

# Day1

December 16, 2023 5:43 PM

Given an array of integers `nums` which is sorted in ascending order, and an integer `target`, write a function to search target in `nums`. If target exists, then return its index. Otherwise, return -1. You must write an algorithm with  $O(\log n)$  runtime complexity.

**Example 1:**  
**Input:** `nums = [-1,0,3,5,9,12]`, `target = 9`  
**Output:** 4  
**Explanation:** 9 exists in `nums` and its index is 4  
**Example 2:**  
**Input:** `nums = [-1,0,3,5,9,12]`, `target = 2`  
**Output:** -1  
**Explanation:** 2 does not exist in `nums` so return -1

From <<https://leetcode.com/problems/binary-search/>>

Basic thought:  
Divide the array into two parts, and to see if it's in the first range of array, if not, switch to the second array. Repeat the process.

```
Version 1 : [left, right]
Left = 0
Right = numSize - 1
While(left <= right):
    Middle = (left + right) / 2
    If(nums[middle] > target):
        Right = middle - 1
    Else if (nums[middle] < target):
        Left = middle + 1
    Else return middle
Return -1
```

```
Version 2: [left, right)
Left = 0
Right = numSize
While(left < right):
    Middle = (left + right) / 2
    If(nums[middle] > target):
        Right = middle
    Else if (nums[middle] < target):
        Left = middle + 1
    Else return middle
Return -1
```

Given an integer array `nums` and an integer `val`, remove all occurrences of `val` in `nums` [in-place](#). The order of the elements may be changed. Then return the *number of elements* in `nums` which are *not equal* to `val`.

Consider the number of elements in `nums` which are not equal to `val` be `k`, to get accepted, you need to do the following things:

- Change the array `nums` such that the first `k` elements of `nums` contain the elements which are not equal to `val`. The remaining elements of `nums` are not important as well as the size of `nums`.
- Return `k`.

**Custom Judge:**  
The judge will test your solution with the following code:  

```
int[] nums = [...]; // Input array
int val = ...; // Value to remove
int[] expectedNums = [...]; // The expected answer with correct length.
// It is sorted with no values equaling val.
int k = removeElement(nums, val); // Calls your implementation
assert k == expectedNums.length;
sort(nums, 0, k); // Sort the first k elements of nums
for (int i = 0; i < actualLength; i++) {
    assert nums[i] == expectedNums[i];
}
```

  
If all assertions pass, then your solution will be **accepted**.

**Example 1:**  
**Input:** `nums = [3,2,2,3]`, `val = 3`  
**Output:** 2, `nums = [2,2,...]`  
**Explanation:** Your function should return `k = 2`, with the first two elements of `nums` being 2. It does not matter what you leave beyond the returned `k` (hence they are underscores).  
**Example 2:**  
**Input:** `nums = [0,1,2,2,3,0,4,2]`, `val = 2`  
**Output:** 5, `nums = [0,1,4,0,3,...]`  
**Explanation:** Your function should return `k = 5`, with the first five elements of `nums` containing 0, 0, 1, 3, and 4. Note that the five elements can be returned in any order. It does not matter what you leave beyond the returned `k` (hence they are underscores).

**Constraints:**

- `0 <= nums.length <= 100`
- `0 <= nums[i] <= 50`
- `0 <= val <= 100`

From <<https://leetcode.com/problems/remove-element/>>

Given an integer array `nums` sorted in **non-decreasing** order, return an array of *the squares of each number* sorted in non-decreasing order.

**Example 1:**  
**Input:** `nums = [-4,-1,0,3,10]`  
**Output:** `[0,1,9,16,100]`  
**Explanation:** After squaring, the array becomes `[16,1,0,9,100]`. After sorting, it becomes `[0,1,9,16,100]`.  
**Example 2:**  
**Input:** `nums = [-7,-3,2,3,11]`  
**Output:** `[4,9,9,49,121]`

**Constraints:**

- `1 <= nums.length <= 10`
- `-10 <= nums[i] <= 10`
- `nums` is sorted in **non-decreasing** order.

From <<https://leetcode.com/problems/squares-of-a-sorted-array/>>

## Ordered Tree

A tree is ordered if there is a meaningful linear order among the children (Left to Right)

## Tree ADT

Accessor methods:

Position root()	Position parent(p)	Iterable children(p)	Integer numChildren(p)
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Query Methods:

Boolean	isInternal(p)	Boolean isExternal(p)	Boolean isRoot(p)
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## Binary Tree

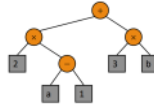
A binary tree is a tree with the following properties:  
Each internal node has at most two children  
Proper binary trees (or full): each node has zero or two children  
The children of a node are an ordered pair

Alternative recursive definition : A binary tree is either:

- A tree consisting of a single node, or
- A tree whose root has an ordered pair of children, each of which is a binary tree.

Binary Tree associated with an arithmetic expression

Internal nodes: operators  
External nodes: operands  
Example: arithmetic expression tree for the expression  $(2 \times (3 - 1) + (3 \times 3))$

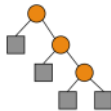


Binary Tree associated with a decision process

Internal nodes: questions with yes/no answer  
External nodes: decisions  
Example: dining decision



In a nonempty proper binary tree  $T$ , with  $n_e$  external nodes and  $n_i$  internal nodes, we have  $n_e = n_i + 1$ .



## Thought:

To delete an element, we have to put the elements behind it forward one memory location. We cannot delete it directly.

Use two pointers, one fast and one slow.  
Fast pointer is used to find the val (the target element) in the array.  
Slow pointer is the index of the array after deleting the elements.

```
Slow = 0
For ( fast = 0; fast < nums.size ; fast ++){
    If(nums[fast] != val){
        Nums[slow] = nums[fast]
        Slow ++
    }
}
```

Return slow

## Binary Tree ADT

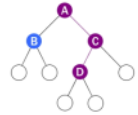
Methods:

Position left(p)	Position right(p)	Position sibling(p)
addLeft(p,e)	addRight(p,e)	set(p,e)
Attach(p,T1,T2)		

remove(p): Removes the node at position `p`, replacing it with its child (if any), and returns the element that had been stored at `p`; an error occurs if `p` has two children.

## Height and Depth

Example :



node A:

Height = 3 (no. of edges on longest path from A to A > C > D > leaf i.e. 3 edges)  
depth = 0

## Properties of A Binary Tree:

Notation

$n$  number of nodes  
 $e$  number of external nodes  
 $i$  number of internal nodes  
 $h$  height

- $A = 1 \leq n \leq 2^{h+1} - 1$
  - $1 \leq n_e \leq 2^h$
  - $A \leq n_i \leq 2^{h-1} - 1$
  - $\log(n+1) - 1 \leq h \leq n - 1$
- Also, if  $T$  is proper, then  $T$  has the following properties:
- $2n + 1 \leq n_e \leq 2^{h+1} - 1$
  - $A + 1 \leq n_i \leq 2^h$
  - $A \leq n_e \leq 2^{h-1} - 1$
  - $\log(n+1) - 1 \leq h \leq (n-1)/2$



In a nonempty proper binary tree  $T$ , with  $n_e$  external nodes and  $n_i$  internal nodes, we have  $n_e = n_i + 1$ .

