

Today's Content:

- Max min pair → .
- Subarray with max min pair = { }³
- Heaps: { Tang / Peazy / Lemon Squazy }
 - CBT
 - insertion / heapify
 - Heap vs BBST
 - Problems if time permits

SQ) Given N elements find max nnn pair $\rightarrow (i, j) \Rightarrow \underbrace{arr[i]^n arr[j]}_{\text{max}}$

$$\underline{N=4} : \begin{array}{ccccccccc} & 0 & 1 & 2 & 3 & \} & \underline{\text{ans} = 7} & (4^13) = 7 & (3^12) = 1 \\ & \boxed{4} & 3 & 2 & 7 & \} & & (4^12) = 6 & (3^12) = 4 \\ & & & & & & & (4^17) = 3 & (2^17) = 5 \end{array}$$

Ideas: Iterate over pairs & get nnn

$$\underline{\text{TC: } O(N^2)} \quad \underline{\text{SC: } O(1)}$$

$$\underline{\text{Ex: }} \begin{array}{ccccccccc} 5 & 3 & 2 & 7 & \} & \text{nnn} = 5 \end{array}$$

Ideas: Sort q, then adjacent elements: $\star \begin{array}{ccccccccc} 2 & 3 & 5 & 7 & \} \\ \downarrow & \downarrow & \downarrow & \downarrow \\ 1 & 2 & 2 & 2 \end{array} : \underline{\text{ans} = 2}$

Hint: $\begin{array}{c} \overrightarrow{10000} \quad \text{vs} \quad 0 \overbrace{111} \\ \downarrow \quad \quad \quad \downarrow \\ -16 \quad \quad \quad 15 \end{array}$

Ex: $0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8$

// Bunch of strings, say we need to search for a prefix?

↳ Type

$N = 9$: 22 61 38 27 21 34 42 37 43

	5 4 3 2 1 0	$\left\{ \begin{array}{l} \text{// find man } \underline{a^T b} = ? \\ a = 22, \text{ find } b \text{ such that } \underline{22^T b = \text{Man}} \end{array} \right.$
22 :	0 1 0 1 1 0	
61 :	1 1 1 1 0 1	
38 :	1 0 0 1 1 0	
27 :	0 1 1 0 1 1	
21 :	0 1 0 1 0 1	
34 :	1 0 0 0 1 0	
42 :	1 0 1 0 1 0	
37 :	1 0 0 1 0 1	
43 :	1 0 1 0 1 1	

$$\begin{array}{r}
 5 4 3 2 1 0 \\
 \hline
 22 : 0 \downarrow 0 \downarrow 1 \downarrow 1 \downarrow 0 \\
 b : 1 \quad 0 \quad 1 \quad 0 \quad 0 \quad 1 \\
 \hline
 \text{ans} : 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 1
 \end{array}$$

If we fn every element as a^T
and repeat same proc we can
get final ans
fn elem a & get man mn

$$TC: N \times \left\{ \frac{N}{N} \right\}$$

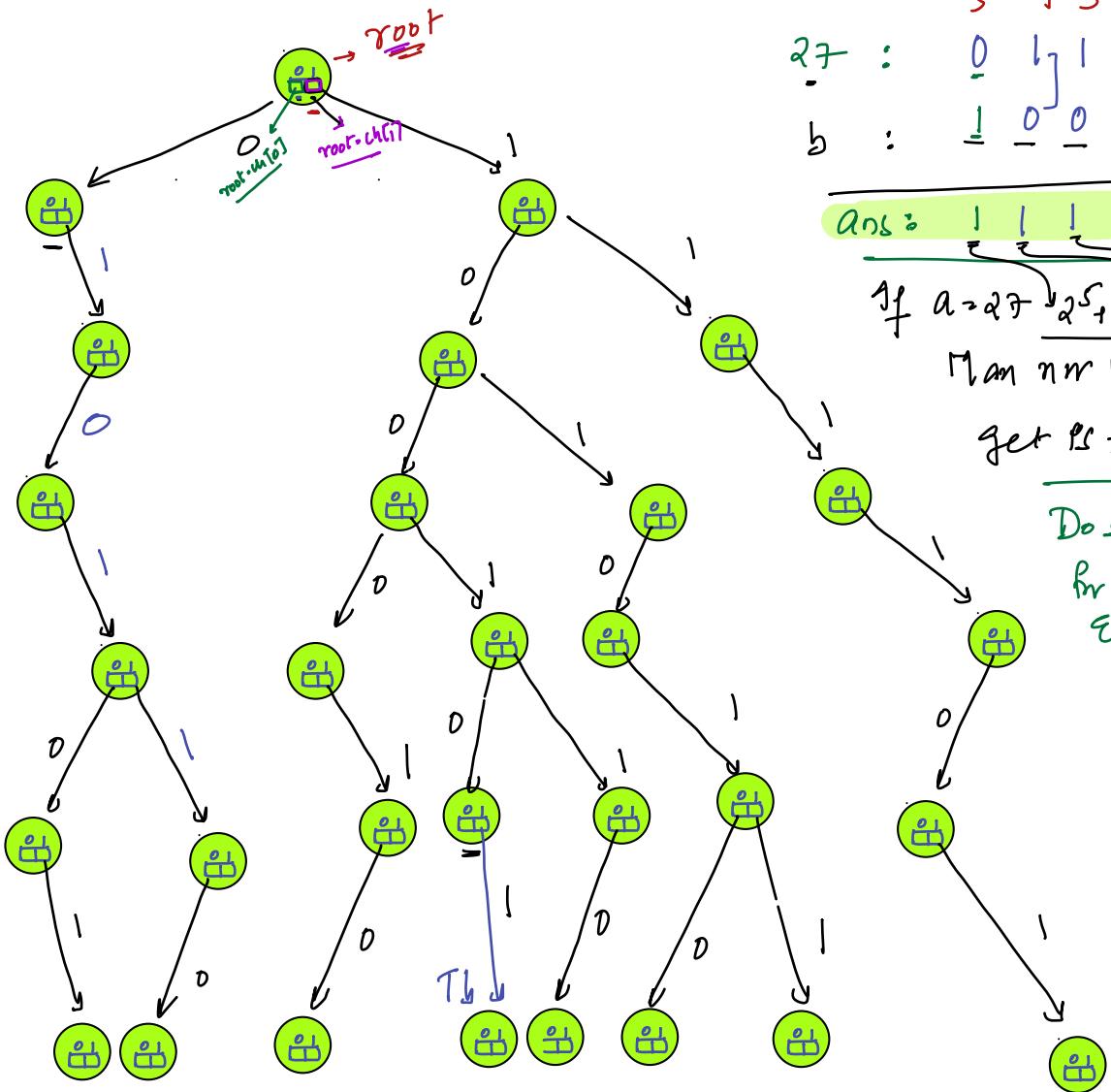
$$TC: \underline{\underline{N}}$$

// Class Node {
| Node c[2]
| }
}

obs1: While inserting we insert
from LSB

obs2: For every number of bits we insert should be same

Step1: Create a root



Price: For every character, how many bits we need to

Iterate \rightarrow [0 30] \rightarrow 81 b91

Enter above process N times $\Rightarrow \underline{O(31 \times N)}$ much better than N^2

P16 B)

```

class Node {
    Node c[2];
}

```

array of children

```

Man(n) {
    Pnt N;
    Read N array Elements
    Node r = new Node(2);
    Pnt n = Man(ar[1]);
    // get more set bit pos for n
    int p = getMSB(n);
}

```

```

    i = 0; i < N; i = i + 1) {
        Pnser(r, ar[i], p)
    }

```

ans = 0;

```

    i = 0; i < N; i = i + 1) {
        if (ar[i] == 1, for a we need
            to get man nrr value?

```

ans = Man(ans, mannr(r, ar[i], p))

to : 35 hrcat

Pnt Man nrr pair(Pnt ar[])

T_C: N * 31

S_C: N * 31

void Pnser(Node cur, Pnt n, Pnt m) {

```

    i = 0; j >= 0; i --) {
        if (cur.ch[i] == NULL) {
            cur.ch[i] = new Node();
        }
        Pnt p = checkBpt(n, i);
        if (cur.ch[i] == NULL) {
            cur.ch[i] = new Node();
        }
        cur = cur.ch[i];
    }
}

```

Pnt mannr(Node cur, Pnt n, Pnt m)

Pnt ans = 0;

```

    i = 0; j >= 0; i --) {

```

Pnt p = checkBpt(n, i);

if (cur.ch[i - p] == NULL) {

// In your ans ith bit will
 can set

ans = ans + (1 << i)

cur = cur.ch[i - p];

else {

cur = cur.ch[p];

return ans;

28) Subarray with Max nw value ?
sum

$$\underline{\text{Ex:}} \quad ar[4] = \{ \underline{\underline{1}} \underline{\underline{2}} \underline{\underline{8}} \underline{\underline{4}} \}$$

$$\begin{matrix} [3] & [2] & [8] & [4] \\ [3, 2] & [2, 8] & [8, 4] & \\ [3, 2, 8] & [2, 8, 4] & & \\ [3, 2, 8, 4] & & & \end{matrix} \quad // \quad \left. \begin{matrix} [i, j] = pf[j] - pf[i-1] \\ [i, j] = pf[j]^n \cdot pf[i-1] \end{matrix} \right\}$$

$$\underline{\text{Ex:}} \quad a[4] = \{ a_0, a_1, a_2, a_3 \}$$

$$pf[nr[4]] = \{ a_0^0, a_0^1, a_0^2, a_0^3, a_0^1 \cdot a_1^1, a_0^1 \cdot a_1^2, a_0^1 \cdot a_1^3, a_0^2 \cdot a_1^1, a_0^2 \cdot a_1^2, a_0^2 \cdot a_1^3, a_0^3 \cdot a_1^1, a_0^3 \cdot a_1^2, a_0^3 \cdot a_1^3 \}$$

$$pf[6] = nr \text{ of all elements } [0, 6] = n_0^1 n_1^1 n_2^1 n_3^1 n_4^1 n_5^1$$

$$pf[2] = nr \text{ of all elements } [0, 2] = n_0^1 n_1^1 n_2^1 \quad \boxed{nr[1, 6]}$$

$$pf[6]^n \cdot pf[2] =$$

In your pf[nr[]]: get max nw pair, {Max Subarray XOR}
 given by Tree

Edge case:

$$Pfmr[4] = \{ \overset{0}{a_0}, \overset{1}{a_0^n a_1}, \overset{2}{a_0^n a_1^n a_2}, \overset{3}{a_0^n a_1^n a_2^n a_3}, \overset{4}{a_0^n a_1^n a_2^n a_3^n}, 0 \}$$

$$0 \ 1 : a_1$$

$$0 \ 2 : a_1^n a_2$$

$$0 \ 3 : a_1^n a_2^n a_3$$

$$1 \ 2 : a_2$$

$$1 \ 3 : a_2^n a_3$$

$$2 \ 3 : a_3$$

few subarray "m" are missing \rightarrow

$$a_0$$

$$a_0^n a_1$$

$$a_0^n a_1^n a_2$$

$$a_0^n a_1^n a_2^n a_3$$

Way to solve this

\rightarrow In $Pfmr[]$ we can get all their value n

\rightarrow Iterate a set man

II If we add extra 0 in $Pfmr[]$

$$0 \ 4 : a_0$$

$$1 \ 4 : a_0^n a_1$$

$$2 \ 4 : a_0^n a_1^n a_2$$

$$3 \ 4 : a_0^n a_1^n a_2^n a_3$$

// pseudo code :

→ given array $ar[N]$

TC: $O(N)$

SC: $O(N)$

$pfmr[0] = ar[0]$

for $ans = ar[0]$

$i = 1; i < N; i = i + 1 \}$

$pfmr[i] = pfmr[i-1] \oplus ar[i]$

$ans = \max(ans, pfmr[i])$

return $\max(ans, PlanXORpair(pfmr))$

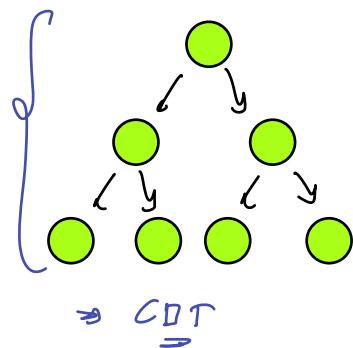
}



// Every square is Rectangle \Rightarrow

→ All CBT's are BBT ✓

→ All BBT's are CBT's ✗



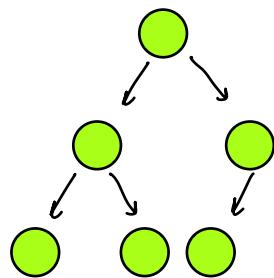
Complete Binary Tree:

A Binary Tree is Said to be CBT if

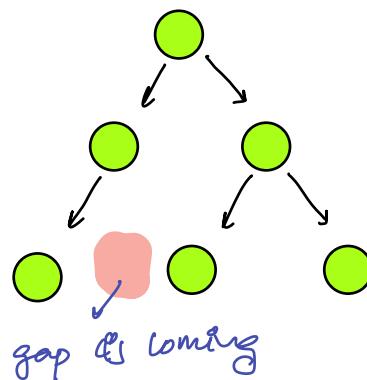
- Data is filled level by level from L-R :
- Except last level all levels have to be filled

Completness

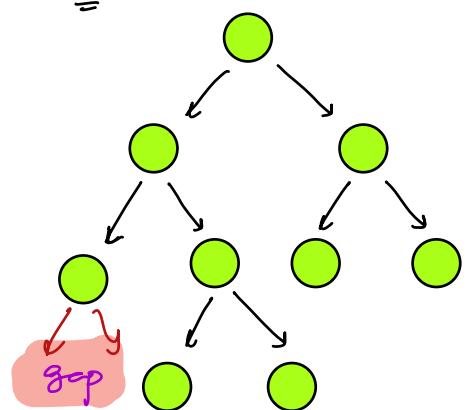
Ex1: CBT ✓



Ex2: NOT CBT



Ex3: NOT CBT

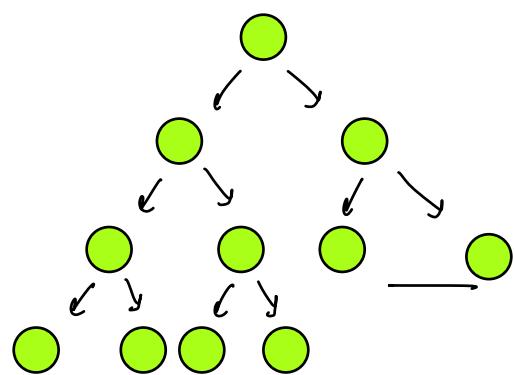


Ques1: Height of a Balanced Tree = (log N)

Ques2: → Balanced Binary Tree

$$\text{H for } \frac{G}{\text{Nodes}} \rightarrow |H(LST) - H(RST)| \leq 1$$

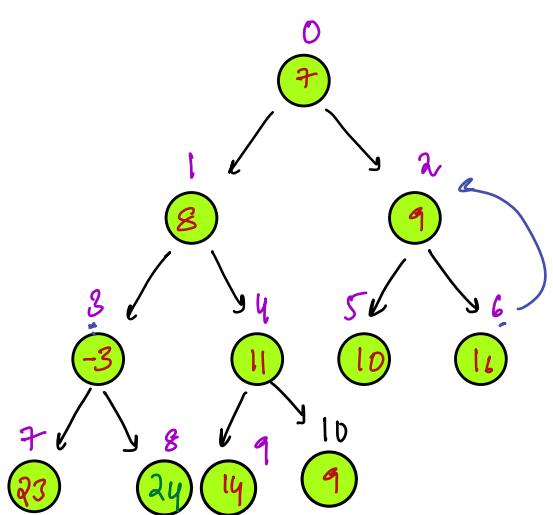
condn ⇒ Every CBT → BBT



$$|H(LST) - H(RST)| \leq 1$$

Height of Every CBT for N Nodes is log N

Construction of CBT: \Rightarrow Complete CBT we will store in Array



Insert 10
Insert 16
Insert 23
Insert 24
Insert 14
Print (9)

left right

Ques 3: parent at i , children at $\{2^{i+1}, 2^{i+2}\}$

Ques 4: children at i , parents at $\{\frac{q-1}{2}\}$

parent $\rightarrow \lfloor \frac{q-1}{2} \rfloor$

$$q=3 \rightarrow 1 \rightarrow \lfloor \frac{2}{2} \rfloor$$

$$q=7 \rightarrow 3 \rightarrow \lfloor \frac{6}{2} \rfloor$$

$$q=6 \rightarrow 2 \rightarrow \lfloor \frac{5}{2} \rfloor$$

heaps

?

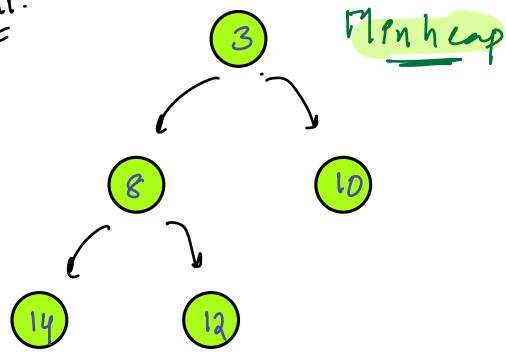
CBT

property

Every Node \geq (of its child nodes): Maxheap

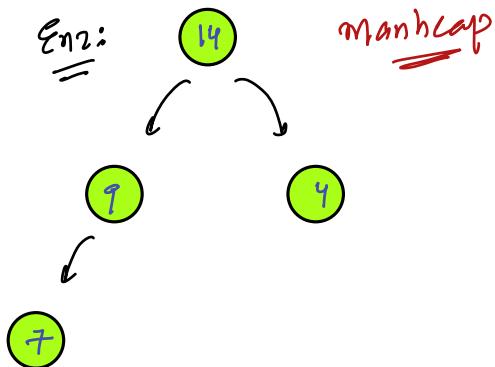
Every Node \leq (of its child nodes): Minheap

Ex1:



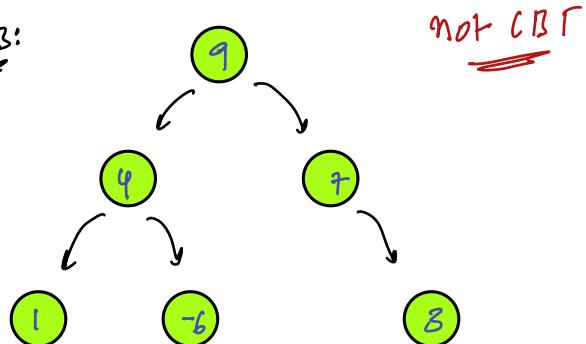
Minheap

Ex2:



Maxheap

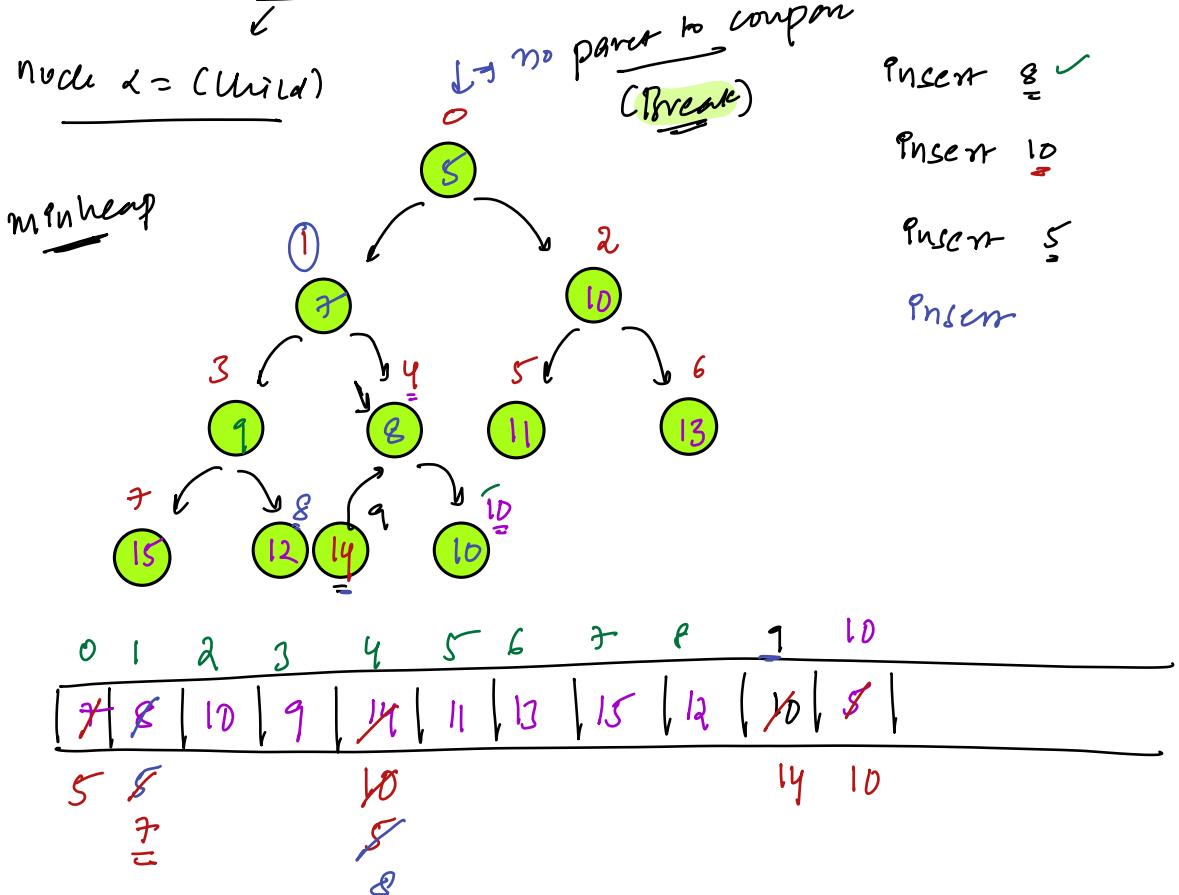
Ex3:



not CBT

// Insert in heap CBT: We are given an 16
↳ so we increase size

Ex: Given Min heap, insert new element



void insert (**lptr & pnt** t , **pnt** n) $\{ \rightarrow O(\log N)$

$t.add(n);$

$\text{put } i = t.size() - 1$

while ($i > 0$) {

pnt $p = (i-1)/2$

if ($t[p] > t[i]$) {

swap ($t[p], t[i]$)

$i = p;$

else { break; }

$T \leq O(\log N)$

minheap

manheap \sim

getMan() $\Rightarrow O(1)$

from smaller

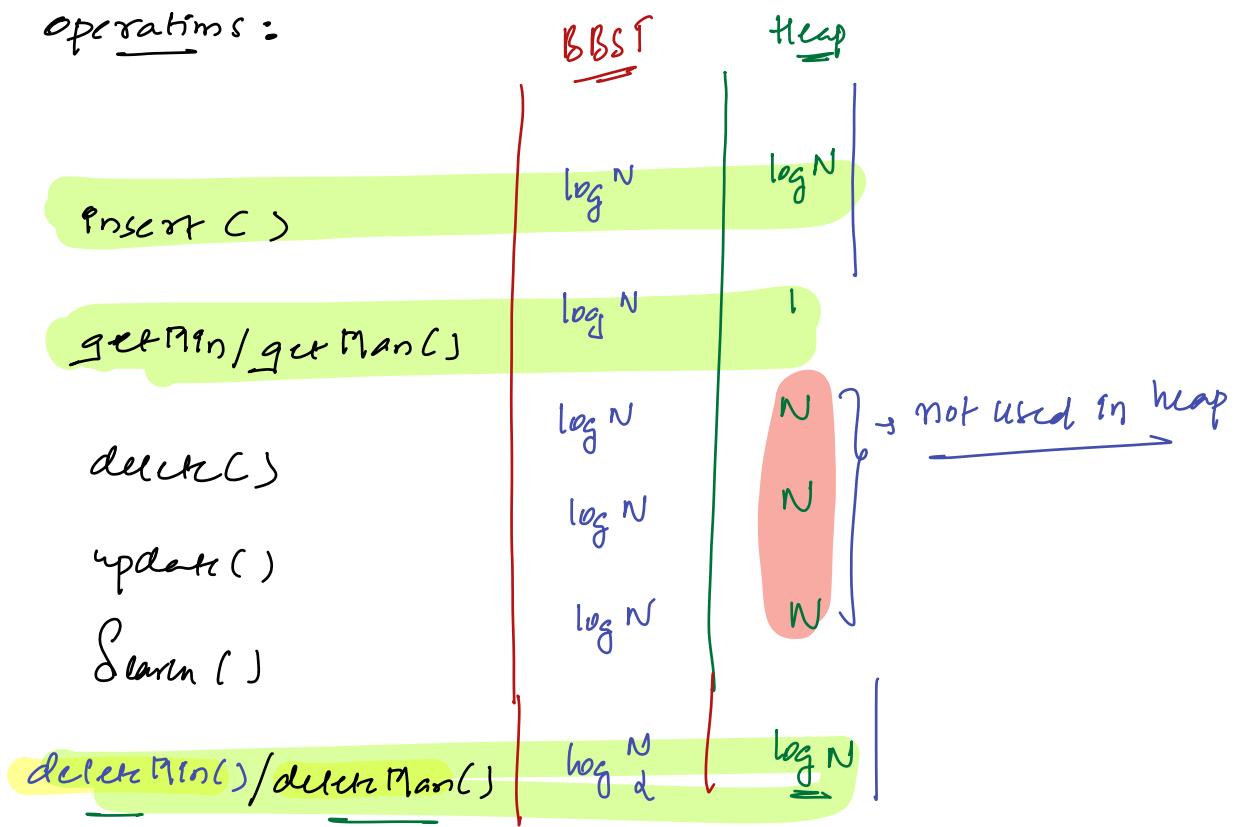
// getmin $\rightarrow O(1)$

// del : $\rightarrow O(N)$

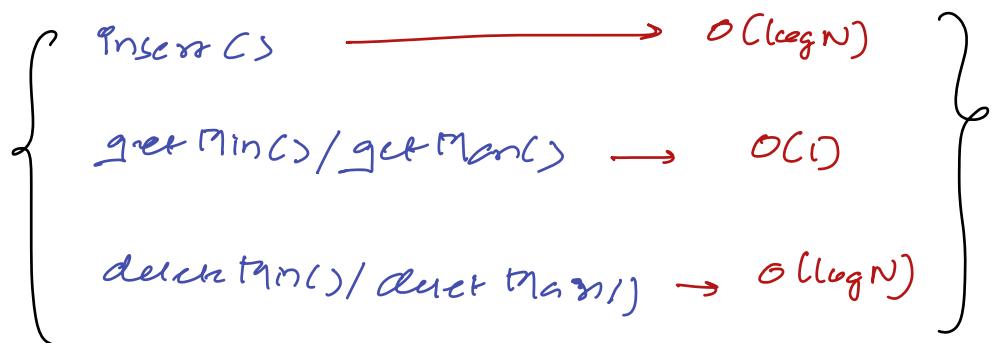
// update : $\rightarrow O(N)$

// search : $\rightarrow O(N)$

operations:



operations:



C++

Priority-queue

Java

Priority Queue

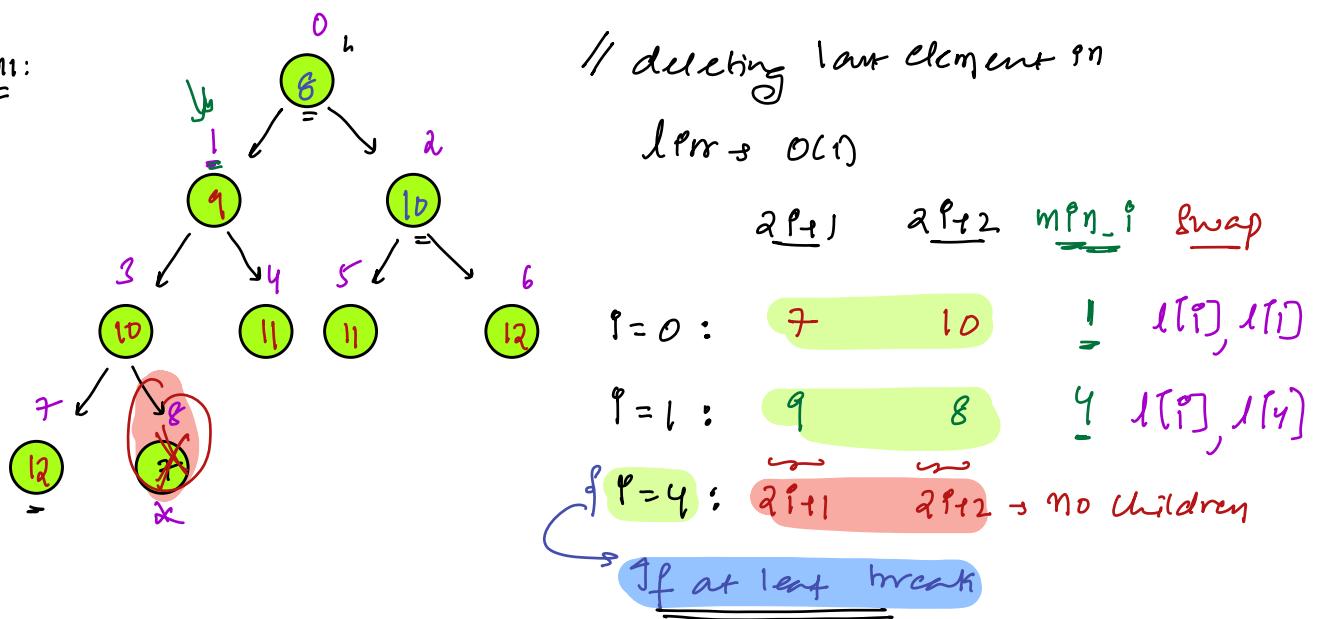
Python

(heapq)

Delete in heap → given a list:

gives min heap, delete min element

Ex1:



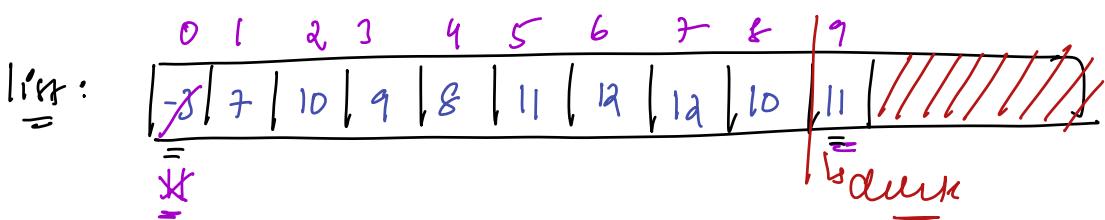
$2^{p+1} \quad 2^{p+2} \quad \underline{\text{min_}}^i \quad \underline{\text{swap}}$

$p = 0 : \quad 8 \quad 10 \quad 1 \quad l[0] \leftarrow l[1], \quad p = 1$

$p = 1 : \quad 9 \quad 11 \quad 3 \quad l[0] \leftarrow l[3] : \quad p = 3$

$p = 3 : \quad 13$

l[0] ← l[3] : {no swap}



void deletemin(l & lnt, i) $\Rightarrow (\underline{\log N})$

int n = l.size();

l[0] = l[n-1] // bring last element to front

l.deletel // it will delete last element

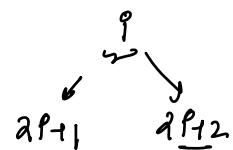
n = n-1 // size reducing

i = 0

while(i < n)

mⁱⁿ-i = i;

left = 2ⁱ⁺¹, right = 2ⁱ⁺²



if(left < n $\&$ ar[mⁱⁿ-i] > ar[left]) {

mⁱⁿ-i = left

if(right < n $\&$ ar[mⁱⁿ-i] > ar[right]) {

mⁱⁿ-i = right

if(T != mⁱⁿi) {

Swap(ar[i], ar[mⁱⁿi])

i = mⁱⁿ-i

else { break }

↳ if mⁱⁿi == i we anyway break

indicating a new min. found

// S_{my} :

$TODO$ → $ManCap$

{ Plan / Problem Solving Step

$MinCap$

$T_{rec} \rightarrow L \xrightarrow{All} R$ }

$T_{rec} \rightarrow R \rightarrow L$

$s_0 s_1 s_2 s_3 s_4 s_5$

