

Force at Angle Example

- A person is pushing a 15 kg block across a floor with $\mu_k = 0.4$ at a constant speed. If she is pushing down at an angle of 25 degrees, what is the magnitude of her force on the block?

x- direction: $\Sigma F_x = ma_x$

$$F_{\text{push}} \cos(\theta) - F_{\text{friction}} = 0$$
$$F_{\text{push}} \cos(\theta) - \mu F_{\text{Normal}} = 0$$
$$F_{\text{Normal}} = F_{\text{push}} \cos(\theta) / \mu$$

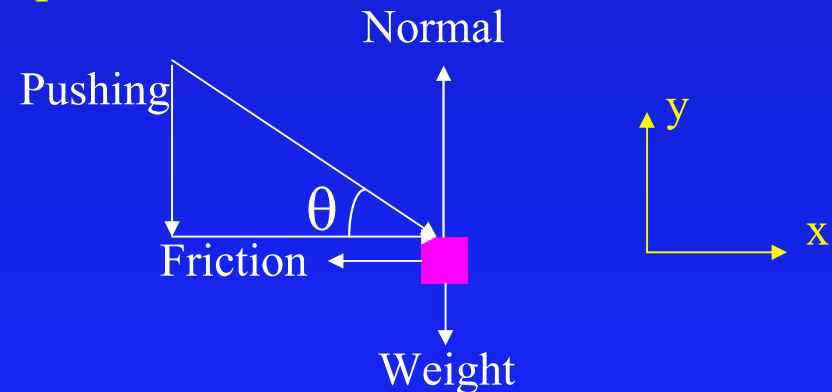
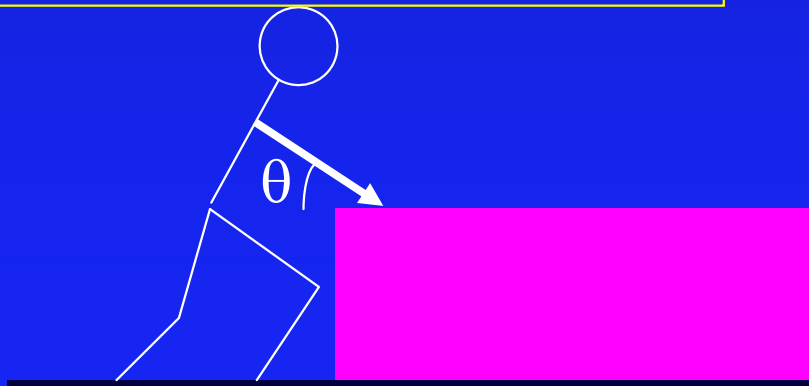
y- direction: $\Sigma F_y = ma_y$

$$F_{\text{Normal}} - F_{\text{weight}} - F_{\text{Push}} \sin(\theta) = 0$$
$$F_{\text{Normal}} - mg - F_{\text{Push}} \sin(\theta) = 0$$

Combine:

$$F_{\text{push}} \cos(\theta) / \mu - mg - F_{\text{push}} \sin(\theta) = 0$$
$$F_{\text{push}} (\cos(\theta) / \mu - \sin(\theta)) = mg$$
$$F_{\text{push}} = mg / (\cos(\theta) / \mu - \sin(\theta))$$

$$F_{\text{push}} = 80 \text{ N}$$



Position vs Time Plots

- Gives location at any time.
- Displacement is change in position.
- Slope gives instantaneous velocity.

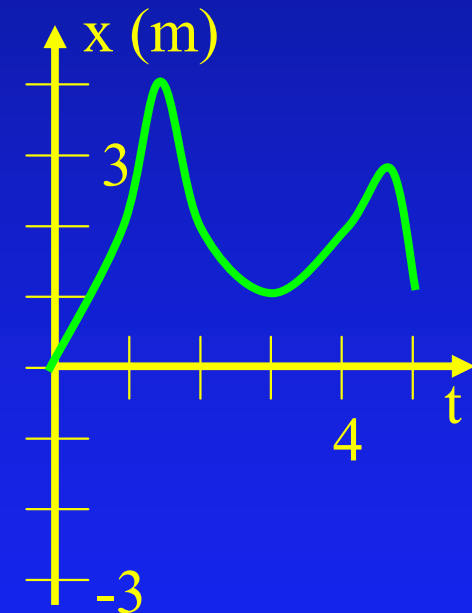
Position at $t=3$, $x(3) = 1$

Displacement between $t=5$ and $t=1$. $\Delta x = -1.0$ m

$$1.0 \text{ m} - 2.0 \text{ m} = -1.0 \text{ m}$$

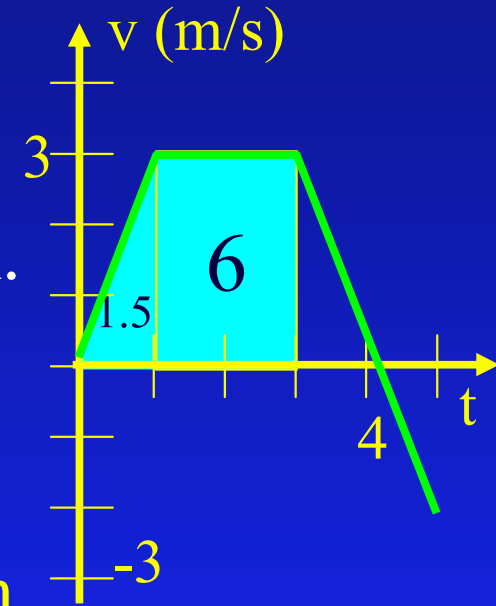
Average velocity between $t=5$ and $t=1$. $v = -0.25$ m/s

$$-1 \text{ m} / 4 \text{ s} = -0.25 \text{ m/s}$$



Velocity vs Time Plots

- Gives velocity at any time.
- Area gives displacement
- Slope gives instantaneous acceleration.



velocity at $t=2$, $v(2) = 3 \text{ m/s}$

Displacement between $t=0$ and $t=3$: $\Delta x = 7.5 \text{ m}$

$$t=0 \text{ to } t=1: \frac{1}{2} (3 \text{ m/s}) (1 \text{ s}) = 1.5 \text{ m}$$

$$t=1 \text{ to } t=3: (3 \text{ m/s}) (2 \text{ s}) = 6 \text{ m}$$

Average velocity between $t=0$ and $t=3$? $v = 7.5 \text{ m} / 3 \text{ s} = 2.5 \text{ m/s}$

Change in v between $t=5$ and $t=3$. $\Delta v = -2 \text{ m/s} - 3 \text{ m/s} = -5 \text{ m/s}$

Average acceleration between $t=5$ and $t=3$: $a = -5 \text{ m/s} / (2 \text{ s}) = -2.5 \text{ m/s}^2$