

these parameters found in the literature [60-63].

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SUPPLEMENTAL MATERIAL

Spin-orbit coupling

The spin-orbit coupling acts as an on-site term, $H_{\text{SOC}} = 2\eta \sum_{\mathbf{r}} \mathbf{L}_{\mathbf{r}} \cdot \mathbf{S}_{\mathbf{r}}$, where the sum is over the Ru sites. The crystal field splits the five Ru d orbitals in the e_g doublet and the t_{2g} triplet but only the t_{2g} orbitals are relevant close to the Fermi level. These three orbitals behave like a $l = 1$ angular momentum representation. Once expressed in terms of these orbitals only, the spin-orbit coupling Hamiltonian becomes [37, 38]

$$H_{\text{SOC}} = i\eta \sum_{\mathbf{k}} \sum_{l,m,n} \epsilon_{lmn} \sum_{s,s'} \sigma_{ss'}^x \epsilon_{\mathbf{k}l}^{\dagger} \epsilon_{\mathbf{k}l} \epsilon_{\mathbf{k}m} s'$$

where l, m, n are orbital indices, s, s' are spin indices and σ^x is the x -th Pauli matrix. The orbital indices are defined in the following way: $l = 1, 2, 3$ for, respectively, the orbital d_{yz} (B), d_{zx} (A) and d_{xy} (C).

Interaction parameters

In Table I, we give different estimates of the interaction parameters used in the main text (U , U' and J) that can be found in the literature. In Refs. [60] and [61], a constrained random phase approximation (cRPA) calculation was performed to estimate these parameters. These two references give consistent results and an estimate for J/U of 0.1. In Ref. [62], an RG calculation performed in the one-dimensional limit of the d_{xz} and d_{yz} orbitals lead to the right prediction for the crossover to 3D Fermi liquid behaviour in Sr_2RuO_4 ($T_{3D} \simeq 60\text{K}$). A value of 2.2 eV was taken for U and the relevant parameter range for J was considered to be between 0.13 and 0.4 eV. This corresponds to a value of J/U between 0.059 and 0.18. These estimates are in fair agreement with the range of J/U for which our calculation is in agreement with the measured critical specific heat jump, which is roughly given by $0.05 < J/U < 0.065$ and $0.075 < J/U < 0.085$. In Ref. [63] (see also references therein), a mean-field (MF) rotationally invariant slave bosons calculation was performed to study the impact of the Coulomb repulsion on the quasiparticle bands. From a survey of numerous references, they located U in the region 1.5-3.1 eV and J at 0.35 eV. Finally, Ref. [61] also reports a local density approximation associated with a dynamical mean field theory (LDA+DMFT) calculation. They obtain an estimate of $J = 0.4$ eV by fitting the predicted mass enhancement to the experimental value. This estimate is somewhat larger than the previous ones.

TABLE I. (continued)

Ref.	Method	U	U'	J	J/U
[60]	cRPA	2.56	1.94	0.26	0.101
[61]	cRPA	2.3	$U - 2J$	0.25	0.108
[62]	1D RG	2.2	-	0.13-0.4	0.059-0.18
[63]	MF	1.5-3.1	$U - 2J$	0.35	0.11-0.23
[61]	LDA+DMFT	2.3	$U - 2J$	0.4	0.17

TABLE I. Interaction parameters (in eV) obtained by various methods.

Pairing eigenvalue

In Fig. 5, we show the pairing eigenvalue λ for different pairing symmetries. The favoured state is the one with the largest value of $|\lambda|$. We show the eigenvalue for two odd-parity channels: one for the chiral state $\mathbf{d} = (p_x \pm ip_y)\hat{\mathbf{z}}$ and one for the most favoured helical state $\mathbf{d} =$