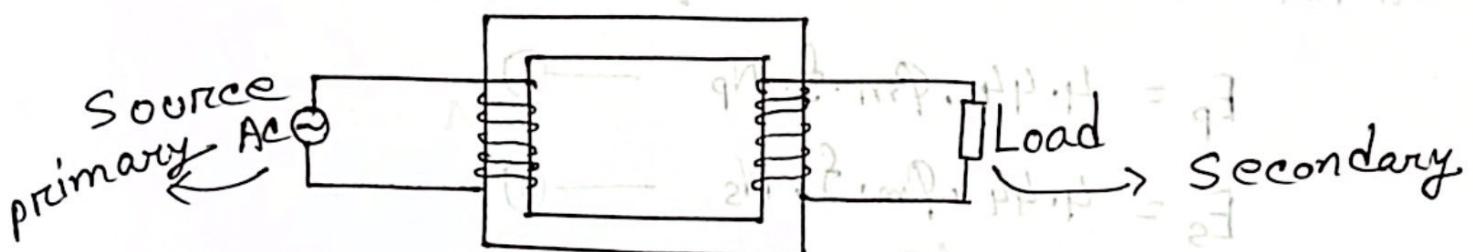


Transformer



⇒ The side where the source that is the primary source

power → Primary = Secondary $V_p I_p = V_s I_s$

frequency → Primary = Secondary

$$\text{EMF or } E = -N \frac{d\phi}{dt}$$

Hence,

N = Number of turns,

ϕ = magnetic flux

t = time

⇒ The side with a higher number of turns has a higher voltage. If the number of turns is less the voltage is also less

Turns Ratio, $a = \frac{N_p}{N_s}$

Transformation Ratio, $K = \frac{N_s}{N_p} = \frac{1}{a}$

No-load Condition

RMS Value of EMF Equation

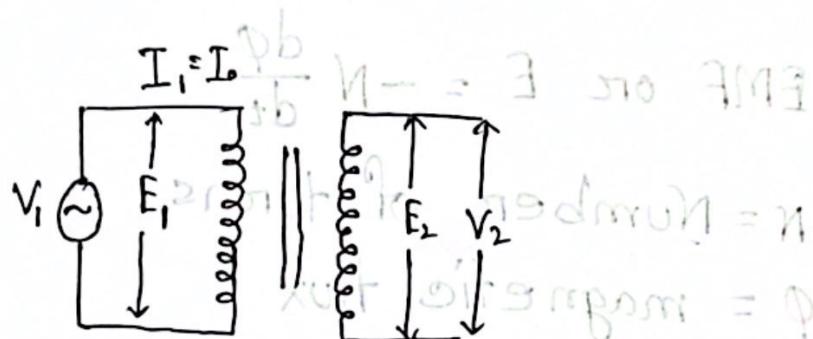
$$E_p = 4.44 \cdot \Phi_m \cdot f \cdot N_p \quad \text{--- (1)}$$

$$E_s = 4.44 \cdot \Phi_m \cdot f \cdot N_s \quad \text{--- (2)}$$

$$\textcircled{1} : \textcircled{2} \Rightarrow \frac{E_1}{E_2} = \frac{N_p}{N_s} \Rightarrow \frac{E_1}{N_p} = \frac{E_2}{N_s} = K = 4.44 \Phi_m f$$

$\Rightarrow K > 1$; $N_s > N_p \rightarrow$ Step-up transformer

$\Rightarrow K < 1$; $N_s < N_p \rightarrow$ Step-down transformer



When in no load condition

$I_1 = I_o \rightarrow I_w \rightarrow$ Working Component
 $I_1 = I_o \rightarrow I_{w/H} \rightarrow$ Magnetizing Component

Losses

\Rightarrow Iron loss / Core loss + Copper loss ($I^2 R$)

↓ ↓

Eddy Current loss Hysteresis loss

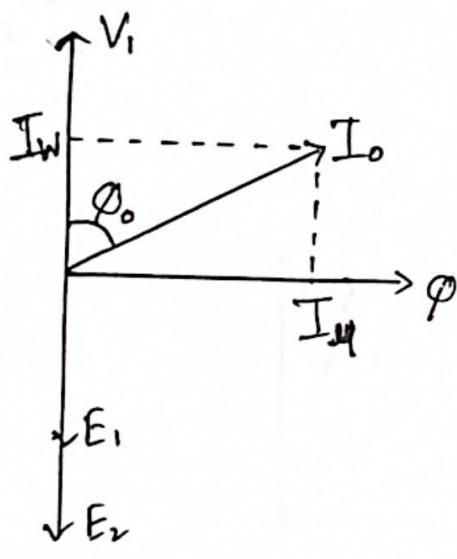
Flux equation

$$E = -N \frac{d\phi}{dt} \quad [\phi = \phi_m \sin \omega t]$$

$$\Rightarrow \phi = -N \frac{d(\phi_m \sin \omega t)}{dt}$$

$$= k \sin(\omega t - 90^\circ)$$

■ No-load transformer phasor diagram



$$\vec{I}_0 = \vec{I}_w + \vec{I}_4$$

$$I_{w0} = I_0 \cos \phi_0$$

$$I_{40} = I_0 \sin \phi_0$$

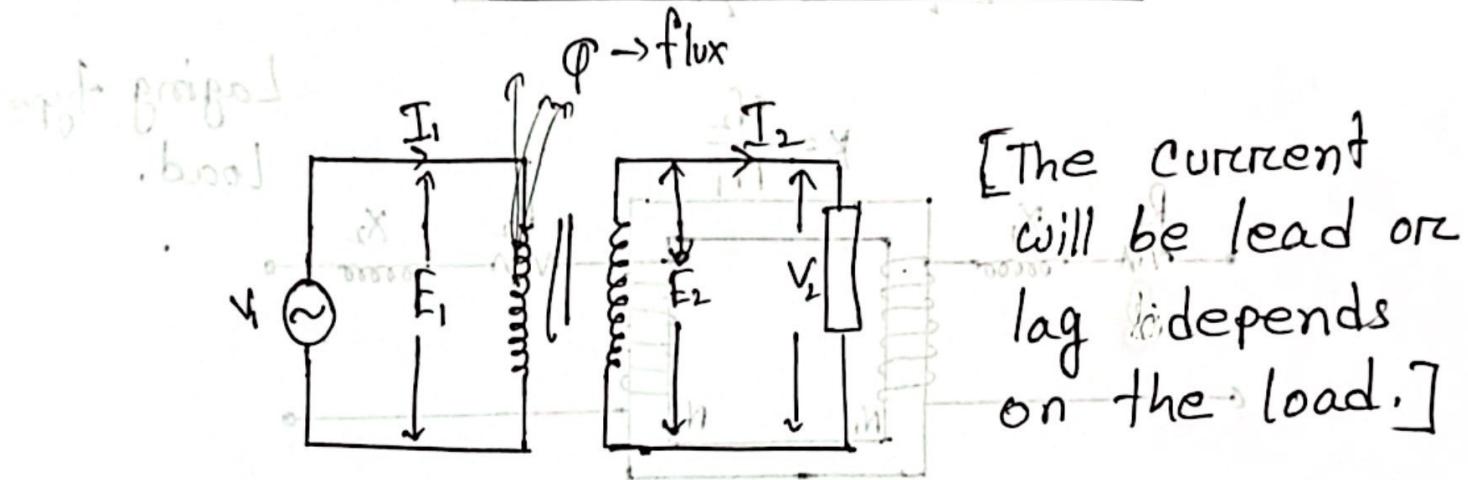
$$I_0 = \sqrt{I_{w0}^2 + I_{40}^2}$$

■ Ideal Power balance eqn

$$KVE = E_1 I_1 = E_2 I_2 \quad [I_2 = 0]$$

$$\Rightarrow E_2 I_2 = 0 = E_1 I_1$$

Transformer on Load



$$\vec{I}_1 = \vec{I}_o + \vec{I}'_2$$

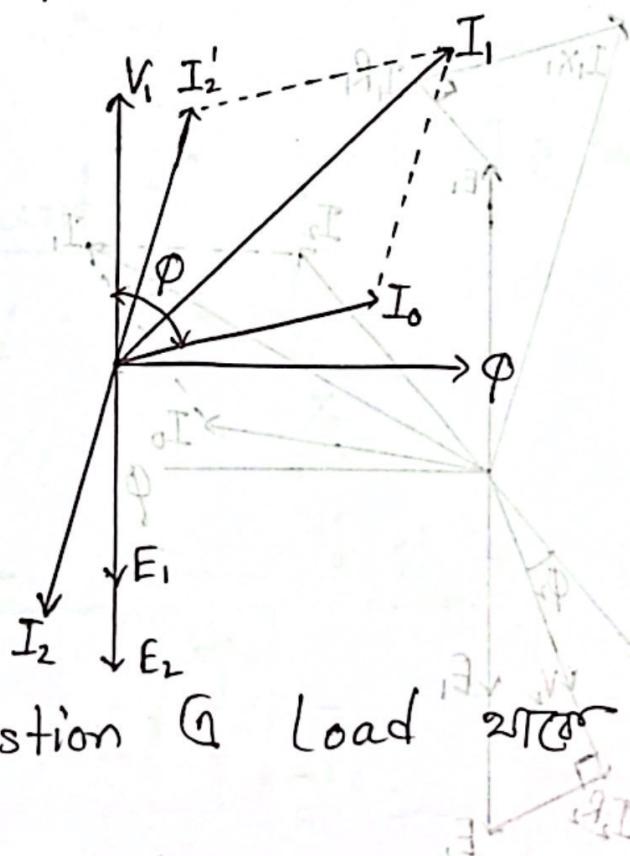
$$I'_2 = K I_2$$

$$= \frac{N_2}{N_1} \cdot I_2$$

$$jX_1 I_o + jR_1 I + V_o = E_1$$

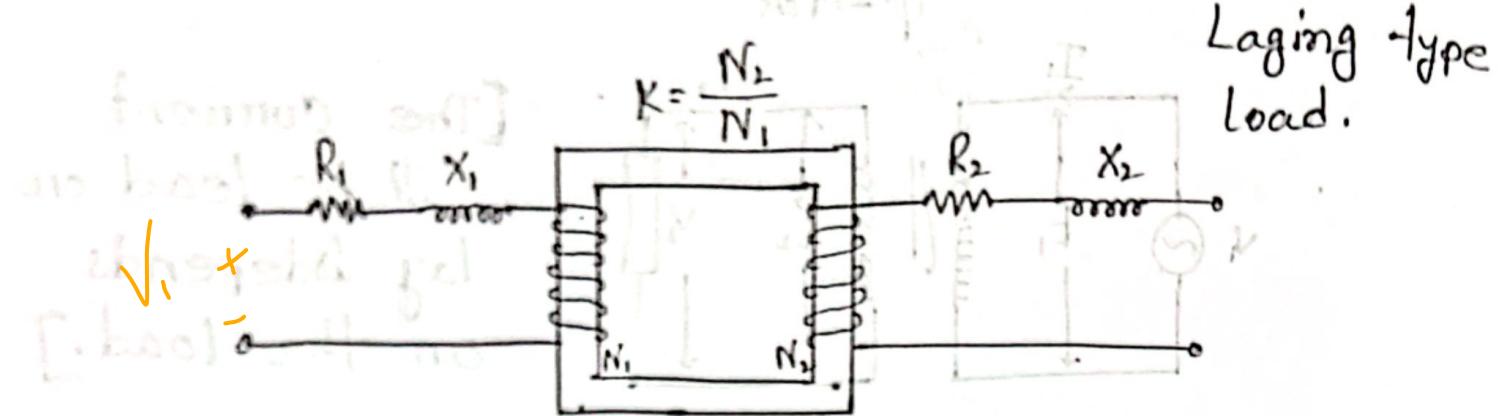
$$(jX_1 + jR_1) I + E_o = V_o$$

$$(jX_1 + jR_1) I + V_o = E_o - jR_2 I$$



\Rightarrow In Question Q Load after Loaded transformer

Equivalent Circuit

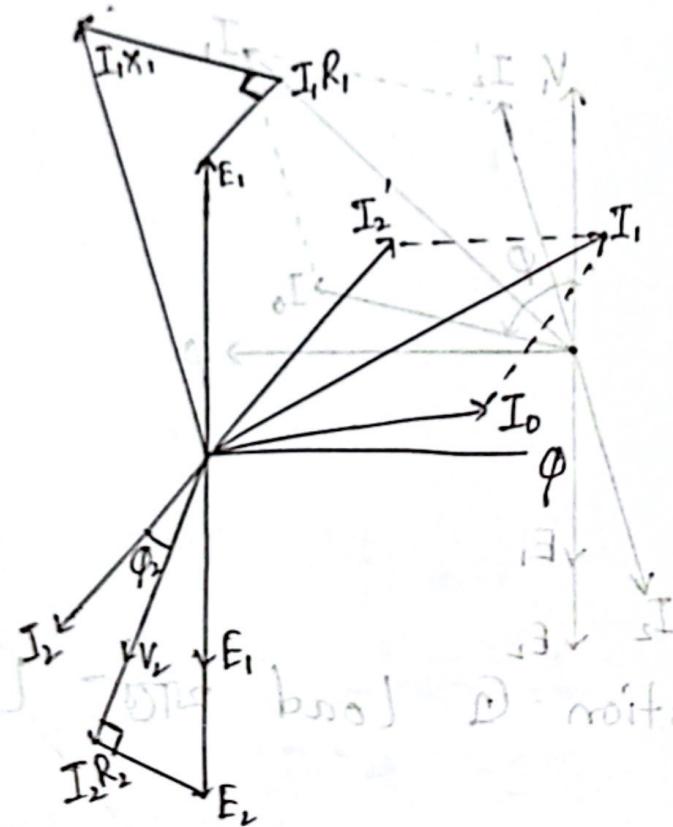


$$\# E_1 = -V_1 + I_1 R_1 + j I_1 X_1$$

$$\Rightarrow V_1 = -E_1 + I_1 (R_1 + jX_1)$$

and,

$$\# E_2 = V_2 + I_2 (R_2 + jX_2)$$



■ Shifting : ~~between primary & secondary~~

Secondary to Primary shift:

$$X'_2 = \frac{X_2}{K^2}$$

$$R'_2 = \frac{R_2}{K^2}$$

$$Z'_2 = \frac{Z_2}{K^2}$$



Primary to Secondary shift:

$$X'_1 = K^2 X_1$$

$$R'_1 = K^2 R_1$$

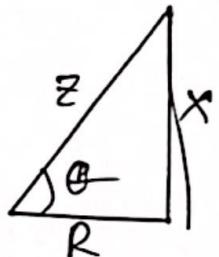
$$Z'_1 = K^2 Z_1$$

■ Only have ^{Value} X_1 and R_1 ,

$$Z_1 = \sqrt{R_1^2 + X^2}$$

$$\tan \theta = \frac{X}{R}$$

$$\theta = \tan^{-1} \left(\frac{X}{R} \right)$$



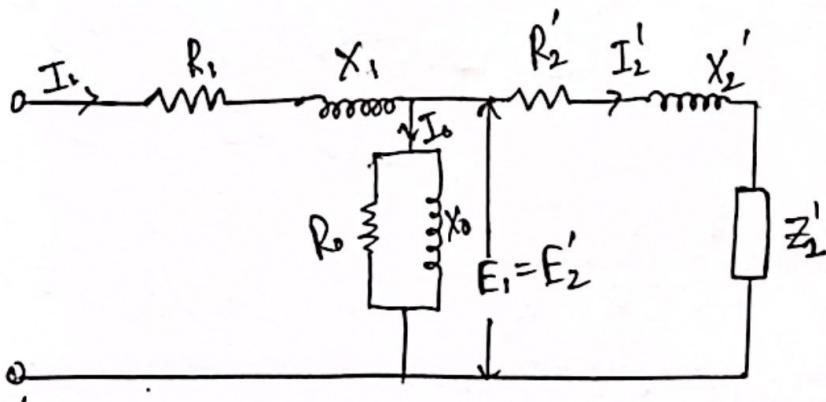
Equivalent

$$R = R_1 + R'_2 = R_1 + \frac{R_2}{K^2}$$

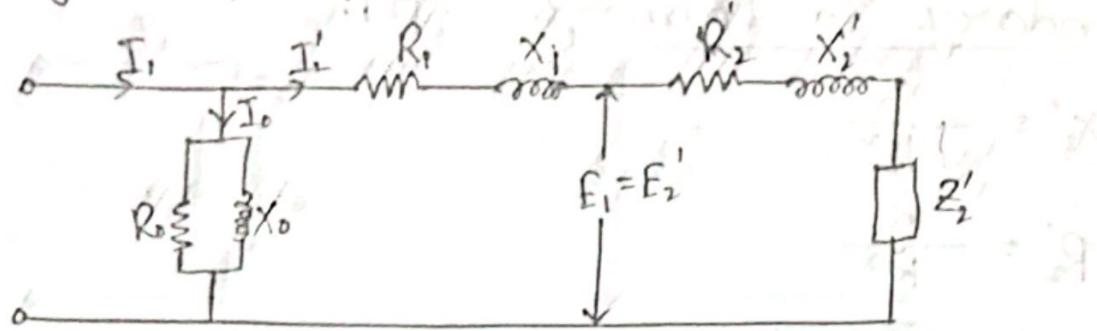
$$X = X_1 + X'_2 = X_1 + \frac{X_2}{K^2}$$

$$I'_2 = K I_2$$

$$E_2 = K E'_2$$



Simplify circuit:



$$(Z_1)_{\text{left}} = 0$$

$$I_2 X = Z_2$$

$$I_2 X = Z_2$$

$$\frac{R}{k} + R_1 = \frac{R}{k} + R = R$$

$$\frac{X}{k} + X = \frac{X}{k} + X = X$$



32.1 The maximum flux density in core of a ~~250/3000~~ $\frac{1}{2}$ volt, 50 Hz single phase transformer is 1.2 mW/m^2 . If the emf per turn is 8 volts, determine.

① Primary and secondary turns

② Area of the core.

Solⁿ: ①

Given that,

$$\text{emf per turn, } E_t = 8 \text{ V}$$

$$V_1 = E_t = 250 \text{ V}$$

$$V_2 = E_t = 3000 \text{ V}$$

we know that, $N_1 \times \text{emf/turn}$
 $E_1 = N_1 \times \text{emf/turn}$
 $\Rightarrow 250 = N_1 \times 8$
 $\Rightarrow N_1 = \frac{250}{8} \approx 32$

and, $E_2 = N_2 \times \text{emf/turn}$

$$\Rightarrow 3000 = N_2 \times 8$$

$$\Rightarrow N_2 = \frac{3000}{8} \approx 375$$

$$A = 20.0 = \text{m}^2$$

$$N_p = 32$$

$$N_s = 375$$

Given that, $f = 50 \text{ Hz}$, $E_1 = 250 \text{ V}$,
 flux density, $\beta_m = 1.2 \text{ wb/m}^2$

we know that,

$$E_1 = 4.44 f \cdot \phi_m \cdot N_1$$

$$\Rightarrow 250 = 4.44 \times 50 \times \beta_m \times A \times 32$$

$$250 = 250 \text{ V}$$

$$\Rightarrow A = \frac{250}{4.44 \times 50 \times 1.2 \times 32}$$

$$= 0.020 \text{ m}^2$$

32.5 The core of a three phase, 50 Hz, 11000/550 volt delta/star, 300 KVA, Core type transformer operate with a flux of 0.05 wb. find

i) number of H.v and L.v turns per phase

ii) emf per turn

iii) full load H.v and L.v phase current.

Soln:

Given that,

$$f = 50 \text{ Hz}, \frac{11000}{550} = 20 \text{ KVA} = 300$$

$$\phi_m = 0.05 \text{ wb}$$

$$E_1 = 11000 \text{ V}$$

$$E_2 = 550 \text{ V}$$

① We know that,

$$E_1 = 4.44 \rho_m f N_1$$

$$\Rightarrow 11000 = 4.44 \times 0.05 \times 50 \times N_1$$

$$\Rightarrow N_1 = \frac{11000}{4.44 \times 0.05 \times 50} = 200.99 \approx 201$$

and, $E_2 = 4.44 \rho_m f N_2$

$$\Rightarrow \frac{550}{\sqrt{3}} = 4.44 \times 0.05 \times 50 \times N_2$$

$$\therefore N_2 = 28.60 \approx 30$$

[E_2 star connection]

again,

$$\frac{N_2}{N_1} = \frac{E_2}{E_1}$$

$$\Rightarrow N_1 = N_2 \times \frac{E_1}{E_2} = 30 \times \frac{11000}{550 \sqrt{3}}$$

$$= 1040$$

(ii) emf per turn,

$$E_t = \frac{11000}{1040} = 10.57 V$$

(iii) per phase KVA = $\frac{300}{3} \times 100 \times 10^3 VA$.

We know that,

$$KVA = E_t I_t$$

$$\Rightarrow I_t = \frac{11000}{100 \times 10^3} = 0.1 A$$

and, $I_2 = \frac{N_1}{N_2} \times I_t = \frac{201}{30} \times \frac{1040}{30} \times 0.1$
 $= 315.46 A$

32.11] A single-phase transformer has 1000 turns on the primary and 200 turns on the secondary. The no load current is 3 amp. at a p.f of 0.2 lagging. Calculate the primary current and power factor when the second current is 280 A at a p.f of 0.8 Lagging.

Soln:

Given that,

$$N_1 = 1000$$

$$N_2 = 200$$

$I_0 = 3 \text{ A}$ at a p.f. of
0.2 lagging

$$I_1 = ?$$

p.f. at Primary when

$$I_2 = 280 \text{ A}$$
 at a p.f. 0.8
lagging.

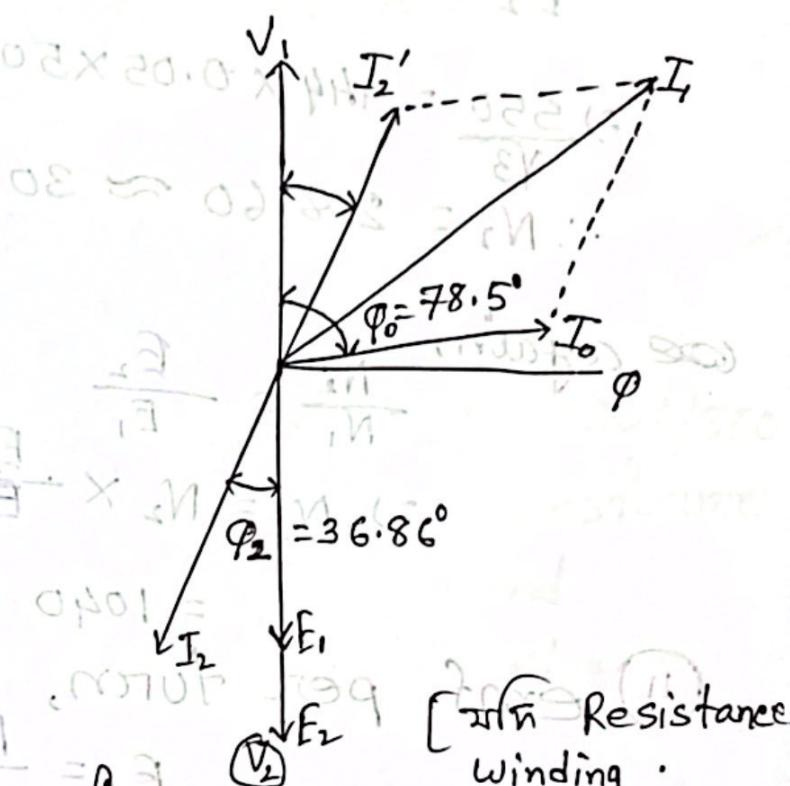
Considering V_1 as reference.

$$\text{So, } \cos \phi_0 = 0.2$$

$$\Rightarrow \phi_0 = \cos^{-1}(0.2) = 78.5^\circ$$

$$\text{and, } \cos \phi_2 = 0.8$$

$$\Rightarrow \phi_2 = \cos(0.8) = 36.86^\circ$$



[मात्रा Resistance winding.]

Component Q

ता थारे गाइन]

$V_2 \rightarrow E_1, E_2$

phase Q]

सार्व गाइन]

$$\vec{I}_o = 3 \angle -78.5^\circ A$$

$$I'_2 = K I_2$$

$$= \frac{N_2}{N_1} \times I_2 = \frac{200}{1000} \times 280 \\ = 56 A$$

$$\therefore \vec{I}_2 = 56 \angle -36.86^\circ$$

$$\text{Now, } \vec{I}_1 = \vec{I}_o + \vec{I}'_2$$

$$= 3 \angle -78.5^\circ + 56 \angle -36.86^\circ$$

32.13 A transformer has a primary winding of 800 turns and a secondary winding of 200 turns. When the load current on the secondary is 80 A at 0.8 p.f lagging, the primary current is 25 A at 0.7078 lagging. Determine graphically or otherwise the no-load current of the transformer and its phase with respect to the voltage.

Soln:

Given that,

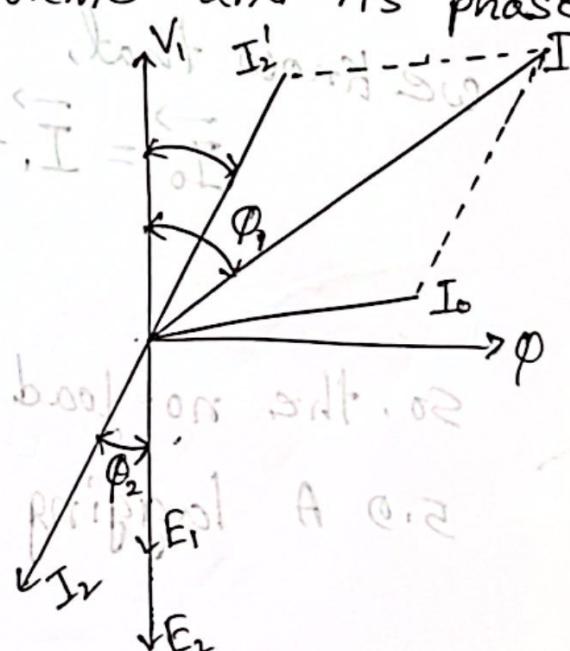
$$N_1 = 800$$

$$N_2 = 200$$

$$I_2 = 80 A \text{ at pf } 0.8 \text{ lagging}$$

$$I_1 = 25 A \text{ at pf } 0.7078 \text{ on sub bridge A.C.}$$

$$I_o = ?$$



Here,

$$\cos \varphi_2 = 0.8$$

$$\therefore \varphi_2 = \cos^{-1}(0.8)$$

$$= 36.86^\circ$$

and, $\cos \varphi_1 = 0.7078$

$$\varphi_1 = \cos^{-1}(0.7078)$$

$$= 44.04^\circ$$

Now, $\vec{I}_1 = 25 \angle -44.04^\circ A$

$$\vec{I}'_2 = K \vec{I}_2$$

$$\text{to A as } \vec{I}'_2 = \frac{N_2}{N_1} \vec{I}_2; \vec{I}_2 = \frac{200}{800} \times 80 = 20 A$$

$$\text{second eqn: } \vec{I}'_2 = 20 \angle -36.86^\circ A$$

we know that,

$$\vec{I}_0 = \vec{I}_1 - \vec{I}'_2 \Rightarrow 25 \angle -44.04^\circ - 20 \angle -36.86^\circ$$

$$= 5.0 \angle -73.32^\circ A$$

So, the no-load current is approximately 5.0 A lagging the applied voltage by 73.32°