

GRAPH ANALYSIS LIBRARY (v0.0 beta)

(A preliminary documentation)

1) INTRODUCTION

1.1) WHAT IS GALib?

GALib is a library for the analysis of graphs and complex networks in Python/NumPy. Networks are represented by their adjacency matrices as rank-2 ndarrays. This choice limits the size of the networks GALib can handle but it allows to exploit NumPy to boost performance far beyond any code written in pure Python.

GALib is intended to be used simply a library, say, a collection of functions which can be called during interactive sessions or in scripts. GALib does not need to define a graph object because it is designed to work on adjacency matrices of graphs declared as rank-2 NumPy arrays, which are well-established and efficient objects in the NumPy package.

The library contains 3 modules. See the Reference Guide or the interactive documentation for a detailed list of functions within each module.

- *gatools.py* : miscellaneous helper functions, e.g. data-type transformations.
- *galib.py* : basic graph descriptors, e.g. degrees and clustering.
- *gamodels.py* : Generation of synthetic networks and randomization.

In an interactive session type `help(modulename)` to see a list of functions included in each of the modules or `help(functionname)` to access the information of each function. In Ipython simply type `modulename?` or `functionname?`

In addition to the library files GALib comes with several example scripts to illustrate its use (see `.../GALib/Examples/` folder). For network scientists who are not familiar with the Python / NumPy environment, GALib includes also a few helper scripts to generate and save into files ensembles of random or scale-free networks, as-well-as ensembles of rewired networks conserving the degrees. Users only need to modify a few selected fields and let GALib do the rest. See `.../GALib/HelperScripts/` folder.

1.2) INSTALLATION

As a library, GALib does not require any installation, but the modules need to be placed in the python path such that they can be imported. The only requirement is to have NumPy/SciPy installed together with Python. If NumPy/SciPy is not yet installed in the computer, visit the following webpage for further information (<http://www.scipy.org>).

For beginners to Python/NumPy/SciPy it is highly recommended to install a Python distribution that already includes NumPy, SciPy and other utilities for numerical and scientific tools. These are easy to install and stable distributions. For example Canopy (<https://www.enthought.com/products/canopy/>) and Anaconda (<https://store.continuum.io/cshop/anaconda/>)

If you don't aim to modify the code in GALib the simplest way to install it is to copy the modules into the sites-package folder. This is a special folder that is installed with Python to place third party libraries and packages. However, its exact location depends both on the operating system and the Python version(s) or distribution(s) currently installed.

1) Find the current python version installed.

This might be more complicated and annoying than it sounds because there might be several versions of Python installed in the computer. For example, Mac OS X and Linux come with a pre-installed version of Python. When re-installing Python through a distribution the older version is not removed and each version has its own "site-packages" folder. To find the current Python version open a terminal and type "python". An interactive shell will open (type `exit()` to leave the interactive shell). The current Python version is displayed in the header. If a Python distribution has been installed that includes NumPy and SciPy, very likely iPython has been installed too. iPython is an advanced interactive shell for Python. If this is the case, open another terminal and type `ipython` to open another interactive shell. In the header the version of Python used by iPython is displayed. Make sure that the two version displayed in the headers are the same. If the two versions are different you will have to copy GALib into the site-packages folder of both Python versions to warranty that it will always work independently of how to run the scripts.

2) Locate the "site-packages" folder.

Once the current version of installed Python installed is known, search the filesystem for folders named "site-packages". Usually the whole path looks like `.../lib/pythonX.Y/site-packages` where X.Y is the Python version number. If several Python versions are installed in the computer, locate the "site-packages" folders for those versions you will be using.

3) Copy the modules of GALib into the "site-packages" folder.

4) Check GALib is correctly installed.

Close any open interactive shells and open them again by typing `python` or `ipython` in the terminal, or open another IDLE session. Import the modules by typing `import galib`, `import gatools` and `import gamodels`. If no error is returned, the library is correctly installed. Otherwise a warning will be raised that the modules are not found.

Now, if you intend to modify the library or to include your own functions to it, the modules in the "site-packages" are usually not possible to modify due to permission restrictions. Alternatively, you can place the modules of GALib in any folder you wish, e.g. `"/usr/myusername/GraphAnalysisLibrary"`. To allow Python to find GALib a text file can be created in the site-packages folder that contains additional folders to be included in the path. Follow steps 1) and 2) previously and do the following:

3) Open a new text document in an editor and type in the files the path you want to include, e.g. the file will have a single line with the text `"/usr/myusername/GraphAnalysisLibrary"`. Save the text document in the "site-packages" folder and give it the extension `".pth"` instead of `".txt"` or any other, for example: `"extrapythonpaths.pth"`. You can include as many paths as you want in a `.pth` file, every path being in one independent line.

1.3) FUTURE PLANS

At this starting stage GALib includes basic graph analysis tools that are robust. In future releases more functionalities, graph measures and network model generators will be included:

- Further measures for weighted and/or directed networks.
- Further classical graph models.
- Functions to compute the roles of nodes in networks with modular organization.
- Support for sparse matrices to increase the size of networks handled.
- Improved data conversions for graph formats used by other packages (Pajek, graph-tools, NetworkX, Gephi, etc.)

Any third party collaboration to improve GALib is highly welcome.

1.4) GALib and my own research

GALib is an accidental by-product of my scientific research. In 2004 I started my Ph.D. in the group of Prof. Jürgen Kurths at the University of Potsdam (Germany) to make research in brain connectivity. My goal was to uncover the topological organization of long-range connections in the cat and the macaque brains. Back in those times complex networks was a exploding baby field and the computational tools were scarce. There was very good software like Pajek, but such pre-packaged programs were too rigid environments for a field constantly in change. I couldn't wait with the hope that somebody would implement new functions to those programs. And I wanted to learn the hard way. So I just started coding myself every graph measure that I needed. I enjoyed that process very much and I ended making my own contributions to graph theory, particularly on the meaning and quantification of significance of graph measures.

Over these nine years I was often tempted to publicly release the library. The evolution of Numeric and Numarray into NumPy delayed my intentions, and it was good so. The extra experience I have gained in the mean time allowed me to improve every single function from code that "just works" to "hopefully optimized". Slowly I discovered that optimizing Python code is very non-trivial.

This initial release of GALib is a bit short in functionalities, the reason is that I am only releasing the code for which I feel confident enough. In the following year(s) GALib will keep growing as I optimize functions still awaiting revision and as my own research continues. I hope that users can also contribute to GALib by including functionalities developed for their own interest.

2) USER GUIDE

2.1) GETTING STARTED

In GALib, graphs and networks are represented by their adjacency matrices, that is, 2-dimensional numpy arrays. The library makes extensive use of NumPy's array manipulation tools to compute the metrics of the networks. An empty network of N nodes is thus represented by a $N \times N$ numpy array full of zeros.

```
>>> from numpy import*
>>> N = 20
>>> emptynet = np.zeros((N,N), dtype=uint8)
```

The dtype is optional and depends on whether the network shall be binary or weighted. Usually, for binary networks the unsigned 8-bit type can be used (uint8) and regular floating-point dtype (float) for real-valued weighted networks. See the numpy documentation for the available data types.

After importing GALib its functions can be applied to existing networks, or synthetic networks can be generated for their analysis. In the following, a random graph of the Erdős-Renyi type is generated with $N = 20$ nodes and link probability 0.2 for its further analysis.

```
>>> from galib import *
>>> from gamodels import *
>>> N = 20
>>> p = 0.2
>>> net = ErdosRenyiGraph(N, p)
```

In order to know the dtype of the generated network simply type:

```
>>> net.dtype
dtype('uint8')
```

Now, the number of links in the network can be recovered from counting the number of 1s in the adjacency matrix. As the network is binary, we only need to sum over its elements. The 0.5 factor is applied because in this case the network is undirected:

```
>>> L = 0.5 * net.sum()
>>> L
36.0
>>> density = (2*L)/(N*(N-1))
>>> density
0.18947368421052632
>>>
```

Now we compute the degree of every node using the `Degree()` function and compute the mean degree $\langle k \rangle$ using the numpy method `array.mean()`.

```
>>> knodes = Degree(net)
>>> knodes
array([5, 3, 1, 3, 2, 6, 3, 4, 3, 3, 4, 5, 2, 3, 3, 6, 6, 3, 6, 1])
>>> meank = knodes.mean()
>>> meank
3.6000000000000001
>>>
```

GAlib works also with directed networks and, whenever applicable, functions include the optional boolean parameter `directed`. By default all GAlib functions and network generators that can be used with directed networks come specified for undirected networks, i.e. with parameter `directed=False`. In the following example we generate a random directed graph.

```
>>> dinet = ErdosRenyiGraph(N, p, directed=True)
>>> Ld = dinet.sum()
>>> Ld
68
>>> density = float(Ld) / (N*(N-1))
>>> density
0.17894736842105263
>>>
```

As a directed network, its nodes have different input and output degrees (in-k and out-k), therefore the `Degree()` function has to be called with the parameter `directed=True` and with two names for each of the arrays to be unpacked:

```
>>> inknodes, outknodes = Degree(dinet, True)
>>> inknodes
array([2, 4, 6, 1, 4, 2, 4, 2, 4, 6, 4, 2, 2, 2, 2, 5, 3, 5, 5, 3])
>>> outknodes
array([3, 3, 0, 3, 5, 8, 1, 2, 1, 4, 5, 4, 2, 3, 2, 7, 7, 1, 2, 5])
>>>
```

NOTE:

Notice that when functions are called for directed network measures, they often return 2-dimensional arrays that need to be adequately unpacked as in the example above.

Another popular graph measure is the clustering coefficient, that is, the fraction of triangles in a network out of all possible triangles the network could have. It is therefore a measure of transitivity or cohesiveness. A tree graph has no triangles and its clustering coefficient $C = 0$. On the contrary, a complete graph of size $N \geq 3$ has $C = 1$ because all nodes form triangles with all their neighbours. Additionally one can define the local clustering of individual nodes. The function `Clustering()` computes both the clustering coefficient of the network and the local clustering of every node,

returning a floating number between 0 and 1, and an array of length N with the local clustering of every node. Remember to adequately call the function to unpack both results. For the random graph generated above we have:

```
>>> clustcoef, clustnodes = Clustering(net)
>>> clustcoef
0.1271186440677966
>>> clustnodes
array([[ 0.3          ,  0.          ,  0.          ,  0.          ,  0.          ,
         0.13333333,  0.33333333,  0.          ,  0.          ,  0.          ,
         0.16666667,  0.          ,  0.          ,  0.33333333,  0.          ,
         0.13333333,  0.2          ,  0.33333333,  0.06666667,  0.          ]])
>>>
```

WARNING:

Notice that the clustering coefficient C and the mean of the local clustering are not equal. In the previous case, the mean value of the local clustering is:

```
>>> clustnodes.mean()
0.09999999999999992
```

that is different from the actual value `clustcoef`. This is not an error, but a well-known property which arises from the manner the local clustering is defined. Indeed, in random graphs the local clustering is known to anti-correlate with the degree of the node.

NOTE:

The function `Clustering()` only accepts undirected networks. The reason is that there is no agreed manner on how to define what a triangle is in directed networks and several approaches might be taken. In future releases GAlib will have support for Clustering in directed networks.

2.2) DATA I/O

Reading networks from files and saving them into files is done using the standard data I/O tools of numpy: functions `loadtxt()` and `savetxt()` are available to work with text files. Functions `load()` and `save()` work with the standard binary data format of numpy. For large datasets we recommend `load()` and `save()` because of their better performance. In the following example we save the random network created before into a file and read it again. Then we make sure that the network is the same using the `ArrayCompare()` function in the *gatools.py* module

```
>>> savetxt('filepath.txt', net, fmt='%d')
>>> newnet = loadtxt('filepath.txt', dtype=uint8)
>>> from gatools import*
>>> ArrayCompare(net, newnet)
True
>>>
```

to save and read the data as binary files, we could instead do the following:

```
>>> save('filepath.npy', net)
>>> newnet = load('filepath.npy')
>>> ArrayCompare(net, newnet)
True
>>>
```

Notice that `savetxt()` and `loadtxt()` require data type formatter options to be explicitly introduced, while `save()` and `load()` functions remember the dtype of the array. The function `ArrayCompare()` is a simple wrap around NumPy's array comparison utilities. When `a1` and `a2` are two NumPy arrays of the same shape, `a1 == a2` returns another array of the same shape with the element-wise result of the comparison. `ArrayCompare()` is True if all the elements are equal and False if there is at least one element in both arrays that is not equal.

GAlib also includes support to read and write network files in popular network formats used by other graph analysis software, e.g. Pajek. See the example script *DataConversions.py* in *GAtools/Examples*.

2.3) UTILITY SCRIPTS (EVEN FOR THE NON-PYTHON PROGRAMMERS)

GAlib includes several scripts useful for network scientists, independently of their usual programming environment or skills. These scripts are intended to easily perform some tedious tasks such as the generation of ensembles of random or rewired networks.

(Section to be continued...)

3) LIBRARY REFERENCE

(Section to be improved...)

GAlib consists of three modules: *gatoools.py*, *galib.py* and *gamodels.py*.

- *gatoools.py* : miscellaneous helper functions, e.g. data-type transformations.
- *galib.py* : basic graph descriptors, e.g. degrees and clustering.
- *galib_models.py* : Generation of synthetic networks and randomization.

3.1) GRAPH DESCRIPTORS (*galib.py*)

The module *galib.py* contains the core functions to perform graph analysis.

3.1.1) Basic connectivity descriptors

Degree(<i>net</i> [, <i>directed</i>])	Computes the number of neighbours of every node.
Intensity(<i>net</i> [, <i>directed</i>])	The total strength of a node in a weighted network.
Reciprocity(<i>net</i> [, <i>weighted</i>])	Fraction of reciprocal links.
ReciprocalDegree(<i>net</i> [, <i>normed</i>])	Reciprocity of every node and excess degrees.
AvNeighboursDegree(<i>net</i> [, <i>knntype</i> , <i>fulloutput</i>])	Mean neighbours' degree of nodes with degree <i>k</i> .
Clustering(<i>net</i>)	Clustering coefficient and clustering of every node.
RichClub(<i>net</i> [, <i>weighted</i> , <i>rctype</i>])	Density of subnetwork with degree > <i>k'</i> , for <i>k'</i> = 0 to <i>kmax</i> .
MatchingIndex(<i>net</i> [, <i>normed</i>])	Number of common neighbours of every pair of nodes.

3.1.2) Paths and graph distance

FloydWarshall(<i>net</i>)	Computes the graph distance between all pairs of nodes.
PathsAllinOne(<i>net</i>)	Computes several graph distance and path measures.
AllShortestPaths(<i>net</i> , <i>start</i> , <i>end</i> , <i>length</i>)	Finds all the Hamiltonian shortest paths between from node <i>start</i> to node <i>end</i> .

3.1.3) Components, modules, higher-order organization

AssortativityMatrix(<i>net</i> , <i>partition</i> [, <i>norm</i> , <i>maxweight</i>])	Returns the assortativity matrix of <i>net</i> given a partition.
ConnectedComponents(<i>distnet</i>)	Find groups of nodes, disconnected from each other.
Modularity(<i>net</i> , <i>partition</i> [, <i>degree</i>])	Computes the Newman modularity of <i>net</i> given a partition of nodes.
K_Core(<i>net</i> , <i>kmin</i>)	Finds the K-core of a network with degree <i>k</i> >= <i>kmin</i> .
K_Shells(<i>net</i>)	Returns the K-shells of a network for all <i>k</i> from <i>kmin</i> to <i>kmax</i> .

3.2) NETWORK GENERATION MODELS AND NETWORK RANDOMIZATION

3.2.1) Random network generators

Lattice1D(<i>N</i> , <i>z</i>)	Returns a ring lattices of <i>N</i> nodes, each connected to its 2 <i>z</i> closest neighbours.
WattsStrogatzGraph(<i>N</i> , <i>z</i> , <i>prew</i> [, <i>lattice</i>])	Returns a small-world network after the Watts & Strogatz model.
ErdosRenyiGraph(<i>N</i> , <i>p</i> [, <i>directed</i>])	Returns a random graphs after the Erdos & Renyi model.
RandomGraph(<i>N</i> , <i>L</i> [, <i>directed</i>])	Returns a random graph of <i>N</i> nodes and <i>L</i> links.
BarabasiAlbertGraph(<i>N</i> , <i>m0</i> , <i>m</i> [, <i>outdtype</i> =uint8])	Returns a scale-free network after the Barabasi & Albert model.
ScaleFreeGraph(<i>N</i> , <i>density</i> , <i>exponent</i> [, <i>directed</i>])	Returns a scale-free graph of size <i>N</i> and given exponent.

3.2.2) Network rewiring and randomization algorithms

RewireNetwork(<i>net</i> , <i>prewire</i> [, <i>directed</i> , <i>weighted</i>])	Rewires <i>prew</i> times the links of <i>net</i> conserving its degrees.
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3.2.3) Hierarchical and modular (HM) network models

HMpartition(<i>hmshape</i>)	Returns the partition of a HM network of given sizes per hierarchical scale.
HMRandomNetwork(<i>hmshape</i> , <i>avklist</i> [, <i>directed</i> , <i>outdtype</i>])	Returns a random hierarchical and modular network of the "matruschka" type.
RavaszBarabasiModel(<i>xxxxxx</i>)	HM networks of the type defined by Ravasz & Barabasi.

3.3) EXTRA TOOLS FOR THE GRAPH ANALYSIS LIBRARY (*gatoools.py*)

The module `GAtools.py` contains functions that are helpful in the analysis of graphs although they are not graph measures.

3.3.1) I/O and data conversions

<code>LoadLabels(filepath)</code>	Reads the labels of nodes from a file.
<code>SaveLabels(filepath, labels)</code>	Saves the labels of nodes into a file.
<code>ReadPartition(filepath)</code>	Reads from a file the nodes of a partition.
<code>SavePartition(filepath, partition)</code>	Saves a partition of nodes into a file.
<code>LoadFromPajek(filepath[, getlabels])</code>	Reads a network from a text file in Pajek format.
<code>Save2Pajek(filepath, net[, labels, directed])</code>	Saves a network into a text file in Pajek format.
<code>ExtractSubmatrix(net, nodelist1[, nodelist2])</code>	Returns the submatrix composed by given nodes.
<code>SymmetriseMatrix(net)</code>	Converts a directed network into undirected by averaging the weights.
<code>LaplacianMatrix(net)</code>	Computes the Laplacian matrix of network <code>net</code> .
<code>CleanPaths(pathlist)</code>	Removes opposite paths from undirected graphs.

3.3.2) Array and matrix comparisons

<code>ArrayCompare(array1, array2)</code>	Compares whether two arrays are identical or not.
<code>HammingDistance(array1, array2[, normed])</code>	Computes the Hamming distance of two arrays.

3.3.3) Additional math / combinatorics functions

<code>MinMax(data)</code>	Sorts entries of a dataset from smaller to larger.
<code>MaxMin(data)</code>	Sorts entries of a dataset from larger to smaller.
<code>NonZeroMin(data)</code>	Returns the smallest nonzero value in a numerical dataset.
<code>CumulativeDistribution(data, nbins[, nbins, range, normed])</code>	Computes the cumulative distribution of a dataset.
<code>Factorial(x)</code>	Returns the factorial of an integer number.
<code>BinomialCoefficient(n,m)</code>	Computes the binomial coefficient.
<code>StdDeviation(data)</code>	Mean value and standard deviation of a dataset.
<code>Quartiles(data)</code>	Finds the Q1, Q2 and Q3 quartiles of a dataset.
<code>AllPermutations(data)</code>	Given a set, it returns all possible permutations.
<code>AllCombinations(data)</code>	Given a set, finds all combinations of given size.
<code>AllBipartitions(data)</code>	Given a set, finds all its bipartitions.

4) ACKNOWLEDGMENTS

This library has been developed along several years as part of my scientific work. Therefore my main gratitude is for all the anonymous european and german tax-payers who have contributed to the financial support for my work. In return, GAlib is free for everyone to use, modify and extend after the terms in the copyright file included. I am also grateful to those institutions and organizations that have distributed the financial support in form of research grants: The Helmholtz Institute for Supercomputational Science, the University of Potsdam, the Bundesministerium für Bildung und Forschung (Germany), the Deutsche Forschungsgemeinschaft, the Bernstein Center for Computational Neuroscience, the Humboldt-Universität zu Berlin and the 7th Framework Programme for Research of the European Commission.

I also owe my gratitude to the developers of Ipython and to Enthought (for providing the Enthought Python Distribution, now Canopy) for providing the tools I work with every day and simplifying my life such that I could concentrate on the coding and on my research.

APPENDIX: ON CODE STYLE AND PEP-8

I have tried to follow all recommendations in PEP-8 (Style Guide for Python Code) with the exception of the rules for naming functions. In GAlib I use CamelCase for the names of the functions for several reasons. Contrary to the main philosophy behind the style guides in PEP-8, that code is more often read than written, I spend 80% of my time writing code (or working interactively) and only 20% reading my code. I very much disagree with the two main recommendations in PEP-8 to name functions:

- names of functions should be lowercase.
- functions should have short names.

First, naming functions in lowercase is to give functions the same hierarchical importance of variables and, in my opinion, this is not acceptable. Second, when giving functions very short names there is a very strong risk to accidentally overwrite functions while writing new code or working interactively in the shell. This happens to me very often when

working with NumPy, whose names for functions follow very close to Matlab's functions names. Short function names could be useful when working interactively but given that any proper interactive shell has tab-completion capacities, this is not so important. As an example, NumPy's functions to declare an array as a matrix are `mat()` and `matrix()`, two names one would always like to have free to name their variables. This forces you to declare variable in silly and complicated ways as for example:

```
somematrix = mat(somedata)
or
somematrix = matrix(somedata)
```

with the very important difference that the variable `somematrix` has been declared to be used later on and the function `mat()` will not be used again. Therefore I would prefer that those functions are named `toMatrix()` or `Matrix()`, then I could just declare:

```
mat = Matrix(somedata)
```

so that the variable `mat`, which will be used often in the script has a shorter name.

In summary, naming functions with short names in lowercase does not save typing because it forces you to give variables longer names to distinguish them from the functions, with the difference that variables are more often used in the code while functions are called just once or twice in a script.