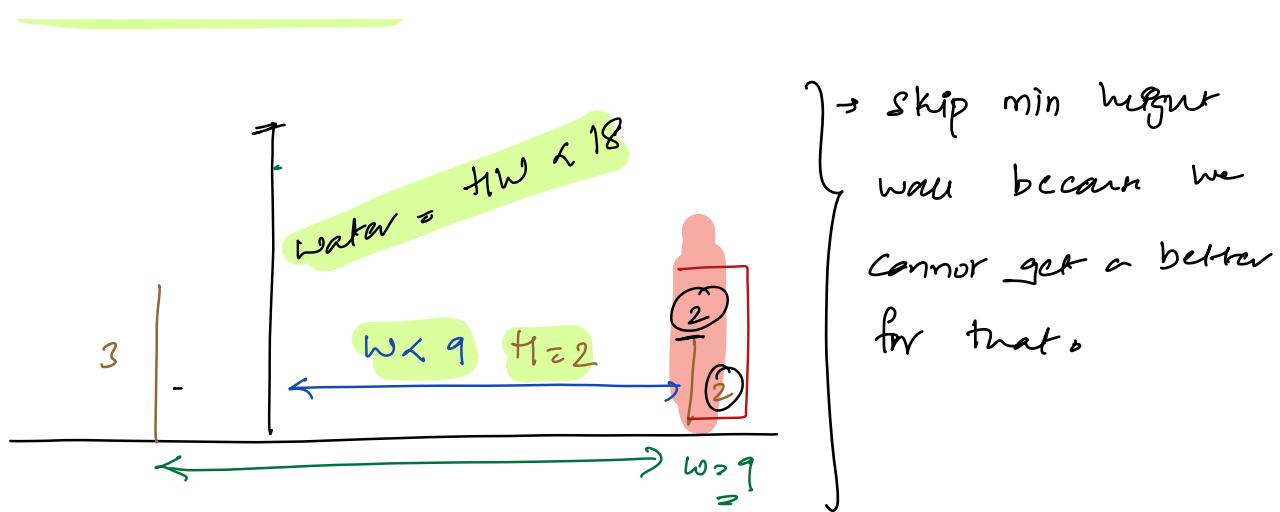
1) We cannot sort  
order changes

2)  $P_1$   $P_2$

We are moving  
the pointer  $\rightarrow$   
minval bcaz  
we cannot get  
better ans

$ans = 0$

$P_1$	$P_2$	$H = \min(ar[P_1], ar[P_2])$	$w: (P_2 - P_1)$	water: ( $H^w$ )
0	9	2	9	18
0	8	1	8	18
0	7	3	7	21
1	7	4	6	24
1	6	5	5	25
1	5	5	4	25
2	5	4	3	12
3	5	4	2	12
3	4	3	1	3
3	3	Break		



Pseudo Code:

1) Check all pairs  $\Rightarrow TC: O(N^2)$   $SC: O(1)$

$$p=0; p < N; p++ \}$$

$$j = p+1; j < N; j++ \}$$

$$H = \min(ar(p), ar(j))$$

$$w = j - i$$

$$water = h'w$$

$$ans = \max(ans, water)$$

return ans

Pseudocode

TODD ?

Q8) Given 3 sorted arrays  $A[], B[], C[]$  of size  $N$

find  $i, j, k$  such that

$\max(A[i], B[j], C[k]) - \min(A[i], B[j], C[k])$  is minimized

$$A[] = \{ 3, 14, 16, 20, 21, 40 \} \leftarrow P_1$$

$$B[] = \{ -6, 23, 24, 30, 35, 50 \} \leftarrow P_2$$

$$C[] = \{ -15, 15, 26, 31, 39, 42 \} \leftarrow P_3$$

$i$	$j$	$k$	$A[i]$	$B[j]$	$C[k]$	$\max$	$\min$	$\Delta$
0	0	0	3	-6	-15	3	-15	18
0	1	1	3	23	15	23	3	20
2	2	2	16	24	26	26	16	8
3	2	1	20	24	15	24	15	9
4	3	3	21	30	31	31	29	2

Ans = 2

BF:

1) There are pairs:

$O(N^3)$  SC:  $O(1)$

$\left. \begin{array}{l} i=0; i < N \\ j=0; j < N \\ k=0; k < N \end{array} \right\}$

3 different arrays

thus  $\downarrow$

$\rightarrow$  BS

$\uparrow$

$\rightarrow$  2 pointers

$A[ ]$	0	1	2	3	4	5	$A[P_1]$	$B[ ]$	$C =$	max	min
	3	14	16	20	21	40	P <sub>1</sub>	14	-15	73	-15
							P <sub>2</sub>	16	23	24	20
								20	24	29	35
								29	35	40	50
							P <sub>2</sub>	40			

man-min  $\geq 18$   
Since not better  
Ans, discard -15

//decreas - diff)

$P_1$	$P_2$	$P_3$	$A[P_1]$	$B[P_2]$	$C[P_3]$	man	min	$(\text{man} - \text{min})$
0	0	0	3	-6	-15	3	-15	18
0	0	1	3	-6	15	15	-6	21
0	1	1	3	23	15	23	3	20
1	1	1	14	23	15	23	14	9
2	1	1	16	23	15	23	15	8
2	1	2	16	23	26	26	16	10
3	1	2	20	23	26	26	20	6
4	1	2	29	23	26	29	23	6
4	2	2	29	24	26	29	24	5
4	3	2	29	20	26	29	26	4
4	3	3	29	20	31	31	29	2
5	3	3	40	20	31	40	30	10
5	4	3	40	35	31	40	31	9
5	4	4	40	35	39	40	35	5
5	5	4	40	50	39	50	39	11

5 5 5 40 50 42 50 40 10

Pseudo code

$$[P_1 = 0, P_2 = 0, P_3 = 0] \quad \text{or} \quad [P_1 > N-1, P_2 > N-1, P_3 > N-1]$$

while ( $P_1 < N_1$   $\&$   $P_2 < N_2$   $\&$   $P_3 < N_3$ )



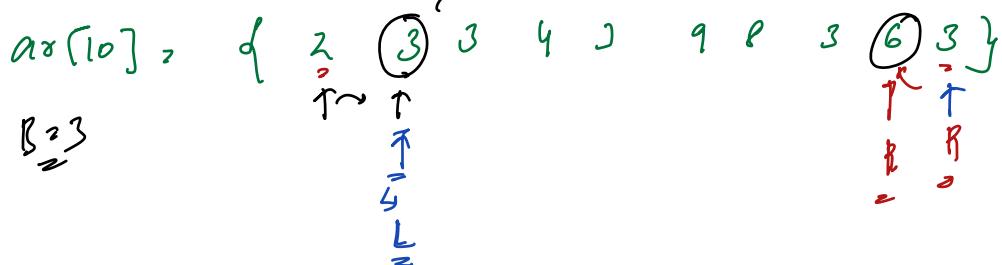
TC:  $O(N \cdot N \cdot N)$

$\Rightarrow O(2N)$

$\Rightarrow O(N)$

SC:  $O(1)$

58) Given  $N$  array elements make all  $\text{Ele} = B$  in right



//

All pairs using map. { $a+b$  with their freq}

$$\begin{array}{l} x+y=20 \\ 6 \\ 3 \quad 17 \\ \text{freq}(8) \quad \text{freq}(12) \\ 5 \quad 2 \end{array} \Rightarrow 10 \text{ pairs}$$

$$\left. \begin{array}{l} x+y=20 \\ 6 \\ 10 \\ \text{freq}(n) \\ 5 \\ 5 \\ 12 \end{array} \right\} \begin{array}{l} y \\ 10 \\ \text{freq}(10) \\ -5 \\ 2 \end{array} \Rightarrow \begin{array}{l} 25 \text{ pairs} \\ (5)(4) \\ 10 \text{ pairs} \end{array}$$

// Intermediate:  $\rightarrow$  things Session

//