

Q8) Given a Square Matrix print boundary/Perimeter/  Clock

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12
3	13	14	15	16

[HARD] \rightarrow _____ }

output:

1 2 3 4 8 12 16 15 14 13 9 5

$\rightarrow N=4$ { 3H, 3V, 3H, 3V }

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

output:

1 2 3 6 9 8 7 4

	0	1	2	3	<u>4</u>
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

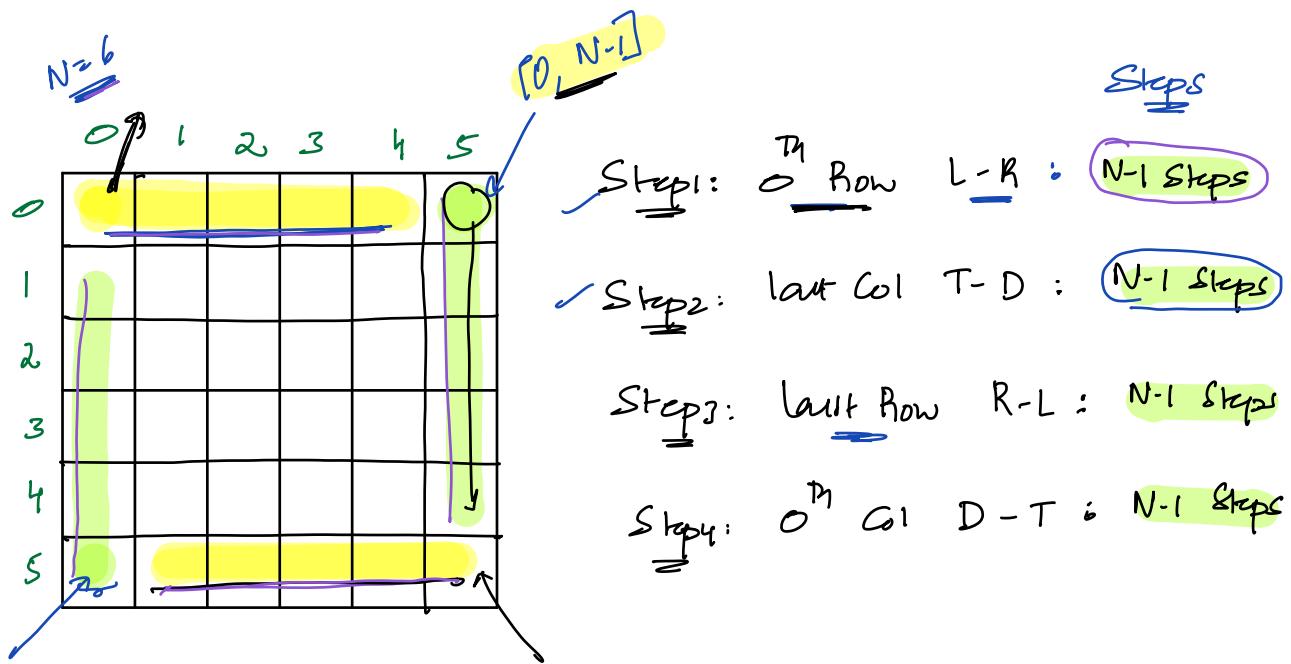
Idea:

Step 1: Print 0th Row (L-R) : 4 Steps

Step 2: Print last col (T-D) : 4 Steps

Step 3: Print last row (R-L) : 4 Steps

Step 4: Print 0th Col (D-T) : 4 Steps



Pseudo Code : $\rightarrow TC: O(N^2)$ } \rightarrow for Rectangular

$i=0, j=0$ \rightarrow $N \geq 1$ & $M \geq 1$

while ($N \geq 1$) { \rightarrow $N-1$ times

$i = i; i < N; i++ \} // Point O^T row$

print (mat [i] [j])

$i++$

// After above loop $i = 0 \quad j = N-1$

$i = i; i < N; i++ \} // Printing last column$

print (mat [i] [j])

$i++$

// After above loop $i = N-1 \quad j = N-1$

$i = i; i < N; i++ \} // Printing last row R-L$

print (mat [i] [j])

$i--$

// After above loop $i = N-1 \quad j = 0$

$i = i; i < N; i++ \} // print first column D-U$

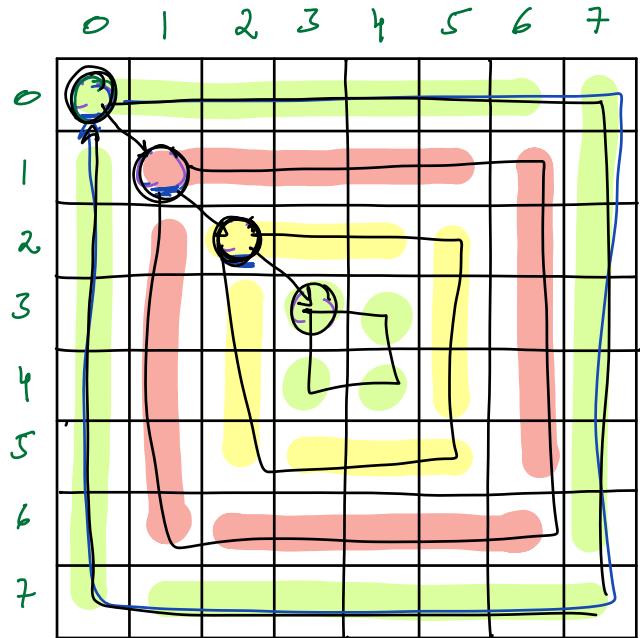
print (mat [i] [j])

$i--$

$N = N-2; i = i+1; j = j+1$

$\text{if } (N == 1) \{ \text{print} (\text{mat}[i][j]) \}$ } Edge Case

N=8



N=8

- Step 1: + Steps $[0, 0] \rightarrow [0, 6]$
 + Steps $[0, 7] \rightarrow [6, 7]$
 + Steps $[7, 7] \rightarrow [7, 1]$
 + Steps $[7, 0] \rightarrow [1, 0]$

N=6

- Steps: 5 Steps $[1, 1] \rightarrow [1, 5]$
 5 Steps $[1, 6] \rightarrow [5, 6]$
 5 Steps $[6, 6] \rightarrow [6, 2]$
 5 Steps $[6, 1] \rightarrow [2, 1]$

N=4 3 Steps $[2, 2] \rightarrow [2, 4]$

- 3 Steps $[2, 5] \rightarrow [4, 5]$
 3 Steps $[5, 5] \rightarrow [5, 3]$
 3 Steps $[5, 2] \rightarrow [3, 2]$

N=2

- 1 Step $[3, 3]$
 1 Step $[3, 4]$
 1 Step $[4, 4]$
 1 Step $[4, 3]$

$N \approx S$

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

Step 1: $\underline{N=5}$ $\underline{i=j}$
 4 steps $[0 \ 0] \rightarrow [0 \ 3]$
 4 steps $[0 \ 4] \rightarrow [3 \ 4]$
 4 steps $[4 \ 4] \rightarrow [4 \ 1]$
 4 steps $[4 \ 0] \rightarrow [1 \ 0]$

$$\frac{N=5}{N=3}, i=0+1, j=0+1$$

2 steps $[1 \ 1] \rightarrow [1 \ 2]$
 2 steps $[1 \ 3] \rightarrow [2 \ 3]$
 2 steps $[3 \ 3] \rightarrow [2 \ 2]$
 2 steps $[2 \ 1] \rightarrow [2 \ 1]$

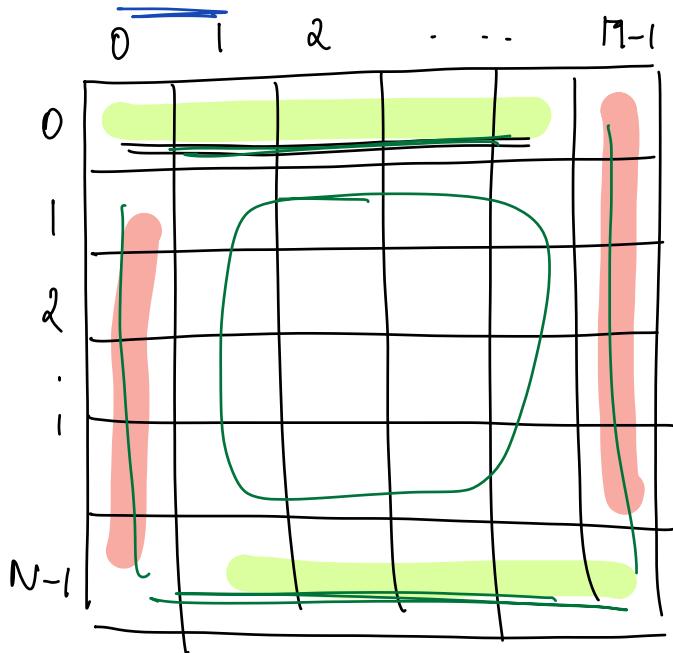
$\underline{N=1}$ $\boxed{i=2, j=2} \rightarrow i, j \text{ at center}$

0 steps
 0 steps
 0 steps
 0 steps

$\underline{N=-1}$ $i=2, j=3 \rightarrow$

// H_{out}: (TODO)

Mat[N][M]



Step 1

from row 0 to M-1 steps (L-R)

last row: N-1 steps (T-D)

last row: M-1 steps (R-L)

from col 0: N-1 steps (D-T)

N → N-2 M → M-2, i = i+1, j = j+1

Edge case: { }

2022

$\overbrace{[N \times M]}^{\substack{N \text{ rows} \\ M \text{ columns}}$

Given a 2D Matrix every row is sorted & every

column is sorted, Check an element $k = \underline{15}, \checkmark, 34, \cancel{30}$

	0	1	2	3	4	5	$k = \underline{15}$
0	-1	2	4	5	9	11	$\leq 15 \ X$
1	1	4	7	8	10	14	$\leq 15 \ X$
2	3	7	9	10	12	18	$\geq 15 \ \{ \text{Maybe/BS} \}$
3	6	10	12	14	16	20	$\geq 15 \ \{ \text{Maybe/BS} \}$
4	9	13	16	19	22	24	$\geq 15 \ \{ \text{Maybe/BS} \}$
5	11	15	19	21	24	27	$\geq 15 \ \{ \text{Maybe/BS} \}$
6	14	20	25	29	31	39	$\geq 15 \ \{ \text{Maybe/BS} \}$
7	18	24	29	32	34	42	

Sol:

$\overline{\text{D}}$ linear search on entire matrix

$\underline{\text{TC}}: [N \times M] \ \underline{\text{SC}}: O(1)$

2) In an sorted arr \underline{N}

To apply $\underline{\text{BS}} \rightarrow \underline{O(\log N)}$

Apply BS in Every Row $\underline{(M)}$

$\underline{\text{TC}}: [N \times \log M]$

$\underline{\text{SC}}: 1$

3) Compare k with last element & apply BS

$\underline{\text{TC}}: N \times \log M \ \underline{\text{SC}}: 1$

	0	1	2	3	4	5
0	-1	2	4	5	9	11
1	1	4	7	8	10	14
2	3	7	9	10	12	18
3	6	10	12	14	16	20
4	9	13	16	19	22	24
5	11	15	19	21	24	27
6	14	20	25	29	31	39
7	18	24	21	32	34	42

$k=15$ (if we try step either we
skip a row or column N)

Idea: $\rightarrow T_C: O(N \cdot M) \quad S_C: O(1)$

$i=0, j=M-1$

while ($i \leq N \wedge j \geq 0 = D$) {

$\text{Mat}[i][j] < k$ ↳

 // skip row, $i++$

$\text{Mat}[i][j] > k$:

 // skip col; $j--$

$\text{Mat}[i][j] == k$

 return True

return False

Neha's skipping

	0	1	2	3	4	5
0	-1	2	4	5	9	11
1	1	4	7	8	10	14
2	3	7	9	10	12	18
3	6	10	12	14	16	20
4	9	13	16	19	22	24
5	11	15	19	21	24	27
6	14	20	25	29	31	39
7	18	24	21	32	34	42

↑ Note:

 we can either start
from top right or bottom left

Top right

Inc

↓ dec

42 > 15

Bottom right

Bottom left

Inc

dec

Q8) Given a 2D Matrix, every element is 0/1,
Every row is sorted,
find the first column which contains = 1

Ex1:

	0	1	2	3	4
0	0	0	0	1	1
1	0	0	0	0	0
2	0	1	1	1	1
3	0	0	0	1	1
4	0	0	0	1	1

$\text{ans} = 1$

Ex2:

	0	1	2	3	4
0	0	0	0	0	1
1	0	0	0	0	0
2	0	0	0	1	1
3	0	0	1	1	1
4	0	0	0	0	1
5	0	0	0	1	1

$j = 1$ $\text{ans} = j + 1$

$$i = 0, j = M - 1$$

while ($i < N \& \& j \geq 0$) {

 mat[i][j] == 1 {

 skip column
 $j--$

 } else

 skip row
 $i++$

 } // ans = j + 1

 if ($j = M - 1$)
 return -1

Ex: TL TODO

	0	1	2	3	4	5
0	0 0 0 0	1 1				
1	0 0 0 0	0 1				
2	0 0 0 0	1 1	1 1			
3	0 1 1 1	1 1	1 1	1 1		
4	0 0 1 1	0 1	1 1	1 1	1 1	
5	0 0 0 0	0 1	1 1	1 1	1 1	
6	0 0 0 0	0 0	0 1	1 1	1 1	1 1

BR

ans = 0 } ans = 0 + 1 = 1

TL TODO

ans = 1

Edge case =

	0	1	2	
0	0 0 1 0			
1	0 0 0 0			
2	0 0 0 0			

$j=1 / \underline{ans = j+1 = 2}$

0	0	0	0
0	0	0	0
0	0	0	0
0	0	0	0

$j=M-1 / \underline{ans = N}$

Ex:

0	0	0	0
0	0	0	1
0	0	0	0
-	-	-	1

$j=-1 | \underline{ans = j+1, \underline{ans = 0}}$

→ _____ Output _____ [HARD]

48) Given N array elements Initialized = 0 & Queries

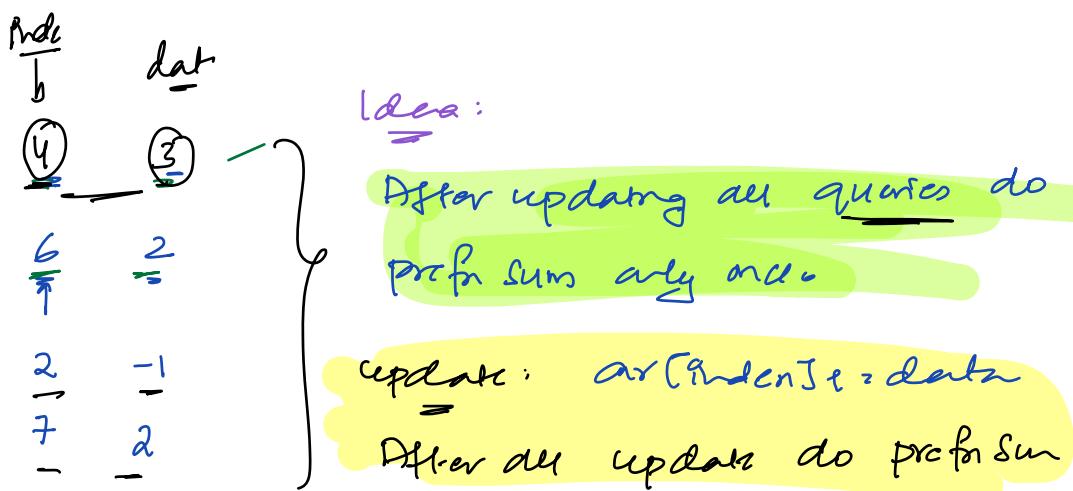
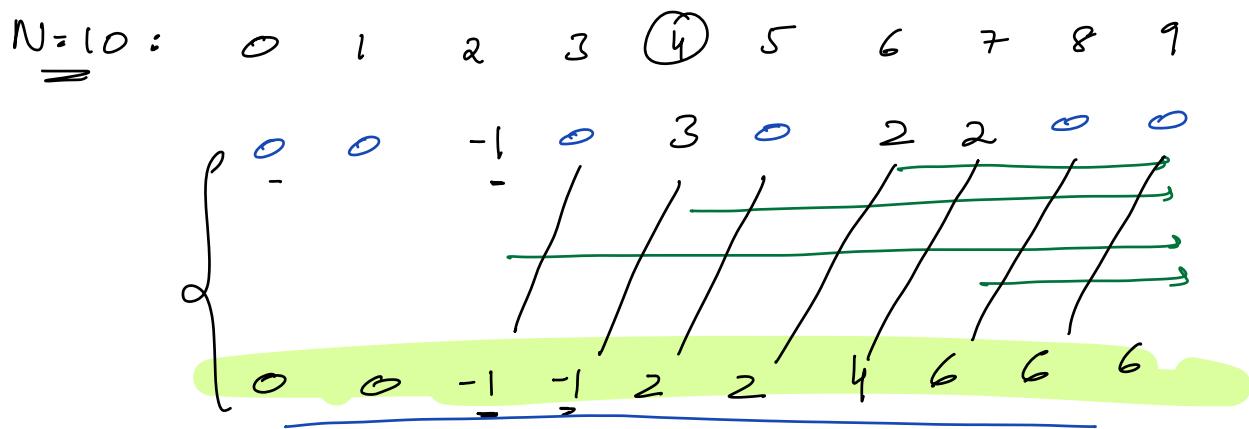
i data } // Repeat $O(j)$ {
 4 3
 6 2
 ↑ =
 2 -1
 7 2

j = i; $j \leq N; j++$ {
 |
 arr[j] = data

TC: $O(N)$
 SC: $O(1)$

Technique

- | | |
|--------------------|--|
| ① Prefork // | $Pf[\sigma] = ar[\sigma]$ |
| ② Copy P | $Pf[\tau] = ar[\sigma] + ar[\tau]$ |
| ③ <u>Carbs</u> X | $Pf[\gamma] = ar[\sigma] + ar[\tau] + ar[\gamma]$ |
| ④ <u>Subs</u> X | $Pf[\delta] = ar[\sigma] + ar[\tau] + ar[\gamma] + ar[\delta]$ |
| ⑤ <u>Editing</u> X | |



Ques) Given N away elements = 0 & Queries

$arr[10]: 0 \quad 1 \quad 2 \quad 3 \quad 9 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9$

$0 \quad 3 \quad 0 \quad -2 \quad 0 \quad 0 \quad -3 \quad 0 \quad 2 \quad 0$

Average propagate

Nullify Each

Pf $0 \quad 3 \quad 3 \quad 1 \quad 1 \quad 1 \quad -2 \quad -2 \quad 0 \quad 0$

Ques 1:

$1 \quad 5 : 3$

Idea:

D update all queries

$3 \quad 7 : -2$

a) later pref

Query: $l \underline{r} \text{ data} :$

update all queries =

```

if ( $r < N-1$ ) {
     $arr[l] += \text{data}$        $arr[r+1] -= \text{data}$ 
}
else {  $\rightarrow r = N-1$  }
     $arr[l] += \text{data}$ 
}

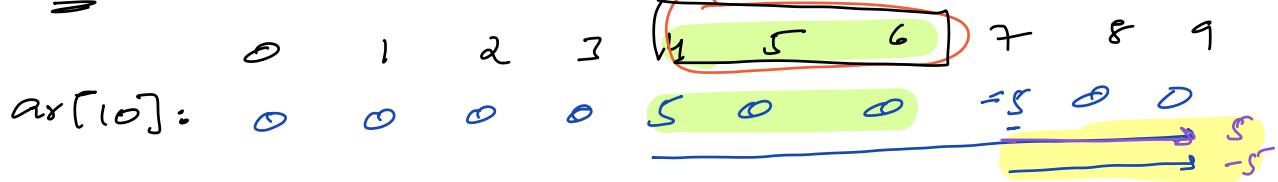
```

Apply same for Rn

$\Rightarrow 10^5 = 10^5, 10^a = 10^a$

$10^{q+r} =$
exponent
 10^{q+r}

Doubts



Query

$$4 \quad 6 \quad 5 \quad \left. \begin{array}{l} \text{arr}[4] = 5 \\ \text{arr}[7] = ? \end{array} \right\}$$

$l \quad r \quad n$

\rightarrow [Add n , $l \xrightarrow{l \rightarrow N-1}$] $\text{arr}[l] = n$

[Subs n , $r+1 \xrightarrow{r+1 \rightarrow N-1}$] $\text{arr}[r+1] = n$