
A beginners guide to solving biological problems in R

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Day 1 schedule

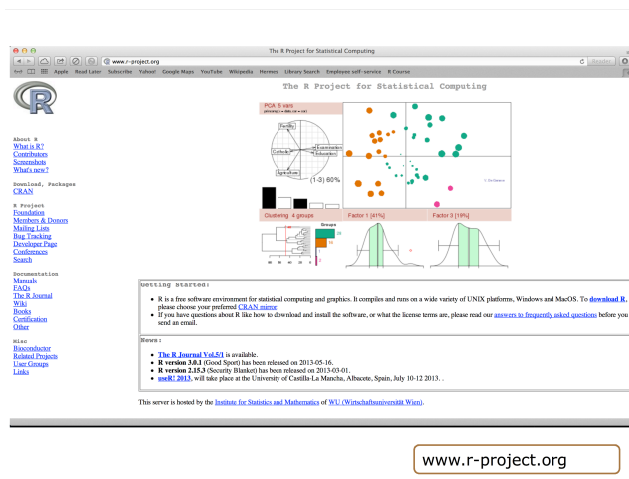
1. Introduction to R and its environment
2. Data structures
3. Data analysis example
4. Programming techniques
5. Statistics

Introduction to R and its environment

1

What's R?

- A statistical programming environment
 - based on S
 - Suited to high level data analysis
- Open source & cross platform
- Extensive graphics capabilities
- Diverse range of add-on packages
- Active community of developers
- Thorough documentation



www.r-project.org

Various platforms supported

- Release 3.1.0 (April 2014)
 - Base package
 - Contributed packages (general purposes extras)
 - >5400 available packages
- Download from <http://www.stats.bris.ac.uk/R/>
- Windows, Mac and Linux versions available
- Executed using command line, or a graphical user interface (GUI)
- On this course, we use the RStudio GUI (www.rstudio.com)
- Everything you need is installed on the training machines
- If you are using your own machine, download both R and RStudio

Getting Started

- R is a program which, once installed on your system, can be launched and is immediately ready to take input directly from the user
- There are two ways to launch R:
 - 1) From the command line (particularly useful if you're quite familiar with Linux)
 - 2) As an application called RStudio (very good for beginners)

Prepare to launch R

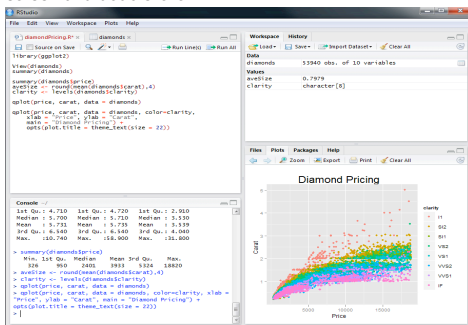
From command line

- To start R in Linux we need to enter the Linux console (also called Linux terminal and Linux shell)
- To start R, at the prompt simply type:
\$ R
- If R doesn't print the welcome message, call us to help!

Prepare to launch R

Using RStudio

- To launch RStudio, find the RStudio icon in the menu bar on the left of the screen and double-click



The Working Directory (wd)

- Like many programs R has a concept of a working directory (wd)
- It is the place where R will look for files to execute and where it will save files, by default
- For this course we need to set the working directory to the location of the course scripts
- At the command prompt in the terminal or in RStudio console type:

```
> setwd("R_course/Day_1_scripts")
```

- Alternatively in RStudio use the mouse and browse to the directory location
- Session → Set Working Directory → Choose Directory...

Basic concepts in R command line calculation

- The command line can be used as a calculator. Type:

```
> 2 + 2  
[1] 4
```

```
> 20/5 - sqrt(25) + 3^2  
[1] 8
```

```
> sin(pi/2)  
[1] 1
```

- Note: The number in the square brackets is an indicator of the position in the output. In this case the output is a 'vector' of length 1 (i.e. a single number). More on vectors coming up...

Basic concepts in R variables

- A variable is a letter or word which takes (or contains) a value. We use the assignment 'operator', `<-`

```
> x <- 10  
> x  
[1] 10  
> myNumber <- 25  
> myNumber  
[1] 25
```

- We can perform arithmetic on variables:

```
> sqrt(myNumber)  
[1] 5
```

- We can add variables together:

```
> x + myNumber  
[1] 35
```

Basic concepts in R variables

- We can change the value of an existing variable:

```
> x <- 21
> x
[1] 21
```

- We can set one variable to equal the value of another variable:

```
> x <- myNumber
> x
[1] 25
```

- We can modify the contents of a variable:

```
> myNumber <- myNumber + sqrt(16)
[1] 29
```

Basic concepts in R functions

- **Functions** in R perform operations on **arguments** (the input(s) to the function). We have already used **sin(x)** which returns the sine of **x**. In this case the function has one argument, **x**. Arguments are *always* contained in parentheses, i.e. curved brackets **()**, separated by commas.

- Try these:

```
> sum(3, 4, 5, 6)
[1] 18
> max(3, 4, 5, 6)
[1] 6
> min(3, 4, 5, 6)
[1] 3
```

- Arguments can be named or unnamed, but if they are unnamed they must be ordered (we will see later how to find the right order).

```
> seq(from=2, to=10, by=2)
[1] 2 4 6 8 10
> seq(2, 10, 2)
[1] 2 4 6 8 10
```

Basic concepts in R vectors

- The basic data structure in R is a **vector** – an ordered collection of values. R even treats single values as 1-element vectors. The function **c()** *combines* its arguments into a vector:

```
> x <- c(3, 4, 5, 6)
> x
[1] 3 4 5 6
```

- As mentioned, the square brackets **[]** indicate position within the vector (the **index**). We can extract individual elements by using the **[]** notation:

```
> x[1]
[1] 3
> x[4]
[1] 6
```

- We can even put a vector inside the square brackets (vector indexing):

```
> y <- c(2, 3)
> x[y]
[1] 4 5
```

Basic concepts in R vectors

- There are a number of shortcuts to create a vector. Instead of:

```
> x <- c(3, 4, 5, 6, 7, 8, 9, 10, 11, 12)
```

- we can write:

```
> x <- 3:12
```

- or we can use the **seq()** function, which returns a vector:

```
> x <- seq(2, 10, 2)
```

```
> x
```

```
[1] 2 4 6 8 10
```

```
> x <- seq(2, 10, length.out = 7)
```

- > x

```
[1] 2.00000 3.33333 4.66667 6.00000 7.33333 8.66667 10.00000
```

- or the **rep()** function:

```
> y <- rep(3, 5)
```

- > y

```
[1] 3 3 3 3 3
```

```
> y <- rep(1:3, 5)
```

```
> y
```

```
[1] 1 2 3 1 2 3 1 2 3 1 2 3
```

Basic concepts in R vectors

- We have seen some ways of extracting elements of a vector. We can use these shortcuts to make things easier (or more complex!)

```
> x <- 3:12
```

```
> x[3:7]
```

```
[1] 5 6 7 8 9
```

```
> x[seq(2, 6, 2)]
```

```
[1] 4 6 8
```

```
> x[rep(3, 2)]
```

```
[1] 5 5
```

- We can add an element to a vector

```
> y <- c(x, 1)
```

```
> y
```

```
[1] 3 4 5 6 7 8 9 10 11 12 1
```

- We can glue vectors together

```
> z <- c(x, y)
```

```
> z
```

```
[1] 3 4 5 6 7 8 9 10 11 12 3 4 5 6 7 8 9 10 11 12 1
```

Basic concepts in R vectors

- We can remove element(s) from a vector

```
> x <- 3:12
```

```
> x[-3]
```

```
[1] 3 4 6 7 8 9 10 11 12
```

```
> x[-(5:7)]
```

```
[1] 3 4 5 6 10 11 12
```

```
> x[-seq(2, 6, 2)]
```

```
[1] 3 5 7 9 10 11 12
```

- Finally, we can modify the contents of a vector

```
> x[6] <- 4
```

```
> x
```

```
[1] 3 4 5 6 7 4 9 10 11 12
```

```
> x[3:5] <- 1
```

```
> x
```

```
[1] 3 4 1 1 1 4 9 10 11 12
```

- Remember! **Square** brackets for indexing **[]**, **parentheses** for function arguments **()**.

Basic concepts in R

vector arithmetic

- When applying all standard arithmetic operations to vectors, application is element-wise

```
> x <- 1:10
> y <- x*2
> y
[1] 2 4 6 8 10 12 14 16 18 20
> z <- x^2
> z
[1] 1 4 9 16 25 36 49 64 81 100
```

- Adding two vectors

```
> y + z
[1] 3 8 15 24 35 48 63 80 99 120
```

- If vectors are not the same length, the shorter one will be recycled:

```
> x + 1:2
[1] 2 4 4 6 6 8 8 10 10 12
```

- But be careful if the vector lengths aren't factors of each other:

```
> x + 1:3
```

Basic concepts in R

Character vectors and naming

- All the vectors we have seen so far have contained numbers, but we can also store strings in vectors – this is called a **character** vector.

```
> gene.names <- c("Pax6", "Beta-actin", "FoxP2", "Hox9")
```

- We can name elements of vectors using the **names** function, which can be useful to keep track of the meaning of our data:

```
> gene.expression <- c(0,3.2,1.2,-2)
```

```
> gene.expression
```

```
[1] 0.0 3.2 1.2 -2.0
```

```
> names(gene.expression) <- gene.names
```

```
> gene.expression
```

```
      Pax6 Beta-actin   FoxP2   Hox9
      0.0      3.2      1.2    -2.0
```

- We can also use the **names** function to get a vector of the names of an object:

```
> names(gene.expression)
```

```
[1] "Pax6"      "Beta-actin" "FoxP2"      "Hox9"
```

Exercise: genes and genomes

- Let's try some vector arithmetic. Here are the genome lengths and number of protein coding genes for several model organisms:

Species	Genome size (Mb)	Protein coding genes
<i>Homo sapiens</i>	3,102	20,774
<i>Mus musculus</i>	2,731	23,139
<i>Drosophila melanogaster</i>	169	13,937
<i>Caenorhabditis elegans</i>	100	20,532
<i>Saccharomyces cerevisiae</i>	12	6,692

- Create **genome.size** and **coding.genes** vectors to hold the data in each column using the **c** function. Create a **species.name** vector and use this vector to name the values in the other two vectors.

Exercise: genes and genomes

- Let's assume a coding gene has an average length of 1.5 kilobases. On average, how many base pairs of each genome is made of coding genes? Create a new vector to record this called **coding.bases**.
- What percentage of each genome is made up of protein coding genes? Use your **coding.bases** and **genome.size** vectors to calculate this. (See earlier slides for how to do division in R.)
- How many times more bases are used for coding in the human genome compared to the yeast genome? How many times more bases are in the human genome in total compared to the yeast genome? Look up indices of your vectors to find out.

Answers to genome exercise

- Creating vectors:

```
> genome.size<-c(3102,2731,169,100,12)
> coding.genes<-c(20774,23139,13937,20532,6692)
> species.name<-c("H. sapiens","M. musculus","D. melanogaster","C. elegans","S. cerevisiae")
> names(genome.size)<-species.name
> names(coding.genes)<-species.name
```

- To calculate the number of coding bases, we need to use the same scale as we used for genome size: 1.5 kilobases is 0.0015 Megabases.

```
> coding.bases<-coding.genes*0.0015
> coding.bases
      H. sapiens      M. musculus D. melanogaster      C. elegans      S. cerevisiae
      31.1610         34.7085         20.9055         30.7980         10.0380
```

Answers to genome exercise

- To calculate the percentage of coding bases in each genome:

```
> coding.pc<-coding.bases/genome.size*100
> coding.pc
      H. sapiens      M. musculus D. melanogaster      C. elegans      S. cerevisiae
      1.004545         1.270908         12.370118         30.798000         83.650000
```

- To compare human to yeast:

```
> coding.bases[1]/coding.bases[5]
H. sapiens
3.104304
> genome.size[1]/genome.size[5]
H. sapiens
258.5
```

- Note that if a new vector is created using a named vector, the names are usually carried across to the new vector. Sometimes this is what we want (as for **coding.pc**) but sometimes it is not (when we are comparing human to yeast). We can remove names by setting them to the special NULL value:

```
> names(coding.pc)<-NULL
> coding.pc
[1] 1.004545 1.270908 12.370118 30.798000 83.650000
```

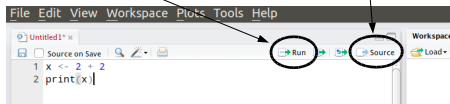
Writing scripts with Rstudio

Typing lots of commands directly to R can be tedious. A better way is to write the commands to a file and then load it into R.

- Click on **File -> New** in Rstudio
- Type in some R code, e.g.

```
x <- 2 + 2  
print(x)
```

- Click on **Run** to execute the **current line**, and **Source** to execute the **whole script**



Sourcing can also be performed manually with `source("myScript.R")`

Getting Help

- To get help on any R function, type `?` followed by the function name. For example:

```
> ?seq
```
- This retrieves the syntax and arguments for the function. You can see the default order of arguments here. The help page also tells you which **package** it belongs to.
- There will typically be example usage, which you can test using the **example** function:

```
> example(seq)
```
- If you can't remember the exact name type `??` followed by your guess. R will return a list of possibles

```
> ??plot
```

Interacting with the R console

- R console symbols
 - `;` end of line
 - Enables multiple commands to be placed on one line of text
 - `#` comment
 - indicates text is a comment and not executed
 - `+` command line wrap
 - R is waiting for you to complete an expression
- **Ctrl-c** or **escape** to clear input line and try again
- **Ctrl-l** to clear window
- Press **q** to leave help (using R from the terminal)
- Use the **TAB key** for command auto completion
- Use **up and down arrows** to scroll through the command history

R packages

- R comes ready loaded with various libraries of functions called **packages**. e.g. the function **sum()** is in the **base** package and **sd()**, which calculates the standard deviation of a vector, is in the **stats** package
- There are 1000s of additional packages provided by third parties, and the packages can be found in numerous server locations on the web called **repositories**
- The two repositories you will come across the most are
 - **The Comprehensive R Archive Network (CRAN)**
 - **Bioconductor**
- CRAN is mirrored in many locations. Set your local mirror in RStudio using Tools → Options, and choose a CRAN mirror
- Set the Bioconductor package download tool by typing:

```
> source("http://bioconductor.org/biocLite.R")
```
- Bioconductor packages are then loaded with the biocLite() function:

```
> biocLite("PackageName")
```

R packages

- 5400+ packages on CRAN:
 - Use CRAN search to find functionality you need:
<http://cran.r-project.org/search.html>
 - Or, look for packages by theme:
<http://cran.r-project.org/web/views/>
- 750 packages in Bioconductor:
 - Specialised in genomics:
<http://www.bioconductor.org/packages/release/bioc/>
- **Other repositories:**
- 1700+ projects on R-forge:
 - <http://r-forge.r-project.org/>
- R graphical manual:
 - <http://rgm3.lab.nig.ac.jp/RGM>

Bottomline: **always** first look if there is already an R package that does what you want before trying to implement it yourself

Exercise: Install Packages ggplot and DESeq

- ggplot2 is a commonly used graphics package (we will try it tomorrow).
 - Use **install.packages()** function...

```
install.packages("ggplot2")
```
 - or in RStudio goto Tools → Install Packages... and type the package name
- DESeq is a BioConductor package (www.bioconductor.org)
 - Use **biocLite()** function

```
biocLite("DESeq")
```
- R needs to be told to use the new functions from the installed packages
 - Use **library(...)** function to load the newly installed features

```
library(ggplot2) # loads ggplot functions
```

```
library(DESeq) # loads DESeq functions
```
 - **library()**
 - Lists all the packages you've got installed locally

Data structures

2

R is designed to handle experimental data

- Although the basic unit of R is a vector, we usually handle data in **data frames**.
- A data frame is a set of observations of a set of variables – in other words, the outcome of an experiment.
- For example, we might want to analyse information about a set of patients. To start with, let's say we have ten patients and for each one we know their name, sex, age, weight and whether they give consent for their data to be made public.

The patients data frame

We are going to create a data frame called 'patients', which will have ten rows (observations) and seven columns (variables). The columns must all be equal lengths.

	First_Name	Second_Name	Full_Name	Sex	Age	Weight	Consent
1	Adam	Jones	Adam Jones	Male	50	70.8	TRUE
2	Eve	Parker	Eve Parker	Female	21	67.9	TRUE
3	John	Evans	John Evans	Male	35	75.3	FALSE
4	Mary	Davis	Mary Davis	Female	45	61.9	TRUE
5	Peter	Baker	Peter Baker	Male	28	72.4	FALSE
6	Paul	Daniels	Paul Daniels	Male	31	69.9	FALSE
7	Joanna	Edwards	Joanna Edwards	Female	42	63.5	FALSE
8	Matthew	Smith	Matthew Smith	Male	33	71.5	TRUE
9	David	Roberts	David Roberts	Male	57	73.2	FALSE
10	Sally	Wilson	Sally Wilson	Female	62	64.8	TRUE

Let's see how we can construct this from scratch.

Character, numeric and logical data types

- Each column is a vector, like previous vectors we have seen, for example:

```
> age<-c(50, 21, 35, 45, 28, 31, 42, 33, 57, 62)
> weight<-c(70.8, 67.9, 75.3, 61.9, 72.4, 69.9, 63.5, 71.5, 73.2, 64.8)
```
- We can define the names using character vectors:

```
> firstName<- c("Adam", "Eve", "John", "Mary", "Peter", "Paul", "Joanna",
"Matthew", "David", "Sally")
> secondName<-c("Jones", "Parker", "Evans", "Davis", "Baker", "Daniels",
"Edwards", "Smith", "Roberts", "Wilson")
```
- We also have a new type of vector, the **logical** vector, which only contains the values TRUE and FALSE:

```
> consent<-c(TRUE,TRUE,FALSE,TRUE,FALSE,FALSE,FALSE,TRUE,FALSE,TRUE)
```

Character, numeric and logical data types

- Vectors can only contain one type of data; we cannot mix numbers, characters and logical values in the same vector. If we try this, R will convert everything to characters:

```
> c(20, "a string", TRUE)
[1] "20"      "a string" "TRUE"
```
- We can see the type of a particular vector using the **mode** function:

```
> mode(firstName)
[1] "character"
> mode(age)
[1] "numeric"
> mode(weight)
[1] "numeric"
> mode(consent)
[1] "logical"
```

Factors

- Character vectors are fine for some variables, like names.
- But sometimes we have categorical data and we want R to recognize this.
- A factor is R's data structure for categorical data.

```
> sex<-c("Male", "Female", "Male", "Female", "Male", "Male", "Female",
"Male", "Male", "Female")
> sex
[1] "Male"  "Female" "Male"  "Female" "Male"  "Male"  "Female" "Male"
"Male"  "Female"
> factor(sex)
[1] Male  Female Male  Female Male  Male  Female Male  Female
Levels: Female Male
```
- R has converted the strings of the sex character vector into two **levels**, which are the categories in the data.
- Note the values of this factor are not character strings, but levels.
- We can use this factor to compare data for males and females.

Creating a data frame (first attempt)

- We can construct a data frame from other objects:

```
> patients<-data.frame(firstName, secondName, paste(firstName,secondName),
sex, age, weight, consent)
> patients
  firstName secondName paste.firstName..secondName. sex age weight consent
1      Adam      Jones      Adam Jones      Male  50   70.8      TRUE
2       Eve      Parker      Eve Parker      Female  21   67.9      TRUE
3      John      Evans      John Evans      Male   35   75.3     FALSE
4      Mary      Davis      Mary Davis      Female  45   61.9      TRUE
5     Peter      Baker      Peter Baker      Male   28   72.4     FALSE
6      Paul    Daniels      Paul Daniels      Male   31   69.9     FALSE
7   Joanna    Edwards    Joanna Edwards      Female  42   63.5     FALSE
8  Matthew      Smith    Matthew Smith      Male   33   71.5      TRUE
9    David    Roberts    David Roberts      Male   57   73.2     FALSE
10   Sally     Wilson     Sally Wilson      Female  62   64.8      TRUE
```

- The **paste** function joins character vectors together.
- We can access particular variables using the **dollar** operator:

```
> patients$age
[1] 50 21 35 45 28 31 42 33 57 62
```

Naming data frame variables

- R has inferred the names of our data frame variables from the names of the vectors or the commands (eg the paste command).
- We can name the variables after we have created a data frame using the **names** function, and we can use the same function to see the names:

```
> names(patients)<-c("First_Name", "Second_Name", "Full_Name", "Sex",
"Age", "Weight", "Consent")
> names(patients)
[1] "First_Name" "Second_Name" "Full_Name" "Sex" "Age"
"Weight" "Consent"
```

- Or we can name the variables when we define the data frame:

```
> patients<-data.frame(First_Name=firstName, Second_Name=secondName,
Full_Name=paste(firstName,secondName), Sex=sex, Age=age, Weight=weight,
Consent=consent)
> names(patients)
[1] "First_Name" "Second_Name" "Full_Name" "Sex" "Age"
"Weight" "Consent"
```

Factors in data frames

- When creating a data frame, R assumes all character vectors should be categorical variables and converts them to factors. This is not always what we want:

```
> patients$firstName
[1] Adam Eve John Mary Peter Paul Joanna Matthew David Sally
Levels: Adam David Eve Joanna John Mary Matthew Paul Peter Sally
```

- We can avoid this by asking R not to treat strings as factors, and then explicitly stating when we want a factor by using **factor**:

```
> patients<-data.frame(First_Name=firstName, Second_Name=secondName,
Full_Name=paste(firstName,secondName), Sex=factor(sex), Age=age,
Weight=weight, Consent=consent, stringsAsFactors=FALSE)
> patients$Sex
[1] Male Female Male Female Male Male Female Male Male Female
Levels: Female Male
> patients$First_Name
[1] "Adam" "Eve" "John" "Mary" "Peter" "Paul" "Joanna"
"Matthew" "David" "Sally"
```

Matrices

`matrix(..., ncol=..., nrow=...)`

- Data frames are R's speciality, but R also handles matrices:

```
> e <- matrix(1:10, nrow=5, ncol=2)
> e
     [,1] [,2]
[1,]    1    6
[2,]    2    7
[3,]    3    8
[4,]    4    9
[5,]    5   10
> f <- matrix(1:10, nrow=2, ncol=5)
> f
     [,1] [,2] [,3] [,4] [,5]
[1,]    1    3    5    7    9
[2,]    2    4    6    8   10
> f %*% e
     [,1] [,2]
[1,]   95  220
[2,]  110  260
```

The `%*%` operator is the matrix multiplication operator, not the standard multiplication operator.

Lists

`list(name1=obj1, name2=obj2, ...)`

- We have seen that vectors can only hold data of one type. How can we store data of multiple types? Or vectors of different lengths in one object?
- We can use lists. A list can contain objects of any type.

```
one.to.ten <- 1:10
uniform.mat <- matrix(runif(100), ncol=10, nrow=10)
year.to.october <- data.frame(one.to.ten, month.name[1:10])
```

```
myList <- list( ls.obj.1=one.to.ten, ls.obj.2=uniform.mat,
ls.obj.3=year.to.october )
names(myList)
```

- We can use the dollar syntax to access list items (in fact, a data frame is a special type of list):

```
myList$ls.obj.1
```

- We can also use `myList[[1]]` to get the first item in the list.
- (For the curious: this double indexing is necessary because lists are in fact just like vectors – they can only contain one type of object. But one of the types they can contain is a list. So any list like the above is actually a list of lists; the first element `myList[1]` is a list containing a vector, and so we need double indexing to actually get the vector.)

Indexing data frames and matrices

Special cases:
`a[i,]` i-th row
`a[, j]` j-th column

- You can index multidimensional data structures like matrices and data frames using commas. If you don't provide an index for either rows or columns, all of the rows or columns will be returned.

```
object [ rows , columns ]

> e[1,2]
[1] 6
> e[1,]
[1] 1 6
> patients[1,2]
[1] "Jones"
> patients[1,]
  First_Name Second_Name Full_Name Sex Age Weight Consent
1       Adam      Jones Adam Jones Male   50   70.8   TRUE
```

Advanced indexing

- As values in R are really vectors, so indices are actually vectors, and can be numeric or logical:

```
> s <- letters[1:5]
> s[c(1,3)]
[1] "a" "c"
> s[c(TRUE, FALSE, TRUE, FALSE, FALSE)]
[1] "a" "c"
> a<-1:5
> a<3
[1] TRUE TRUE FALSE FALSE FALSE
> s[a<3]
[1] "a" "b"
> s[a>1 & a<3]
[1] "b"
> s[a==2]
[1] "b"
```

Operators

- arithmetic

$+$, $-$, $*$, $/$, $^$

- comparison

$<$, $>$, $<=$, $>=$, $==$, $!=$

- logical

$!$, $&$, $|$, xor

(equal to, not equal to)

these always return
logical values !
(TRUE, FALSE)

Exercise

- Create a data frame called **my.patients** using the instructions in the slides. Change the data if you like.
- Check you have created the data frame correctly by loading the original version from this file in the *Day_1_scripts* folder using **source**:

```
> source("1.2_patients.R")
```
- Remake your data frame with three new variables: country, continent, and height. Make up the data. Make country a character vector but continent a factor.
- Try the **summary** function on your data frame. What does it do? How does it treat vectors (numeric, character, logical) and factors? (What does it do for matrices?)
- Use logical indexing to select the following patients:
 - Patients under 40
 - Patients who give consent to share their data
 - Men who weigh as much or more than the average European male (70.8 kg)

Logical indexing answers

- Patients under 40:
`> patients[patients$Age<40,]`
- Patients who give consent to share their data:
`> patients[patients$Consent==TRUE,]`
- Men who weigh as much or more than the average European male (70.8 kg):
`> patients[patients$Sex=="Male" & patients$Weight>=70.8,]`

R for data analysis

3

3 steps to Basic data analysis

1. Reading in data
 - `read.table()`
 - `read.csv()`, `read.delim()`
2. Analysis
 - Manipulating & reshaping the data
 - Any maths you like
 - Plotting the outcome
 - High level plotting functions (covered tomorrow)
3. Writing out results
 - `write.table()`
 - `write.csv()`

A simple walkthrough

Exemplifies 3 steps to R analysis

- 50 neuroblastoma patients were tested for NMYC gene copy number by interphase nuclei FISH
 - Amplification of NMYC correlates with worse prognosis
 - We have count data
 - Numbers of cells per patient assayed
 - For each we have NMYC copy number relative to base ploidy
- We need to determine which patients have amplifications
 - (i.e >33% of cells show NMYC amplification)

Step 1.

Read in the data

Patient	Nuclei	NB Amp	NB Nor	NB Del
1	44	0	41	3
2	67	3	58	6
3	33	7	26	0
4	36	6	30	0
5	51	5	45	1
6	43	0	38	5
7	64	1	56	7
8	58	2	49	7
9	56	0	53	3
10	66	0	56	10
11	33	13	19	1

This data is a tab delimited text file
Each row is a record, each column is a field
Columns are separated by tabs in the text.

We need to read in the results table and assign it to an object (rawData)

```
rawData <- read.delim("1.3_NBcountData.txt")
rawData[1:10,] # View the first 10 rows to ensure import is OK
               # Note data frame contains a patient index column
```

If the data had been comma separated values, then sep=","

```
read.csv("1.3_NBcountData.csv")
?read.table for a full list of arguments
```

1.3_NBcountData.R
(script commands)

1.3_NBcountData.txt
(data file)

Handling missing values

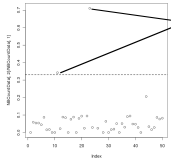
- The data frame contains some 'NA' values, which means the values are missing – a common occurrence in real data collection.
- NA is a special value that can be present in objects of any type (logical, character, numeric etc).
- NA is not the same as NULL. NULL is an empty R object. NA is one missing value within an R object (like a data frame or a vector).
- Often R functions will handle NAs gracefully, but sometimes we have to tell the functions what to do with them. R has some built-in functions for dealing with NAs, and functions often have their own arguments (like na.rm) for handling them.

```
> x<-c(1,NA,3)
> mean(x)
[1] NA
> mean(x,na.rm=TRUE)
[1] 2
> mean(na.omit(x))
[1] 2
> is.na(x)
[1] FALSE TRUE FALSE
```

Step 2.

Analysis (reshaping data & maths)

- Our analysis involves identifying patients with > 33% NB amplification
 - `prop <- rawData$NB_Amp / rawData$Nuclei` # create an index of results
 - `amp <- which(prop > 0.33)` # Get sample names of amplified patients
- We can plot a simple chart of the % NB amplification
 - `plot(prop, ylim=c(0,1))`
 - `abline(h=0.33)`



These 2 samples are amplified (11 & 23)

Step 3.

Outputting the results

- We write out a data frame of results (patients > 33% NB amplification) as a 'comma separated values' text file
 - `write.csv(rawData[amp,], file="selectedSamples.csv")` # Export table, file name = selectedSamples.csv
 - Files are directly readable by Excel and Calc
- Its often helpful to double check where the data has been saved
 - Use get working directory function
 - `getwd()` # print working directory

Data analysis exercise:

Which samples are near normal?

- Patients are near normal if:

`(NB_Amp/Nuclei < 0.33 & NB_Del == 0)`

- Modify the condition in our previous code to find these patients
- Write out a results file of the samples that match these criteria, and open it in a spreadsheet program

1.3_NBcountData.R
(script commands)

Solution to NB normality test

Basic data analysis

```
> norm <- which( prop < 0.33 & rawData$NB_Del==0)
> norm

[1] 3  4  7 15 20 24 36 37 42 47

> write.csv(rawData[norm,], "My_NB_output.csv")
```

R programming techniques

4

Basic R 'Built-in' functions for working with objects

- R has many built-in functions for doing simple calculations on objects. Start with a random sample of 15 numbers from 1 to 100 and try the functions below.

```
> x<-sample(100,15)
```

- Arithmetic with vectors
 - Min / Max value number in a series

```
min(x) ; max(x)
```

- Sum of values in a series

```
sum(x)
```

- Average estimates (mean / median)

```
mean(x) ; median(x)
```

- Range of values in a series

```
range(x)
```

- Variance

```
var(x)
```

- Arithmetic with vectors
 - Rank ordering

```
rank(x)
```

- Quantiles

```
quantile(x) ; boxplot(x)
```

- Square Root

```
sqrt(x)
```

- Standard deviation

```
sd(x)
```

- Trigonometry functions

```
tan(x) ; cos(x) ; sin(x)
```

Basic R 'Built-in' functions for working with data frames

- We have seen before how we can get the **names** of our variables, but for dataframes and matrices we can also get these names with **colnames**, and the names of the rows with **rownames**:

```
> names(patients)
[1] "First_Name" "Second_Name" "Full_Name" "Sex" "Age" "Weight" "Consent"
> colnames(patients)
[1] "First_Name" "Second_Name" "Full_Name" "Sex" "Age" "Weight" "Consent"
> rownames(patients)
[1] "1" "2" "3" "4" "5" "6" "7" "8" "9" "10"
```

We can get the numbers of rows or columns with **nrow** and **ncol**:

```
> nrow(patients)
[1] 10
> ncol(patients)
[1] 7
```

We can also find the length of a vector or a list with **length**, although this may give confusing results for some structures, like data frames:

```
> length(c(1,2,3,4,5))
[1] 5
> length(patients)
[1] 7
> length(patients$Age)
[1] 10
```

Remember, a data frame is a list of variables, so its length is the number of variables. The length of one of the variable vectors (like Age) is the number of observations.

Basic R 'Built-in' functions for working with data frames

We can add rows or columns to a data frame using **rbind** and **cbind**:

```
> newpatient<-c("Kate","Lawson","Kate Lawson","Female","35","62.5","TRUE")
> rbind(patients,newpatient)
```

	First_Name	Second_Name	Full_Name	Sex	Age	Weight	Consent
1	Adam	Jones	Adam Jones	Male	50	70.8	TRUE
2	Eve	Parker	Eve Parker	Female	21	67.9	TRUE
3	John	Evans	John Evans	Male	35	75.3	FALSE
4	Mary	Davis	Mary Davis	Female	45	61.9	TRUE
5	Peter	Baker	Peter Baker	Male	28	72.4	FALSE
6	Paul	Daniels	Paul Daniels	Male	31	69.9	FALSE
7	Joanna	Edwards	Joanna Edwards	Female	42	63.5	FALSE
8	Matthew	Smith	Matthew Smith	Male	33	71.5	TRUE
9	David	Roberts	David Roberts	Male	57	73.2	FALSE
10	Sally	Wilson	Sally Wilson	Female	62	64.8	TRUE
11	Kate	Lawson	Kate Lawson	Female	35	62.5	TRUE

```
> cbind(patients,10:1)
```

We can also remove rows and columns:

```
patients[-1,] # remove first row
patients[,-1] # remove first column
```

Basic R 'Built-in' functions for working with data frames

Sorting a vector with **sort**:

```
> sort(patients$Second_Name)
[1] "Baker" "Daniels" "Davis" "Edwards" "Evans" "Jones" "Parker" "Roberts" "Smith"
"Wilson"
```

Sorting a data frame by one variable with **order**:

```
> order(patients$Second_Name)
[1] 5 6 4 7 3 1 2 9 8 10
> patients[order(patients$Second_Name),]
  First_Name Second_Name Full_Name Sex Age Weight Consent
5      Peter      Baker  Peter Baker  Male  28  72.4  FALSE
6      Paul    Daniels   Paul Daniels  Male  31  69.9  FALSE
4      Mary     Davis   Mary Davis  Female  45  61.9   TRUE
7    Joanna   Edwards  Joanna Edwards  Female  42  63.5  FALSE
3      John     Evans   John Evans   Male  35  75.3  FALSE
1      Adam     Jones   Adam Jones   Male  50  70.8   TRUE
2       Eve     Parker   Eve Parker  Female  21  67.9   TRUE
9     David   Roberts  David Roberts  Male  57  73.2  FALSE
8   Matthew     Smith  Matthew Smith  Male  33  71.5   TRUE
10    Sally    Wilson   Sally Wilson  Female  62  64.8   TRUE
```

The R workspace

- The objects we have been making are created in the R workspace.
- When we load a package, we are loading that package's functions and data sets into our workspace.
- You can see what is in your workspace with **ls**:

```
> ls()
```
- You can attach data frames to your workspace and then refer to the variables directly:

```
> attach(patients)
> Full_Name
```
- You can remove objects from the workspace with **rm**:

```
> x<-1:5
[1] 1 2 3 4 5
> rm(x)
> x
Error: object 'x' not found
```
- You can remove everything by giving **rm** a list of all the objects returned by **ls**:

```
> rm(list=ls())
```

The R workspace

- Your workspace is like an unsaved Word document.
- When you quit R, it will usually save your workspace to a hidden file called '.Rdata' in your current directory. This workspace will be loaded again if you open R in the same directory.
- This file is a binary, computer-readable file, not a human-readable file, which you have to open with R (like a Word document in Office).
- It is safer to explicitly save your workspace using **save.image**:

```
> save.image("phd.chapter.1.R")
```
- This way, if you are working on several different projects, you can make sure the objects for each project are saved to named files, rather than trying to remember which directory you were working in, or risking overwriting some objects you forgot about and need later.
- To load a particular image, use **load**:

```
> load("phd.chapter.1.R")
```

Packages in the R workspace

- You can see which packages are loaded into your workspace with **search**:

```
> search()
[1] ".GlobalEnv"      "tools:rstudio"   "package:stats"   "package:graphics"
[5] "package:grDevices" "package:utils"   "package:datasets" "package:methods"
[9] "Autoloads"       "package:base"
```
- **.GlobalEnv** is where all the objects you create are stored.
- Most of the core functions are in **stats**, **utils**, **methods** and **base**.
- We will cover **graphics** and **grDevices** tomorrow afternoon.
- **Search** shows the search path R runs through whenever you use an object or function name. It will first look in your global environment, then in the **Rstudio** tools (if using Rstudio), then in the **stats** package and so on.
- When loading packages, you will often see warnings about some objects or functions being 'masked'. This means that the newly loaded package contains an object with the same name as some object in a package that is already loaded. R will use the object in the new package whenever it comes across the name, because the new package will be earlier in the search path.

Introducing loops

- Many programming languages have ways of doing the same thing many times, perhaps changing some variable each time. This is called **looping**.
- Loops are not used in R so often, because we can usually achieve the same thing using vector calculations.
- For example, to add two vectors together, we do not need to add each pair of elements one by one, we can just add the vectors.
- But there are some situations where R functions can not take vectors as input. For example, **read.csv** will only load one file at a time.
- What if we had ten files to load in, all ending in the same extension (like .csv)?

Introducing loops

- We could do this:

```
> colony<-data.frame()      # Start with empty data frame

> colony1<-read.csv("1.4_colony_Run1Counts.csv")
> colony2<-read.csv("1.4_colony_Run2Counts.csv")
> colony3<-read.csv("1.4_colony_Run3Counts.csv")
...
> colony10<-read.csv("1.4_colony_Run10Counts.csv")

> colony<-rbind(colony1,colony2,colony3,...,colony10)
```

But this will be boring to type, difficult to change, and prone to error.
- As we are doing the same thing 10 times, but with a different file name each time, we can use a **loop** instead.

LOOPS

Commands & flow control

- R has two basic types of loop:
 - for** loop: run some code on every value in a vector
 - while** loop: run some code while some condition is true
- Here are two simple examples of these loops:

```
for (f in 1:10) {
  print(f)
}
```

```
i <- 1
while ( i <= 10 ) {
  print(i)
  i <- i + 1
}
```

when this condition is false the loop stops

LOOPS

Commands & flow control

- Here's how we might use a **for** loop to load in our CSV files.
- If the data files are in your current working directory, we can look up files containing a particular substring in their name using the **dir** function:

```
dir(pattern="Counts.csv")  
[1] "1.4_colony_Run1Counts.csv" "1.4_colony_Run2Counts.csv"  
     "1.4_colony_Run3Counts.csv"
```

- So we can load all the files using a **for** loop as follows:

```
colony<-data.frame()  
countfiles<-dir(pattern="Counts.csv")  
for (file in countfiles) {  
  t<-read.csv(file)  
  colony<-rbind(colony,t)  
}
```

- Here, we use a temporary variable **t** to store the data in each file, and then add that data to the main **colony** data frame.

Conditional branching

Commands & flow control

- Use an **if** statement for any kind of condition testing.
- Different outcomes can be selected based on a condition within brackets.

```
if (condition) {  
  ... do this ...  
} else {  
  ... do something else ...  
}
```

- **condition** is any logical value, and can contain multiple conditions
 - e.g. **(a==2 & b <5)**, this is a compound conditional argument

Conditional branching

Commands & flow control

For example, if we were writing a script to load an unknown set of files, using the **for** loop we wrote before, we might want to warn the user if we can't find any files with the pattern we are searching for. Here's how we can use an **if** statement to test for this:

```
colony<-data.frame()  
countfiles<-dir(pattern="Counts.csv")  
  
if (length(countfiles) == 0) {  
  stop("No Counts.csv files found!")  
} else {  
  for (file in countfiles) {  
    t<-read.csv(file)  
    colony<-rbind(colony,t)  
  }  
}
```

The **stop** function outputs the error message and quits.

Code formatting avoids bugs!

- Code formatting is crucial for readability of loops

```
f<-26
while(f!=0){
print(letters[f])
f<-f-1 }

BAD!!!

f <- 26
while( f != 0 ){
  print(letters[f])
  f <- f-1
}

GOOD!
```

- The code between brackets {} **always** is indented, this clearly separates what is executed once, and what is run multiple times
- Trailing bracket } always alone on the line at the same indentation level as the initial bracket {
- Use white spaces to divide the horizontal space between units of your code, e.g. around assignments, comparisons

Exercise

1. Output the patients data frame, with the patients sorted in order of age, oldest first. (You may need the **rev** function.)
2. Load in the **colony** data frame using a for loop. Three of the data files are in the *Day_1_scripts* folder. Load all three files into **colony** using the for loop in the slides.
3. How many observations do you have in the **colony** data frame? Find out by counting the number of rows in **colony** using the **nrow** function.
4. Suppose a power analysis of your data shows that you only need 48 observations to robustly test your hypothesis. This means we can stop loading files when we have loaded at least 48 observations. Modify your **for** loop so it will only load files if the **colony** data frame has less than 48 observations in it.

Answers to exercise

1. To order the patients by decreasing age:

```
patients[rev(order(patients$Age)) , ]
```

3. To find the number of rows in the **colony** data frame:

```
nrow(colony)
```

4. To stop loading files after at least 48 observations have been found, use the code from the first **for** loop slide with a new **if** statement:

```
colony<-data.frame()
countfiles<-dir(pattern="Counts.csv")
for (file in countfiles) {
  if ( nrow(colony) < 48 ) {
    t<-read.csv(file)
    colony<-rbind(colony,t)
  }
}
```

Statistics

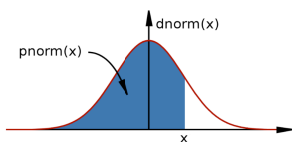
5

Built-in support for statistics

- R is a statistical programming language
 - Classical statistical tests are built-in
 - Statistical modeling functions are built-in
 - Regression analysis is fully supported
 - Additional mathematical packages are available
 - MASS, Waves, sparse matrices, etc

Distribution functions

- mostly commonly used distributions are built-in, functions have stereotypical names, e.g. for normal distribution:
 - `pnorm` - cumulative distribution for x
 - `qnorm` - inverse of `pnorm` (from probability gives x)
 - `dnorm` - distribution density
 - `rnorm` - random number from normal distribution



- available for variety of distributions: `punif` (uniform), `pbinom` (binomial), `pnbinom` (negative binomial), `ppois` (poisson), `pgeom` (geometric), `phyper` (hyper-geometric), `pt` (T distribution), `pf` (F distribution) ...

Distribution functions

- 10 random values from the Normal distribution with mean 10 and standard deviation 5:

```
rnorm(10, mean=10, sd=5)
```

- The probability of drawing 10 from this distribution:

```
dnorm(10, mean=10, sd=5)
```

```
[1] 0.07978846
```

```
dnorm(100, mean=10, sd=5)
```

```
[1] 3.517499e-72
```

- The probability of drawing a value smaller than 10:

```
pnorm(10, mean=10, sd=5)
```

```
[1] 0.5
```

- The inverse of **pnorm**:

```
qnorm(0.5, mean=10, sd=5)
```

```
[1] 10
```

- How many standard deviations for statistical significance?

```
qnorm(0.95, mean=0, sd=1)
```

```
[1] 1.644854
```

Two sample tests

Basic data analysis

- Comparing 2 variances

- Fisher's F test

```
var.test()
```

- Comparing 2 sample means with normal errors

- Student's t test

```
t.test()
```

- Comparing 2 means with non-normal errors

- Wilcoxon's rank test

```
wilcox.test()
```

- Comparing 2 proportions

- Binomial test

```
prop.test()
```

- Correlating 2 variables

- Pearson's / Spearman's rank correlation

```
cor.test()
```

- Testing for independence of 2 variables in a contingency table

- Chi-squared

```
chisq.test()
```

- Fisher's exact test

```
fisher.test()
```

Comparison of 2 data sets example

Basic data analysis

- Men, on average, are taller than women.

- The steps

- Determine whether variances in each data series are different

- Variance is a measure of sampling dispersion, a first estimate in determining the degree of difference

- Fisher's F test

- Comparison of the mean heights.

- Determine probability that mean heights really are drawn from different sample populations

- Student's t test, Wilcoxon's rank sum test

1. Comparison of 2 data sets

Fisher's F test

- Read in the data file into a new object, `heightData`
`heightData<-read.csv("1.5_heightData.csv")`
- attach** the data frame so we don't have to refer to it by name all the time:
`attach(heightData)`
- Do the two sexes have the same variance?
`var.test(Female, Male)`

```
F test to compare two variances

data: Female and Male
F = 1.0073, num df = 99, denom df = 99, p-value = 0.9714
alternative hypothesis: true ratio of variances is not equal to 1
95 percent confidence interval:
 0.6777266 1.4970241
sample estimates:
ratio of variances
 1.00726
```

2. Comparison of 2 data sets

Student's t test

- Student's t test is appropriate for comparing the difference in mean height in our data. We need a one-tailed test.
 - Remember a t test = $\frac{\text{difference in two sample means}}{\text{standard error of the difference of the means}}$

```
t.test(Female, Male, alternative="less")
```

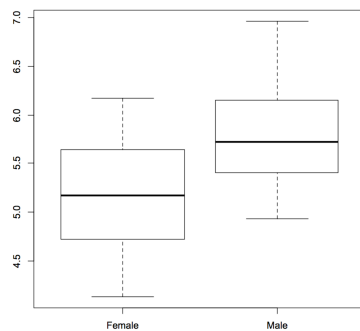
```
Welch Two Sample t-test
```

```
data: Female and Male
t = -8.4508, df = 197.997, p-value = 3.109e-15
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
 -Inf -0.5079986
sample estimates:
mean of x mean of y
 5.168725  5.800214
```

3. Comparison of 2 data sets

Review findings

```
> boxplot(heightData)
```



Linear regression

Basic data analysis

- Linear modeling is supported by the function `lm()`
 - `example(lm)` # the output assumes you know a fair bit about the subject
- `lm` is really useful for plotting lines of best fit to XY data in order to determine intercept, gradient & Pearson's correlation coefficient
 - This is very easy in R
- Three steps to plotting with a best fit line
 - Plot XY scatter-plot data
 - Fit a linear model
 - Add bestfit line data to plot with `abline()` function

Typical linear regression analysis

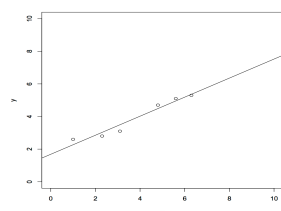
Basic data analysis

X	Y
1.0	2.6
2.3	2.8
3.1	3.1
4.8	4.7
5.6	5.1
6.3	5.3

```
> x<-c(1, 2.3, 3.1, 4.8, 5.6, 6.3)
> y<-c(2.6, 2.8, 3.1, 4.7, 5.1, 5.3)
> plot(y~x, xlim=c(0,10),ylim=c(0,10))
```

```
> myModel<-lm(y~x)
> abline(myModel)
```

Note formula notation
(y is given by x)



Get the coefficients of the fit from:
`summary.lm(myModel)` and
`coef(myModel)`
`resid(myModel)`
`fitted(myModel)`

Get QC of fit from
`plot(myModel)`

Find out about the fit data from
`names(myModel)`

Modelling formulae

- R has a very powerful formula syntax for describing statistical models.
 - Suppose we had two explanatory variables **x** and **z** and one response variable **y**.
 - We can describe a relationship between, say, **y** and **x** using a tilde `~`, placing the response variable on the left of the tilde and the explanatory variables on the right:
- ```
> y~x
```
- It is very easy to extend this syntax to do multiple regressions, ANOVAs, to include interactions, and to do many other common modelling tasks. For example:

```
> y~x # If x is continuous, this is linear regression
> y~x # If x is categorical, this is ANOVA
> y~x+z # If x and z are continuous, this is multiple regression
> y~x+z # If x and z are categorical this is a two-way ANOVA
> y~x+z:x:z # : is the symbol for the interaction term
> y~x*z # * is a shorthand for x+z+x:z
```

---

---

---

---

---

---

---

## The linear model object

### Basic data analysis

- Summary data describing the linear fit is given by
  - `summary(myModel)`

```
> summary(myModel)
```

```
Call:
lm(formula = y ~ x)

Residuals:
 1 2 3 4 5 6
0.33159 -0.22785 -0.39520 0.21169 0.14434 -0.06458

Coefficients:
 Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.68422 0.29056 5.796 0.0044 **
x 0.58418 0.06786 8.608 0.0010 **

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3114 on 4 degrees of freedom
Multiple R-squared: 0.9488, Adjusted R-squared: 0.936
F-statistic: 74.1 on 1 and 4 DF, p-value: 0.001001
```

Y intercept

Gradient

Good fit: would happen 1 in 1000 by chance

$R^2$ , with pValue

## Exercise

### The coin toss

To learn how the distribution functions work, try simulating tossing a fair coin 100 times and then show that it is fair.

- 1) We can model a coin toss using the binomial distribution. Use the **rbinom** function to generate a sample of 100 coin tosses. Look up the binomial distribution help page to find out what arguments this function needs.
- 2) How many heads or tails were there in your sample? You can do this in two ways; either select the number of successes using indices, or convert your sample to a factor and get a summary of the factor.
- 3) If we toss a coin 50 times, what is the probability that we get exactly 25 heads? What about 25 heads or less? Use **dbinom** and **pbinom** to find out.
- 4) The argument to **dbinom** is a vector, so try calculating the probabilities for getting any number of coin tosses from 0 to 50 in fifty trials using **dbinom**. Plot these probabilities using **plot**. Does this plot remind you of anything?

## Coin toss answers

- To simulate a coin toss, give **rbinom** a number of observations, the number of trials for each observation, and a probability of success:

```
> coin.toss<-rbinom(100, 1, 0.5)
```

- Because we only specified one trial per observation, we either have an outcome of 0 or 1 successes. To get the number of successes, use indices or a factor to look up the number of 1s in the **coin.toss** vector (your numbers will vary):

```
> length(coin.toss[coin.toss==1])
```

```
[1] 50
```

```
> summary(factor(coin.toss))
```

```
 0 1
```

```
50 50
```

## Coin toss answers

The probability of getting exactly 25 heads from 50 observations of a fair coin:

```
> dbinom(25, 50, 0.5)
```

The probability of getting 25 heads or less from 50 observations of a fair coin:

```
> pbinom(25, 50, 0.5)
```

The probabilities for getting all numbers of coin tosses from 0 to 50 in fifty trials:

```
> dbinom(0:50, 50, 0.5)
```

To plot this distribution, which should resemble a normal distribution:

```
> plot(dbinom(0:50, 50, 0.5))
```

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## Exercise

### Linear modelling example

Mice have varying numbers of babies in each litter. Does the size of the litter affect the average brain weight of the offspring? We can use linear modelling to find out. (This example is taken from John Maindonald and John Braun's book *Data Analysis and Graphics Using R* (CUP, 2003), p140-143.)

- 1) Install and load the **DAAG** package. The **litters** data frame is part of this package. Take a look at it. How many variables and observations does it have? Does **summary** tell you anything useful? What about **plot**?
- 2) Are any of the variables correlated? Look up the **cor.test** function and use it to test for relationships.
- 3) Use **lm** to calculate the regression of brain weight on litter size, brain weight on body weight, and brain weight on litter size and body weight together.
- 4) Look at the coefficients in your models. How is brain weight related to litter size on its own? What about in the multiple regression? How would you interpret this result?

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## Linear modelling answers

- To install and load the package and look at **litters**:

```
> install.packages("DAAG")
```

```
> library(DAAG)
```

```
> litters
```

```
> summary(litters)
```

```
> plot(litters)
```

- To calculate correlations between variables:

```
> attach(litters)
```

```
> cor.test(brainwt, lsize)
```

```
> cor.test(bodywt, lsize)
```

```
> cor.test(brainwt, bodywt)
```

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## Linear modelling answers

- To calculate the linear models:

```
> lm(brainwt~lsize)
Call:
lm(formula = brainwt ~ lsize)

Coefficients:
(Intercept) lsize
 0.447000 -0.004033
```

```
> lm(brainwt~bodywt)
Call:
lm(formula = brainwt ~ bodywt)
```

```
Coefficients:
(Intercept) bodywt
 0.33555 0.01048
```

```
> lm(brainwt~lsize+bodywt)
Call:
lm(formula = brainwt ~ lsize + bodywt)

Coefficients:
(Intercept) lsize bodywt
 0.17825 0.00669 0.02431
```

Interpretation: brain weight decreases as litter size increases, but brain weight increases proportional to body weight (when bodywt is held constant, the lsize coefficient is positive: 0.00669). This is called 'brain sparing'; although the offspring get smaller as litter size increases, the brain does not shrink as much as the body.

End of Day 1