



**Figure 6.19.** Graphical approach to estimating  $Y_{X/S}^M$  and  $m_s$  for chemostat data for *E. coli* growing on glucose as the limiting nutrient.

model, we must view this conversion as instantaneous. Otherwise, a perceptible period of substrate uptake, prior to conversion to product, would cause a change in the amount of  $X$ . This is unlike maintenance, since the period between substrate uptake and use for maintenance functions may be long, so we allow  $S$  to become incorporated into  $X$  and  $X$  is then degraded when needed; the following equations assume instantaneous conversion of substrate to extracellular product, with the cell acting as a catalyst. The balance on product formation is

$$DP = q_p X \quad (6.80)$$

where  $q_p$  is described by eqs. 6.16, 6.17, or 6.18. For nongrowth-associated product formation,  $q_p$  is a constant ( $\beta$ ), while for growth-associated products it is a function of  $\mu_g$ . For substrate balance, eq. 6.69 becomes

$$D(S_0 - S) = \frac{1}{Y_{X/S}^M} (D + k_d) X + \frac{1}{Y_{P/S}} q_p X \quad (6.81)$$

The biomass balance is unchanged from the case with endogenous metabolism and yields