

and thus the slope,  $m$ , gives  $\Delta\mu$ , and  $R$  is given by the intercept as

$$R = m(f_{-i} - f_{-0}) = \Delta\mu(f_{-i} - f_{-0}) \quad (14.27)$$

where  $f_{-i}$  is the value of  $f_{-}$  at the intercept.

Equation 14.27 has interesting implications in helping to quantify the conditions for which eq. 14.26 is valid. That is,  $t$  must be sufficiently small that

$$\Delta\mu \gg (f_{-0} \Delta\mu + R)e^{\Delta\mu t}$$

when  $\Delta\mu \gg R$ . Thus,

$$\Delta\mu \gg (f_{-0} \Delta\mu + \Delta\mu f_{-i} - \Delta\mu f_{-0})e^{\Delta\mu t} \quad (14.28)$$

or

$$1 \gg f_{-i} e^{\Delta\mu t} \quad (14.29)$$

or

$$0 \gg \ln f_{-i} + \Delta\mu t \quad (14.30)$$

or

$$t \ll \frac{-\ln f_{-i}}{\Delta\mu} \quad (14.31)$$

The analysis also assumes that  $\Delta\mu t > 1$ ; thus, the linear region suitable for use for case 1 situations is

$$\frac{1}{m} < t < \frac{-\ln f_{-i}}{m} \quad (14.32)$$

In case 2, for  $t > 1/(\Delta\mu + R)$ ,

$$f_{-} \approx 1 - (1 + \Delta\mu/R)e^{-(\Delta\mu+R)t} \quad (14.33a)$$

$$\ln f_{+} = \ln(1 - f_{-}) = \ln(1 + \Delta\mu/R) - (\Delta\mu + R)t \quad (14.33b)$$

in which case the intercept is used to evaluate  $f_{+i}$  and the slope  $m = -(\Delta\mu + R)$ :

$$\Delta\mu = m(f_{+i} - 1) = mf_{-i} \quad (14.34)$$

$$R = -mf_{+i} = -m(1 - f_{-i}) \quad (14.35)$$

In case 3, we note that  $f_{-}$  assumes a constant value between 0 and 1, which we denote as  $f_{-}^*$ . Equation 14.25 yields  $f_{-}^*$  by allowing  $t \rightarrow \infty$ , or

$$f_{-}^* \approx R/\Delta\mu \quad (14.36)$$

A plot of  $\ln(f_{-}^* - f_{-})$  versus time will give a slope,  $m$ , such that

$$m = R - |\Delta\mu| \quad (14.37)$$

Equations 14.36 and 14.37 can be combined to give