```
Output: A R1CS r consisting of w three vectors, and the length of each vector is l
Input: the list res of RNode in the created graph
       res \leftarrow \emptyset
  for i \leftarrow 1 to w do
      res.append(\mathbf{new}\ rightnode)
  end for
  for z \leftarrow 1 to l do
      node_a \leftarrow \mathbf{None}
      cons \leftarrow z^{th} constraint in r
      for i \leftarrow 0 to l do
         node_a \leftarrow \mathbf{None}
          if cons.a[i] \neq 0 then
              if i == 0 then
                  node_a \leftarrow CreateConstNode(cons.a[i])
                  res.append(node_a)
              else
                  tmp \leftarrow CreateConstNode(cons.a[i])
                  node_a \leftarrow Multiple(tmp, res[i])
                  res.append(node_a)
                  res.append(tmp)
              end if
             for j \leftarrow 0 to l do
                  node_b \leftarrow \mathbf{None}
                  if cons.b[j] \neq 0 then
                     if j == 0 then
                          node_b \leftarrow CreateConstNode(cons.b[j])
                          res.append(node_b)
                     else
                          tmp \leftarrow CreateConstNode(cons.b[j])
                          node_a \leftarrow Multiple(tmp, res[j])
                          res.append(node_b)
                          res.append(tmp)
                     end if
                     if i and j are the indices corresponding to the last non-zero elements in the constraint. then
                          if only one element in the cons.c is not zero then
                              if leftnode == None then
                                  result node \leftarrow coresponding node of none - zero elementinc
                                 result node.operation \leftarrow Multiple
                                 result node. father \leftarrow \{node_a, node_b\}
                                 node_a.child.append\{\text{result node}\}\
                                  node_b.childappend\{result\ node\}
                              else
                                 rightnode \leftarrow Multiple(node_a, node_b)
                                 res.append(rightnode)
                                 result node \leftarrow coresponding node of none-zero elementinc
                                 result node.operation \leftarrow Add
                                 result node. father \leftarrow \{leftnode, rightnode\}
                                 leftnode.child.append{result node}
                                  rightnode.child.append{result node}
                              end if
                          else
                              for k \leftarrow 0 to l do
                                 if cons.c[k] \neq 0 then
                                      if i == 0 then
                                          node_c \leftarrow CreateConstNode(cons.c[k])
                                          res.append(node_c)
                                      else
                                          tmp \leftarrow CreateConstNode(cons.c[k])
                                          node_c \leftarrow Multiple(tmp, res[k])
                                          res.append(node_c)
                                          res.append(tmp)
                                     end if
                                      if rightnode == None then
                                          rightnode \leftarrow node_c
                                      else
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rightnode \leftarrow Add(rightnode, node_c);
                                res.append(rightnode)
                             end if
                         end if
                     end for
                     if leftnode == None then
                         leftnode \leftarrow Multiple(node_a, node_b)
                         res.append(leftnode)
                     else
                         tmp \leftarrow Multiple(node_a, node_b)
                         leftnode \leftarrow Add(leftnode, tmp)
                         res.append(leftnode)
                         res.append(tmp)
                     end if
                 end if
                 goton ext constraint
              else
                  if leftnode == None then
                     leftnode \leftarrow Multiple(node_a, node_b)
                     res.append(leftnode)
                 else
                     tmp \leftarrow Multiple(node_a, node_b)
                     leftnode \leftarrow Add(leftnode, tmp)
                     res.append(leftnode)
                     res.append(tmp)
                  end if
              end if
          end if
       end for
   end if
end for
```

end for

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Output: the root RNode of the tile to be chosen and a flag
Input: set of the edges of the chosen tile, s
  function GetTile(r, flag, s)
      {f if} r has no predecessor nodes {f then}
         return
      end if
      if flag == False & r.opretion == Multiple & both father nodes of r represents constant value then
      end if
      if flag == True \& r.opretion == Multiple \& both father nodes of r represent variables then
         s.add (< r, father_{left} >)
         s.add(\langle r, father_{right} \rangle)
         return
      end if
      \mathbf{if} \text{ r.operation} == \mathbf{Multiple} \mathbf{then}
         s.add(< r, father_{left} >)
         s.add (< r, father_{right} >)
         if father_{left} represents constant value then
             GetTile(r, false, father_{left})
         end if
         if father_{right} represents constant value then
             GetTile(r, false, father_{right})
         end if
      else
         s.add(\langle r, father_{left} \rangle)
         s.add(\langle r, father_{right} \rangle)
         GetTile(r, false, father_{left})
         GetTile(r, false, father_{right})
      end if
  end function
```