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Section: 11

Task-5

Time complexity of BFS (Task-2):

If the graph is represented as adjacency list and there are V number of nodes/vertex and E number of edges in the graph.

We can discover all neighbors of each node by traversing its adjacency list just once in linear time. (Each neighboring vertex is inserted once into a queue and also each visited vertex is marked so it can not be visited again)

⇒ So, the sum of the size of adjacency lists of all the nodes/vertex is E in case of directed graph. As each vertex maintains a list of all its adjacent edges.

Therefore, the time complexity in case of adjacency list = $O(V) + O(E)$
 $= O(V+E)$

Again, if the graph is represented as an adjacency matrix (Pascally, a $V \times V$ array).

In order to discover all the outgoing edges of each node, we have to traverse an entire row of length V in the matrix. Point to be noted, each row of the adjacency matrix corresponds to a node in the graph. That row includes information about edges that emerge from the vertex.

Therefore, time complexity in case of adjacency

$$\text{matrix} = O(V \times V) = O(V^2)$$

Time complexity of DFS (Task-3):-

Let, V = number of vertex and E = number of edges in the graph.

If the graph is represented as adjacency list, (Like BFS, we can discover all its neighbors by scanning its adjacency list just once in linear time.)

So, the graph, sum of the sizes of adjacent list is E like BFS.

Therefore, the time complexity in this case = $O(E+V)$

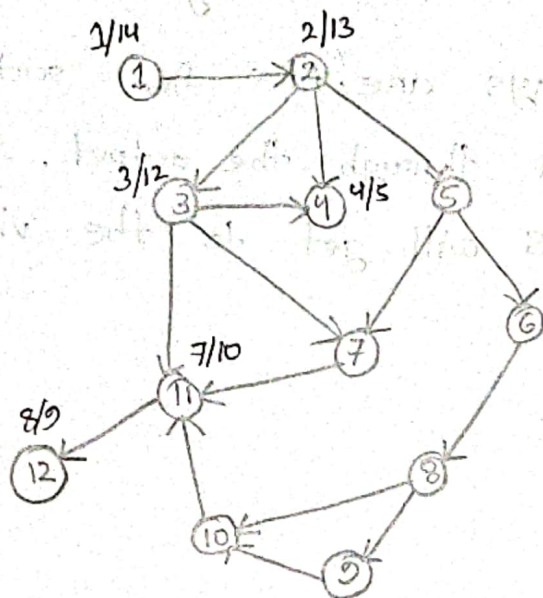
Again, adjacency matrix ($V \times V$)

Like BFS, each row stores information about edges emerging from the node and the discover all its outgoing edges we have to scan an entire row of length V .

So, time complexity of the DFS in this

case = $O(V^2)$.

Gany (used the DFS algorithm) gets to the victory road first.



Performing BFS:

Queue

1	2	3	4	5	7	11	6	12	8
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Dequeue 1 2 3 4 5 7 11 6 12

Steps 1 2 3 4 5 6 7 8 9

Performing DFS:

1 2 3 4 7 11 12

Steps 1 2 3 4 5 6 7

From the above simulation we can see, who
 are using DFS will get to the victory road first.
 But we know, we always are ^{use} BFS for shortest path
 but as we have to find through the output. So,
 those who are using DFS will get to the victory
 road first.