

$$1. \left[\begin{array}{ccc|c} 1 & 2 & -3 & 5 \\ 2 & 1 & -3 & 13 \\ -1 & 1 & 0 & -8 \end{array} \right]$$

$R_2 - 2R_1; R_3 + R_1$

$$\left[\begin{array}{ccc|c} 1 & 2 & -3 & 5 \\ 0 & -3 & 3 & 3 \\ 0 & 3 & -3 & -3 \end{array} \right]$$

$$y = x - 8$$

$$2x + x - 8 - 3z = 13$$

$$3x - 3z = 21$$

$$x - z = 7$$

$$x = 7 + z$$

$$y = z - 1$$

$$7 + z + 2z - 2 - 3z = 5$$

$$5 + 0z = 5$$

$$14 + 2z + z - 1 - 3z = 13$$

$$13 + 0z = 13$$

infinite solutions

$$3. AB \begin{bmatrix} 4 & -3 \\ -3 & 5 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & 4 \\ -2 & -2 \end{bmatrix}$$

$$3 \times 2 \times 2 \times 2$$

$$= \begin{bmatrix} 4 \cdot 4 & 16 + 6 \\ -3 + 15 & -12 - 10 \\ 3 & -2 \end{bmatrix}$$

$$= \begin{bmatrix} -5 & 22 \\ 12 & -22 \\ 3 & -2 \end{bmatrix}$$

$$4 \times 2 \quad 2 \times 3$$