



Figure 16.2. Dynamic behavior that can result from the model developed in Example 16.3. (With permission, from H. M. Tsuchiya and others, Predator-Prey Interactions of *Dictyostelium discoideum* and *Escherichia coli* in Continuous Culture, *J. Bacteriol.*, vol. 110, p. 1147, 1972.)

By defining dimensionless variables such as

$$\bar{X}_b = \frac{X_b}{X_{bF}}, \quad \bar{X}_p = \frac{X_p}{X_{pF}} \quad (16.20)$$

we can express eqs. 16.18 and 16.19 in terms of X_b and X_p .

$$\frac{d\bar{X}_b}{dt} = \mu'_b (1 - \bar{X}_p) \bar{X}_b \quad (16.21)$$

$$\frac{d\bar{X}_p}{dt} = -k'_d (1 - \bar{X}_b) \bar{X}_p \quad (16.22)$$

Equations 16.21 and 16.22 can be solved with the initial conditions of $\bar{X}_b(0) = \bar{X}_{b0}$ and $\bar{X}_p(0) = \bar{X}_{p0}$.

The relationship between \bar{X}_b and \bar{X}_p can be determined by dividing eq. 16.21 by eq. 16.22.