

Video Compression Assignment 2

Prerequisites

- Programming language: Python 3.10+ (IPython)
- Framework: Jupyter

Install dependencies from PyPI:

```
In [2]: %pip install \
        --disable-pip-version-check \
        --quiet \
        numpy \
        Pillow
```

Note: you may need to restart the kernel to use updated packages.

Task 1

Motion Estimation

Please apply the full-search block-matching algorithm to the luma component of `foreman_qcif_1_rgb.bmp` with the reference frame `foreman_qcif_0_rgb.bmp`.

The collocated position in the reference frame of the top-left pixel of each MB is the center of the search window.

The search range is set to $[-16, 15]$. The similarity metric is SAD. Please show MVs for all the MBs in the video frame.

Solution of Task 1

The macroblock size is 16x16, and the search window size is 32x32:

```
In [3]: block_size = (16, 16)
        search_size = (32, 32)
```

The top-left pixel of a macroblock is the block index as well as the center of the search window:

```
plaintext
o: block index
+: other pixel

o + + +
+ + + +
+ + + +
+ + + +
```

For a search window located at the `center`, the range of block index to search is `[center - window_size // 2, center]`:

```
plaintext
o: search block index
x: center block index (also search block index)
+: other pixel

o o o o | o + + +
o o o o | o + + +
o o o o | o + + +
o o o o | o + + +
-----+-----
o o o o | x + + +
+ + + + | + + + +
+ + + + | + + + +
+ + + + | + + + +
```

```
In [4]: from IPython.display import display

        search_block_index_range = (
            (-search_size[0] // 2, 0),
            (-search_size[1] // 2, 0),
        )
        display(search_block_index_range)
```

`((-16, 0), (-16, 0))`

Wrap these concepts into functions:

```
In [5]: from typing import Iterable
        from PIL.Image import Image

        def get_grid_size(frame: Image) -> tuple[int, int]:
```

```

        return (frame.width, frame.height)

def get_block_indexes(
    grid_size: tuple[int, int],
    block_size: tuple[int, int],
) -> tuple[Iterable[int], Iterable[int]]:
    assert grid_size[0] >= block_size[0], (grid_size[0], block_size[0])
    assert grid_size[1] >= block_size[1], (grid_size[1], block_size[1])
    return (
        range(0, grid_size[0] - block_size[0] + 1, block_size[0]),
        range(0, grid_size[1] - block_size[1] + 1, block_size[1]),
    )

def get_block_index_bound(
    frame: Image,
) -> tuple[tuple[int, int], tuple[int, int]]:
    return ((0, max(frame.width - 1, 0)), (0, max(frame.height - 1, 0)))

def get_search_block_indexes(
    center_block_index: tuple[int, int],
    search_block_index_range: tuple[tuple[int, int], tuple[int, int]],
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
) -> tuple[Iterable[int], Iterable[int]]:

    def minmax(value: int, min_value: int, max_value: int) -> int:
        return max(min(value, max_value), min_value)

    return (
        range(
            minmax(
                center_block_index[0] + search_block_index_range[0][0],
                block_index_bound[0][0],
                block_index_bound[0][1],
            ),
            minmax(
                center_block_index[0] + search_block_index_range[0][1],
                block_index_bound[0][0],
                block_index_bound[0][1],
            )
            + 1,
        ),
        range(
            minmax(
                center_block_index[1] + search_block_index_range[1][0],
                block_index_bound[1][0],
                block_index_bound[1][1],
            ),
            minmax(
                center_block_index[1] + search_block_index_range[1][1],
                block_index_bound[1][0],
                block_index_bound[1][1],
            )
            + 1,
        ),
    )

```

The similarity metric is SAD, which is the sum of absolute differences between two blocks:

```

In [6]: from numpy.typing import NDArray

def get_score_sad(
    block_pair: tuple[NDArray, NDArray],
) -> int:
    from numpy import abs

    return abs(block_pair[0] - block_pair[1]).sum(dtype=int)

```

Load the images and extract their luma component:

```

In [7]: import PIL.Image as Image
from numpy import asarray

reference_frame = Image.open("../resources/foreman_qcif_0_rgb.bmp").convert("L")
current_frame = Image.open("../resources/foreman_qcif_1_rgb.bmp").convert("L")

reference_buffer = asarray(reference_frame)
current_buffer = asarray(current_frame)

```

```

In [8]: grid_size = get_grid_size(current_frame)
block_index_bound = get_block_index_bound(current_frame)

display(
    dict(
        grid_size=grid_size,
        block_index_bound=block_index_bound,
    )
)

```

```
{'grid_size': (176, 144), 'block_index_bound': ((0, 175), (0, 143))}
```

Perform full-search block-matching algorithm and calculate the motion vectors (`reference - current`):

```
In [9]: from sys import maxsize

motion_vectors_by_full_search: list[list[tuple[int, int]]] = []

center_block_x_indexes, center_block_y_indexes = get_block_indexes(
    grid_size, block_size
)
for center_block_y_index in center_block_y_indexes:

    motion_vectors_x: list[tuple[int, int]] = []
    for center_block_x_index in center_block_x_indexes:
        center_block = current_buffer[
            center_block_y_index : center_block_y_index + block_size[1],
            center_block_x_index : center_block_x_index + block_size[0],
        ]

        search_block_x_indexes, search_block_y_indexes = get_search_block_indexes(
            (center_block_x_index, center_block_y_index),
            search_block_index_range,
            block_index_bound,
        )
        best_score = maxsize
        motion_vector: tuple[int, int] = None
        for search_block_y_index in search_block_y_indexes:
            for search_block_x_index in search_block_x_indexes:
                search_block = reference_buffer[
                    search_block_y_index : search_block_y_index + block_size[1],
                    search_block_x_index : search_block_x_index + block_size[0],
                ]
                score = get_score_sad((search_block, center_block))

                if best_score > score:
                    best_score = score
                    motion_vector = (
                        search_block_x_index - center_block_x_index,
                        search_block_y_index - center_block_y_index,
                    )

            motion_vectors_x.append(motion_vector)

    motion_vectors_by_full_search.append(motion_vectors_x)
```

Render the output:

```
In [10]: from IPython.display import display, Markdown

table_markdown_str = "| y \\ x |"
for center_block_x_index in center_block_x_indexes:
    table_markdown_str += f" {center_block_x_index} |"
table_markdown_str += "\n"

table_markdown_str += (
    "|-----|" + "-----|" * len(center_block_x_indexes) + "\n"
)

for center_block_y_index, motion_vectors_x in zip(
    center_block_y_indexes, motion_vectors_by_full_search
):
    table_markdown_str += f"| {center_block_y_index} |"
    for motion_vector in motion_vectors_x:
        table_markdown_str += f" {motion_vector} |"
    table_markdown_str += "\n"

display(
    Markdown(
        f"Display the motion vectors `(mx, my)` in the table below:\n{table_markdown_str}"
    )
)
```

Display the motion vectors (m_x, m_y) in the table below:

$y \setminus x$	0	16	32	48	64	80	96	112	128	144	160
0	(0, 0)	(0, 0)	(0, 0)	(0, 0)	(0, 0)	(0, 0)	(-12, 0)	(-6, 0)	(-4, 0)	(-3, 0)	(-16, 0)
16	(0, -16)	(0, 0)	(0, 0)	(0, 0)	(0, -2)	(0, -2)	(-6, 0)	(-14, -7)	(-15, -14)	(-16, -13)	(0, 0)
32	(0, 0)	(0, 0)	(0, 0)	(0, 0)	(0, -16)	(0, 0)	(-5, 0)	(-11, -3)	(-14, -4)	(0, -16)	(-10, -7)
48	(0, 0)	(0, 0)	(-13, -1)	(-3, -4)	(-13, 0)	(-2, -8)	(-6, 0)	(0, 0)	(0, 0)	(-5, -9)	(-1, -16)
64	(0, -7)	(-6, -2)	(0, 0)	(-4, -11)	(-16, -9)	(-16, -12)	(-7, 0)	(0, 0)	(0, 0)	(0, 0)	(0, 0)
80	(0, 0)	(-7, 0)	(-6, -3)	(0, -6)	(-2, -2)	(-16, 0)	(-6, 0)	(-2, 0)	(-3, -6)	(0, -6)	(-6, -7)
96	(0, -2)	(-14, -5)	(-6, -2)	(-7, 0)	(-3, -15)	(-15, -10)	(-16, -12)	(-3, 0)	(-14, -10)	(-12, -14)	(-1, -7)
112	(0, -15)	(-14, -16)	(-13, 0)	(-5, 0)	(0, -16)	(-1, 0)	(-4, 0)	(-3, -5)	(-16, -16)	(-16, -5)	(-6, -13)
128	(0, -5)	(-13, -8)	(-15, 0)	(-16, 0)	(-14, -13)	(-15, -1)	(0, 0)	(-15, -6)	(-16, -14)	(0, 0)	(0, 0)

Task 2

Motion Estimation

Following the previous question, please implement the diamond-search algorithm.

Solution of Task 2

The diamond search pattern of radius 2:

```
plaintext
o: search block index
x: center block index (also search block index)
+: other pixel
```

```
+ + + + +
+ + + o + +
+ + o + o + +
+ o + x + o +
+ + o + o + +
+ + + o + + +
+ + + + +
```

Write this concept into a function:

```
In [11]: def get_diamond_search_block_indexes(
    center_block_index: tuple[int, int],
    search_block_radius: int,
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
    block_size: tuple[int, int],
) -> Iterable[tuple[int, int]]:
    def get_diamond_search_block_index_relative(search_block_radius: int):
        search_block_radius = max(search_block_radius, 0)
        if search_block_radius > 0:
            yield (-search_block_radius, 0)
        for rx in range(-search_block_radius + 1, 0):
            ry = rx + search_block_radius
            yield (rx, -ry)
            yield (rx, +ry)
        if search_block_radius > 0:
            yield (0, -search_block_radius)
        yield (0, 0)
        if search_block_radius > 0:
            yield (0, +search_block_radius)
        for rx in range(1, search_block_radius):
            ry = rx - search_block_radius
            yield (rx, +ry)
            yield (rx, -ry)
        if search_block_radius > 0:
            yield (+search_block_radius, 0)

    for search_block_index_relative in get_diamond_search_block_index_relative(
        search_block_radius
    ):
        search_block_index = (
            center_block_index[0] + search_block_index_relative[0],
            center_block_index[1] + search_block_index_relative[1],
        )
        if (
            block_index_bound[0][0]
            <= search_block_index[0]
            <= block_index_bound[0][1]
            and block_index_bound[1][0]
            <= search_block_index[1]
            <= block_index_bound[1][1]
            and block_index_bound[0][0]
            <= search_block_index[0] + block_size[0] - 1
            <= block_index_bound[0][1]
            and block_index_bound[1][0]
            <= search_block_index[1] + block_size[1] - 1
            <= block_index_bound[1][1]
        ):
            yield search_block_index
```

Take this as an example:

```
plaintext
o: search block index
x: center block index (also search block index)
+: other pixel
```

```
+ o + o + +
o + + + o +
+ + x + + o
```

```

0 + + + 0 +
+ 0 + 0 + +
+ + 0 + + +

```

```

In [12]: display(
    list(
        get_diamond_search_block_indexes(
            center_block_index=(2, 2),
            search_block_radius=3,
            block_index_bound=block_index_bound,
            block_size=block_size,
        )
    )
)

```

```

[(0, 1),
 (0, 3),
 (1, 0),
 (1, 4),
 (2, 2),
 (2, 5),
 (3, 0),
 (3, 4),
 (4, 1),
 (4, 3),
 (5, 2)]

```

Perform diamond-search block-matching algorithm and calculate the motion vectors (`reference - current`):

```

In [13]: search_block_radius_init = block_size[0] // 2
display(search_block_radius_init)

```

8

```

In [14]: from sys import maxsize

motion_vectors_by_diamond_search: list[list[tuple[int, int]]] = []

center_block_x_indexes, center_block_y_indexes = get_block_indexes(
    grid_size, block_size
)
for center_block_y_index in center_block_y_indexes:

    motion_vectors_x: list[tuple[int, int]] = []
    for center_block_x_index in center_block_x_indexes:
        current_center_block_x_index = reference_center_block_x_index = (
            center_block_x_index
        )
        current_center_block_y_index = reference_center_block_y_index = (
            center_block_y_index
        )
        center_block = current_buffer[
            current_center_block_y_index : current_center_block_y_index
            + block_size[1],
            current_center_block_x_index : current_center_block_x_index
            + block_size[0],
        ]

        search_block_radius = search_block_radius_init
        while search_block_radius > 0:
            search_block_indexes = get_diamond_search_block_indexes(
                (
                    reference_center_block_x_index,
                    reference_center_block_y_index,
                ),
                search_block_radius,
                block_index_bound,
                block_size,
            )
            best_score = maxsize
            best_reference_center_block_x_index: int = None
            best_reference_center_block_y_index: int = None
            for (
                search_block_x_index,
                search_block_y_index,
            ) in search_block_indexes:
                search_block = reference_buffer[
                    search_block_y_index : search_block_y_index + block_size[1],
                    search_block_x_index : search_block_x_index + block_size[0],
                ]
                score = get_score_sad((search_block, center_block))
                if best_score > score:
                    best_score = score
                    best_reference_center_block_x_index = search_block_x_index
                    best_reference_center_block_y_index = search_block_y_index

            if (
                reference_center_block_x_index
                == best_reference_center_block_x_index
                and reference_center_block_y_index
                == best_reference_center_block_y_index
            ):
                search_block_radius -= 1

```

```

reference_center_block_x_index = best_reference_center_block_x_index
reference_center_block_y_index = best_reference_center_block_y_index

motion_vector = (
    reference_center_block_x_index - current_center_block_x_index,
    reference_center_block_y_index - current_center_block_y_index,
)
motion_vectors_x.append(motion_vector)

motion_vectors_by_diamond_search.append(motion_vectors_x)

```

Render the output:

```

In [15]: from IPython.display import display, Markdown

table_markdown_str = "| y \\ x |"
for center_block_x_index in center_block_x_indexes:
    table_markdown_str += f" {center_block_x_index} |"
table_markdown_str += "\n"

table_markdown_str += (
    "|-----|" + "-----|" * len(center_block_x_indexes) + "\n"
)

for center_block_y_index, motion_vectors_x in zip(
    center_block_y_indexes, motion_vectors_by_diamond_search
):
    table_markdown_str += f"| {center_block_y_index} |"
    for motion_vector in motion_vectors_x:
        table_markdown_str += f" {motion_vector} |"
    table_markdown_str += "\n"

display(
    Markdown(
        f"Display the motion vectors `(mx, my)` in the table below:\n{table_markdown_str}"
    )
)

```

Display the motion vectors (mx, my) in the table below:

y\x	0	16	32	48	64	80	96	112	128	144	160
0	(0, 0)	(0, 0)	(0, 0)	(0, 0)	(8, 14)	(6, 21)	(-4, 19)	(-6, 0)	(-4, 0)	(14, 16)	(-4, 23)
16	(0, 0)	(0, 0)	(0, 0)	(9, 12)	(19, -3)	(8, 3)	(-5, 4)	(-6, 5)	(-15, -14)	(0, 3)	(0, 0)
32	(0, 0)	(0, 0)	(0, 0)	(9, -14)	(24, -4)	(0, 0)	(-5, 0)	(-11, -3)	(11, 10)	(-15, 11)	(-10, -7)
48	(17, -6)	(0, 0)	(-2, -5)	(7, -8)	(-15, 3)	(-4, 1)	(-5, 1)	(2, 1)	(3, -6)	(0, 0)	(0, 0)
64	(17, -13)	(-6, -2)	(0, 0)	(7, -16)	(-1, 12)	(2, 3)	(-4, 9)	(2, -2)	(0, 0)	(0, 0)	(0, 0)
80	(0, 9)	(0, 16)	(-6, -3)	(9, 8)	(-2, -2)	(-15, 3)	(7, 5)	(-2, 1)	(17, 4)	(1, -6)	(0, 0)
96	(0, -2)	(-14, -5)	(0, 7)	(-1, 4)	(1, 0)	(5, 11)	(-7, 11)	(-9, 10)	(-14, -10)	(3, -4)	(-1, -7)
112	(0, -23)	(-14, 4)	(-16, 8)	(-1, 4)	(10, -32)	(0, 1)	(-4, 0)	(-3, -5)	(0, 0)	(-19, -5)	(-6, -13)
128	(0, -5)	(-13, -8)	(-29, -4)	(-16, 0)	(-14, -13)	(19, -1)	(1, -2)	(0, 0)	(15, -4)	(9, 0)	(0, 0)

Task 3

Intra-frame Prediction

Please apply intra-prediction to the luma component of `foreman_qcif_0_rgb.bmp`.

You only need to implement the four modes (Mode 0, 1, 2, and 4) for the 16x16 luma MB. You do not make an intra-prediction to the top-left MB since there is no predictor for it.

The similarity metric is also SAD. If any pixels are unavailable for a mode, you will not choose it. Please plot the mode for each MB using the example figure below.

```
plaintext
| x | 1 | ... | 2 |
| 4 | 1 | ... | 2 |
| ... | ... | ... | ... |
| 0 | 0 | ... | 4 |
| 0 | 0 | ... | 4 |
```

Solution of Task 3

There are four modes for 16x16 macroblocks in intra-frame prediction:

- Mode 0: Vertical
- Mode 1: Horizontal
- Mode 2: DC
- Mode 4: Diagonal down-right

To simplify illustrations, the block size downgrades to 4x4.

The encoded and prediction partitions are illustrated as follows:

```
plaintext
e: encoded pixel (source)
p: predicted pixel (target)

| Mode 0 | | Mode 1 | | Mode 2 | | Mode 4 | |
|-----| |-----| |-----| |-----| |
| e e e e | | e p p p p | | e e e e | | e e e e | |
| p p p p | | e p p p p | | e p p p p | | e p p p p | |
| p p p p | | e p p p p | | e p p p p | | e p p p p | |
| p p p p | | e p p p p | | e p p p p | | e p p p p | |
| p p p p | | e p p p p | | e p p p p | | p p p p | |
```

The predicted data is calculated as the following illustrations:

```
plaintext
Before:

| Mode 0 | | Mode 1 | | Mode 2 | | Mode 4 | |
|-----| |-----| |-----| |-----| |
| a b c d | | i . . . . | | a b c d | | m a b c | |
| . . . . | | j . . . . | | j . . . . | | j . . . . | |
| . . . . | | k . . . . | | k . . . . | | k . . . . | |
| . . . . | | l . . . . | | l . . . . | | . . . . | |
```

After:

```
| Mode 0 | | Mode 1 | | Mode 2 | | Mode 4 | |
|-----| |-----| |-----| |-----| |
| a b c d | | i i i i i | | a b c d | | m a b c | |
| a b c d | | i i i i i | | i u u u u | | i m a b c | |
| a b c d | | j j j j j | | j u u u u | | j i m a b | |
| a b c d | | k k k k k | | k u u u u | | k j i m a | |
| a b c d | | l l l l l | | l u u u u | | l j i m | |
```

* u = the average of a, b, c, d, i, j, k, l

Wrap these concepts into functions:

```
In [16]: from numpy.typing import NDArray
from typing import Optional

def has_top_predictor(
    block_index: tuple[int, int],
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
) -> bool:
```



```

    return (
        block_index_bound[1][0] <= block_index[1] - 1 <= block_index_bound[1][1]
    )

def has_left_predictor(
    block_index: tuple[int, int],
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
) -> bool:
    return (
        block_index_bound[0][0] <= block_index[0] - 1 <= block_index_bound[0][1]
    )

def get_predicted_block_in_vertical_mode(
    frame_buffer: NDArray,
    block_index: tuple[int, int],
    block_size: tuple[int, int],
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
) -> Optional[NDArray]:
    from numpy import full

    if not has_top_predictor(block_index, block_index_bound):
        return

    top_predictor_buffer = frame_buffer[
        block_index[1] - 1,
        block_index[0] : block_index[0] + block_size[0],
    ]
    predicted_block = full(
        (block_size[1], block_size[0]),
        top_predictor_buffer,
    )

    return predicted_block

def get_predicted_block_in_horizontal_mode(
    frame_buffer: NDArray,
    block_index: tuple[int, int],
    block_size: tuple[int, int],
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
) -> Optional[NDArray]:
    from numpy import full

    if not has_left_predictor(block_index, block_index_bound):
        return

    left_predictor_buffer = frame_buffer[
        block_index[1] : block_index[1] + block_size[1],
        block_index[0] - 1,
    ]
    predicted_block = full(
        (block_size[1], block_size[0]),
        left_predictor_buffer.reshape(-1, 1),
    )

    return predicted_block

def get_predicted_block_in_dc_mode(
    frame_buffer: NDArray,
    block_index: tuple[int, int],
    block_size: tuple[int, int],
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
) -> Optional[NDArray]:
    from numpy import full

    if not has_left_predictor(
        block_index,
        block_index_bound,
    ) or not has_top_predictor(
        block_index,
        block_index_bound,
    ):
        return

    top_predictor_buffer = frame_buffer[
        block_index[1] - 1,
        block_index[0] : block_index[0] + block_size[0],
    ]
    left_predictor_buffer = frame_buffer[
        block_index[1] : block_index[1] + block_size[1],
        block_index[0] - 1,
    ]
    average_value = (
        top_predictor_buffer.sum(dtype=int)
        + left_predictor_buffer.sum(dtype=int)
    ) // (top_predictor_buffer.size + left_predictor_buffer.size)
    predicted_block = full((block_size[1], block_size[0]), average_value)

    return predicted_block

```

```

def get_predicted_block_in_diagonal_downright_mode(
    frame_buffer: NDArray,
    block_index: tuple[int, int],
    block_size: tuple[int, int],
    block_index_bound: tuple[tuple[int, int], tuple[int, int]],
) -> Optional[NDArray]:
    from numpy import empty

    if not has_left_predictor(
        block_index,
        block_index_bound,
    ) or not has_top_predictor(
        block_index,
        block_index_bound,
    ):
        return

    predicted_block = empty(
        (block_size[1], block_size[0]), dtype=frame_buffer.dtype
    )
    diag_size = min(block_size[0], block_size[1])

    for predict_count, predictor_y_index_relative in zip(
        range(1, diag_size + 1), range(diag_size - 2, -2, -1)
    ):
        predictor_index = (
            block_index[0] - 1,
            block_index[1] + predictor_y_index_relative,
        )
        for predicted_index_relative in range(predict_count):
            predicted_index = (
                predicted_index_relative,
                predicted_index_relative + predictor_y_index_relative + 1,
            )
            predicted_block[predicted_index[1], predicted_index[0]] = (
                frame_buffer[
                    predictor_index[1],
                    predictor_index[0],
                ]
            )

    for predict_count, predictor_x_index_relative in zip(
        range(diag_size - 1, 0, -1), range(0, diag_size - 1)
    ):
        predictor_index = (
            block_index[0] + predictor_x_index_relative,
            block_index[1] - 1,
        )
        for predicted_index_relative in range(predict_count):
            predicted_index = (
                predicted_index_relative + predictor_x_index_relative + 1,
                predicted_index_relative,
            )
            predicted_block[predicted_index[1], predicted_index[0]] = (
                frame_buffer[
                    predictor_index[1],
                    predictor_index[0],
                ]
            )

    return predicted_block

```

Load the image and extract the luma component:

```

In [17]: import PIL.Image as Image
from numpy import asarray

source_frame = Image.open("../resources/foreman_qcif_0_rgb.bmp").convert("L")
source_buffer = asarray(source_frame)

```

```

In [18]: grid_size = get_grid_size(source_frame)
block_index_bound = get_block_index_bound(source_frame)

display(
    dict(
        grid_size=grid_size,
        block_index_bound=block_index_bound,
    )
)

```

```
{'grid_size': (176, 144), 'block_index_bound': ((0, 175), (0, 143))}
```

Perform intra-frame prediction and calculate the predicted mode and frame:

```

In [19]: from numpy import zeros_like
from sys import maxsize

modes: list[list[str]] = []
predicted_buffer = zeros_like(source_buffer)

prediction_functions = {

```

```

0: get_predicted_block_in_vertical_mode,
1: get_predicted_block_in_horizontal_mode,
2: get_predicted_block_in_dc_mode,
4: get_predicted_block_in_diagonal_downright_mode,
}

block_x_indexes, block_y_indexes = get_block_indexes(grid_size, block_size)
for block_y_index in block_y_indexes:

    modes_x: list[str] = []
    for block_x_index in block_x_indexes:
        source_block = source_buffer[
            block_y_index : block_y_index + block_size[1],
            block_x_index : block_x_index + block_size[0],
        ]

        best_score = maxsize
        best_mode = None
        best_predicted_block = None
        for mode, prediction_function in prediction_functions.items():
            predicted_block = prediction_function(
                source_block,
                (block_x_index, block_y_index),
                block_size,
                block_index_bound,
            )
            if predicted_block is not None:
                score = get_score_sad((predicted_block, source_block))
                if best_score > score:
                    best_score = score
                    best_mode = mode
                    best_predicted_block = predicted_block

        modes_x.append(best_mode)

    if best_predicted_block is not None:
        predicted_buffer[
            block_y_index : block_y_index + block_size[1],
            block_x_index : block_x_index + block_size[0],
        ] = best_predicted_block

modes.append(modes_x)

```

Render the output:

```

In [20]: from IPython.display import display, Markdown

table_markdown_str = "|"
for block_x_index in block_x_indexes:
    table_markdown_str += f"  |"
table_markdown_str += "\n"

table_markdown_str += "|" + "---|" * len(block_x_indexes) + "\n"

for modes_x in modes:
    table_markdown_str += "|"
    for mode in modes_x:
        if mode is None:
            mode = "x"
        table_markdown_str += f" {mode} |"
    table_markdown_str += "\n"

display(
    Markdown(
        f"Display the intra prediction modes in the table below:\n{table_markdown_str}"
    )
)

```

Display the intra prediction modes in the table below:

x	1	1	1	1	1	1	1	1	1	1
0	2	2	2	2	2	2	2	2	2	2
0	2	2	2	2	1	4	2	2	2	2
0	2	2	2	2	2	2	2	2	2	2
0	2	2	2	2	2	2	2	2	2	2
0	2	2	2	2	2	2	2	2	2	2
0	2	2	2	2	2	2	2	2	2	0
0	2	2	2	2	2	2	2	2	2	2
0	2	2	2	2	2	2	2	2	2	2

```

In [21]: display(Markdown("The source frame (Luma component):"))
display(source_frame)
display(Markdown("The predicted frame (Luma component):"))
display(Image.fromarray(predicted_buffer, mode="L"))

```

The source frame (Luma component):



The predicted frame (Luma component):

