HW 4

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Clustering and PCA

First of all I started by cleaning the data. I centered and scaled the data.

Then, I applied k-means technique for clustering. I used k=2 as there were 2 types of wine by color, red and white, with 25 starts. In order to see if the k-means has clustered data points by wine color into red and white wine, I compare the averages of chemical properties for white wine and red wine in our original data with that of the clustered data.

```
## # A tibble: 2 x 13
     color fixed.acidity volatile.acidity citric.acid residual.sugar chlorides
## * <chr>
                    <dbl>
                                                                    <dbl>
                                      <dbl>
                                                   <dbl>
                                                                              <dbl>
## 1 red
                     8.32
                                      0.528
                                                   0.271
                                                                    2.54
                                                                             0.0875
## 2 white
                     6.85
                                      0.278
                                                   0.334
                                                                             0.0458
                                                                    6.39
##
     free.sulfur.dioxide total.sulfur.dioxide density
                                                             pH sulphates alcohol
## *
                    <dbl>
                                           <dbl>
                                                   <dbl> <dbl>
                                                                     <dbl>
                                                                             <dbl>
## 1
                     15.9
                                            46.5
                                                   0.997
                                                           3.31
                                                                    0.658
                                                                              10.4
## 2
                     35.3
                                           138.
                                                   0.994 3.19
                                                                    0.490
                                                                              10.5
##
     quality
       <dbl>
## *
## 1
        5.64
## 2
        5.88
##
                              volatile.acidity
                                                          citric.acid
          fixed.acidity
##
               8.2895922
                                     0.5319416
                                                            0.2695435
##
         residual.sugar
                                     chlorides
                                                 free.sulfur.dioxide
##
               2.6342666
                                     0.0883238
                                                           15.7647596
   total.sulfur.dioxide
##
                                       density
                                                                   рΗ
##
              48.6396835
                                     0.9967404
                                                            3.3097200
##
               sulphates
                                       alcohol
##
               0.6567194
                                    10.4015216
##
          fixed.acidity
                              volatile.acidity
                                                          citric.acid
##
             6.85167903
                                    0.27458385
                                                           0.33524928
##
         residual.sugar
                                     chlorides
                                                 free.sulfur.dioxide
##
             6.39402555
                                    0.04510424
                                                          35.52152864
##
  total.sulfur.dioxide
                                       density
                                                                   рH
           138.45848785
                                    0.99400486
                                                           3.18762464
##
##
              sulphates
                                       alcohol
##
             0.48880511
                                   10.52235888
```

If we compare averages of the chemical properties of red and white wine in our original data with the averages of chemical properties of red and white wine in clustered data, we can see that averages of chemical properties for red wine in both original and k-means clustered data are almost the same. Similarly, that averages of chemical properties for white wine are also pretty much the same in both original and clustered data. This hints towards the fact that k-means is easily capable of distinguishing the red wines from the white ones.

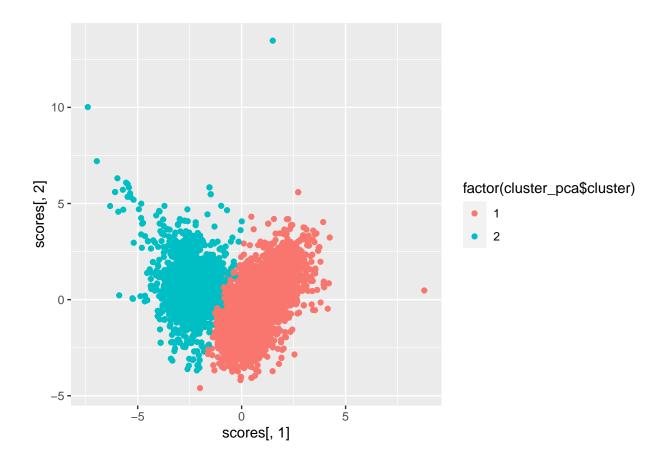
To further verify this, I have also made a confusion matrix. In the table, we can see that k-means has pretty accurately clustered data by wine color. With an accuracy of 98.5%, we can conclude that k-means clustering has done a very good job in terms of dimension reduction

```
## cluster
## color red_hat white_hat
## red 1575 24
## white 68 4830
```

[1] 0.9858396

After, k-means, I proceeded to perform Principal Component Analysis (PCA). As seen in the table below, the first three principal components form 64.3% of the total variance in the data set, which is significantly high. Hence, I used first three components to perform clustering.

```
## Importance of components:
##
                              PC1
                                     PC2
                                            PC3
                                                     PC4
                                                             PC5
                                                                     PC6
                                                                             PC7
## Standard deviation
                           1.7407 1.5792 1.2475 0.98517 0.84845 0.77930 0.72330
## Proportion of Variance 0.2754 0.2267 0.1415 0.08823 0.06544 0.05521 0.04756
  Cumulative Proportion 0.2754 0.5021 0.6436 0.73187 0.79732 0.85253 0.90009
##
                               PC8
                                       PC9
                                             PC10
                                                     PC11
## Standard deviation
                           0.70817 0.58054 0.4772 0.18119
## Proportion of Variance 0.04559 0.03064 0.0207 0.00298
## Cumulative Proportion 0.94568 0.97632 0.9970 1.00000
##
                          PC1
                                 PC2
                                       PC3
## fixed.acidity
                         -0.24
                                0.34 - 0.43
## volatile.acidity
                         -0.38
                                0.12 0.31
## citric.acid
                         0.15
                                0.18 - 0.59
## residual.sugar
                         0.35
                                0.33
                                      0.16
## chlorides
                         -0.29
                                0.32
                                      0.02
## free.sulfur.dioxide
                          0.43
                                0.07
                                      0.13
## total.sulfur.dioxide
                         0.49
                                0.09
                                      0.11
## density
                         -0.04
                               0.58
                                     0.18
                         -0.22 -0.16
## pH
                                     0.46
## sulphates
                         -0.29 0.19 -0.07
## alcohol
                         -0.11 -0.47 -0.26
```



```
## cluster
## color red_hat white_hat
## red 24 1575
## white 4816 82
```

[1] 0.01631522

The clustering done by using the scores from three principal components also did a good job. The accuracy level stood at 98.3 %. But, PCA is not as straight forward as k-means. I used the scores from the principal components to form the clusters. As the accuracy of k-means is relatively higher and it is straight forward, I conclude that it makes more sense to use k-means technique for the given data.

The quality of wine is being rated in a scale of 1-10, however, in our data set there is no rating of 1,2 or 10. Thus, the wine in our data set was rated between 2 and 9 inclusive. I performed k-means with k=7 and 25 starts.

```
##
                 cluster2$cluster
##
   wine$quality
                              3
                                        5
                                             6
                                                 7
##
                3
                     7
                              2
                                   5
                                        4
                                             6
                                                 2
                              2
                    24
                        14
                                  65
                                       21
                                                26
##
##
                5
                  651 183
                             30 449
                                      77
                                          479
                                              269
##
                  640
                       259
                             19 549
                                          346 474
##
                  122 138
                              2
                                           43 191
                                137
                                     446
##
                    22
                         12
                              0
                                  27
                                      97
                                             4
                                                31
##
                9
                     0
                          0
                              0
                                   1
                                        4
                                             0
                                                 0
```

We can see in the confusion matrix that k-means clustering has not been able to clearly distinguish between different qualities of wine. For example, all of the clusters have significant number of wines rated 5, 6 and 7. There is no clear distinction.

Market Segmentation

First of all I started by cleaning the data set. The data set originally contained 7,882 data points and 36 variables.

As there are lots of spam and pornography bots, I filtered out all the users whose tweet fell into 'spam' and 'adult' category. Then I deleted 'spam' and 'adult' variables form the data set. I also excluded 'uncategorized' and. 'chatter' variables from the data set as they did not seem to provide any insights in my analysis. So, I ended up with 32 variables and 7,309 data points.

In order to identify market segments, I performed cluster analysis. Since the data did not show any kinds of hierarchy, I resorted to K-means cluster analysis. I have used K-means++.

For using K-means clustering we need to find the optimal number of clusters or the value of K. In order to find the optimal value of K , I have used Elbow plot and CH index.

Figure 2.1 Elbow Plot

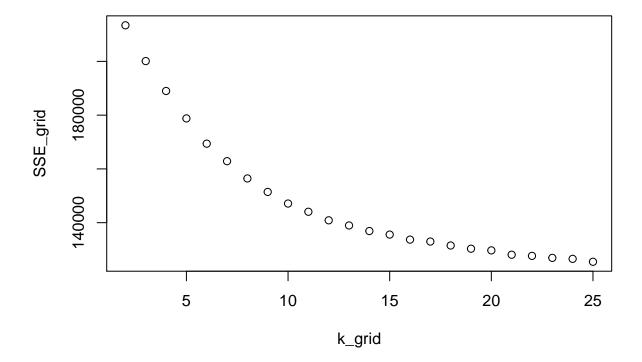
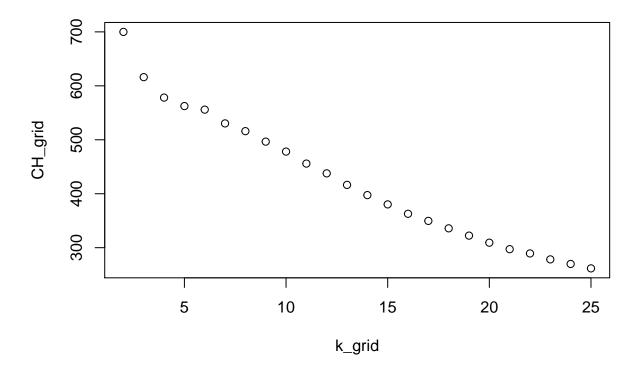
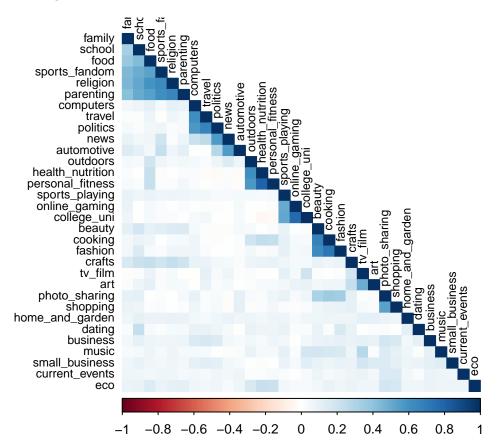


Figure 2.2 CH index plot



The optimal value of K is not clear from the graph. Nevertheless, these plots have hinted towards number 5. For further confirmation, I have plotted a correlogram and have tried to identify possible singularities among the variables.

Figure 2.3 Correlogram



From the correlogram, we can see that some subgroups of the variables are highly correlated with each other. The variables 'family', 'school', 'food', 'sports_fandom', 'religion' seems to be highly correlated. Likewise, 'Computers', 'travel', 'politics', 'news' and 'automotive' are correlated. 'Outdoors', 'health_nutrition' and 'personal_fitness' are correlated with each other. 'Sports_playing', 'online_gaming' and 'college_uni' are also correlated. Lastly, 'beauty', 'cooking' and 'fashion' also seem to have a significant correlation. Therefore, the correlogram corroborates that the optimal value of K is 5.

Summary of cluster 1

Mode FALSE TRUE ## logical 6448 861

Summary of Cluster 2

Mode FALSE TRUE ## logical 6739 570

Summary of Cluster 3

Mode FALSE TRUE ## logical 6626 683

Summary of Cluster 4

Mode FALSE TRUE ## logical 2855 4454

Summary of Cluster 5

Mode FALSE TRUE ## logical 6568 741

What are the clusters?

##	current_events	travel	<pre>photo_sharing</pre>	${\tt tv_film}$
##	1.5226481	1.2276423	2.7119628	1.0162602
##	sports_fandom	politics	food	family
##	1.1382114	1.2346109	2.0929152	0.7642276
##	home_and_garden	music	news	online_gaming
##	0.6248548	0.7468060	1.1068525	1.1521487
##	shopping	health_nutrition	college_uni	sports_playing
##	1.4901278	11.9349593	1.2810685	0.6701510
##	cooking	eco	computers	business
##	3.2775842	0.9024390	0.5528455	0.4680604
##	outdoors	crafts	automotive	art
##	2.6817654	0.6085947	0.6387921	0.7700348
##	religion	beauty	parenting	dating
##	0.7340302	0.4192799	0.7317073	1.0174216
##	school	personal_fitness	fashion	small_business
##	0.5563298	6.3925668	0.7793264	0.2868757
##	current_events	travel	photo_sharing	tv_film
##	1.7596491	1.5017544	6.0526316	1.2122807
##	sports_fandom	politics	food	family
##	1.1298246	1.3807018	1.0526316	0.8964912
##	home_and_garden	music	news	online_gaming
##	0.6245614	1.3140351	1.0175439	1.5280702
##		health_nutrition	college_uni	sports_playing
##	2.1035088	2.1929825	2.1052632	0.9368421
##	cooking	eco	computers	business
##	10.5122807	0.5614035	0.7368421	0.6228070
##	outdoors	crafts	automotive	art
##	0.7929825	0.6368421	0.8859649	0.9807018
##	religion	beauty	parenting	dating
##	0.8315789	3.8175439	0.7385965	0.9105263
##		personal_fitness	fashion	small_business
##	0.9736842	1.3298246	5.4105263	0.5210526
	0.0700012	1.0200210	0.1100200	0.0210020
##	current_events	travel	photo_sharing	tv_film
##	1.6368960	5.5519766	2.5065886	1.2254758
##	sports_fandom	politics	food	family
##	2.0190337	8.8550512	1.4597365	0.9341142
##	home_and_garden	music	news	online_gaming
##	0.6193265	0.6354319	5.2503660	1.1566618

##		health_nutrition	college_uni	sports_playing
##	1.3674963	1.6588580	1.6676428	0.7188873
##	cooking	eco	computers	business
##	1.2635432	0.5885798	2.4568082	0.6793558
##	outdoors	crafts	automotive	art
##	0.9121523	0.6354319	2.3396779	0.7510981
##	religion	beauty	parenting	dating
##	1.0263543	0.4597365	0.9311859	1.0614934
##		personal_fitness	fashion	small_business
##	0.7262079	1.0102489	0.6749634	0.4743777
##	current_events	travel	photo_sharing	tv_film
##	1.4499326	1.0880108	2.3298159	1.0498428
##	sports_fandom	politics	food	family
##	0.9696902	1.0159407	0.7608891	0.5875617
##	home_and_garden	music	news	online_gaming
##	0.4384823	0.5913785	0.6755725	1.1632241
##	shopping	health_nutrition	college_uni	sports_playing
##	1.2887292	1.0781320	1.5422093	0.5646610
##	cooking	eco	computers	business
##	0.8547373	0.3776381	0.3614728	0.3414908
##	outdoors	crafts	automotive	art
##	0.3834755	0.3643916	0.5756623	0.6349349
##	religion	beauty	parenting	dating
##	0.5246969	0.3354288	0.4492591	0.5534351
##		personal_fitness	fashion	small_business
##	0.4573417	0.6409969	0.5229008	0.2748092
##	current_events	travel	photo_sharing	tv_film
##	1.6518219	1.2955466	2.6545209	1.1106613
##	sports_fandom	politics	food	family
##	5.8475034	1.1160594	4.5087719	2.4601889
##	home_and_garden	music	news	online_gaming
##	0.6599190	0.7462888	1.0202429	1.2793522
##	shopping	$health_nutrition$	college_uni	sports_playing
##	1.4844804	1.8771930	1.5236167	0.8002699
##	cooking	eco	computers	business
##	1.6261808	0.6423752	0.7152497	0.4885290
##	outdoors	crafts	automotive	art
##	0.6990553	1.0634278	1.0256410	0.8839406
##	religion	beauty	parenting	dating
##	5.1916329	1.0877193	4.0013495	0.8299595
##		personal_fitness	fashion	small_business
##	2.6626181	1.1848853	1.0377868	0.3967611

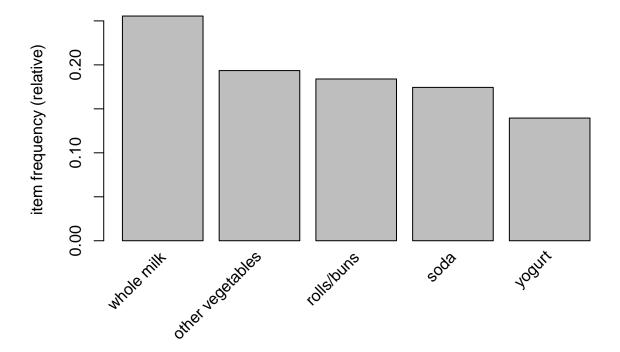
After running the k-means++ with K=5, I checked the number of data points in each cluster. The cluster with highest number of data points had 4454 data points. That is about 60 percent of the total number of data points I considered in the analysis. This cluster includes the people who have tweeted less than 2 times on an average in all the categories. This could mean that most of the followers of "NutrientH20" are not active users of "twitter" or social media in general. Despite not being active users of social media, these people are following "Nutrient20" which means that the current social media marketing strategy is working quite well.

The cluster with the lowest number of people, on an average tweeted more about 'photo sharing', 'cooking', and 'fashion'. Therefore, in order to attract and appeal to more of the people who are more interested in

photo sharing, cooking and fashion the company should position their brand in a way that it seems like it is related to photo sharing or cooking or fashion.

Association rules for grocery purchases

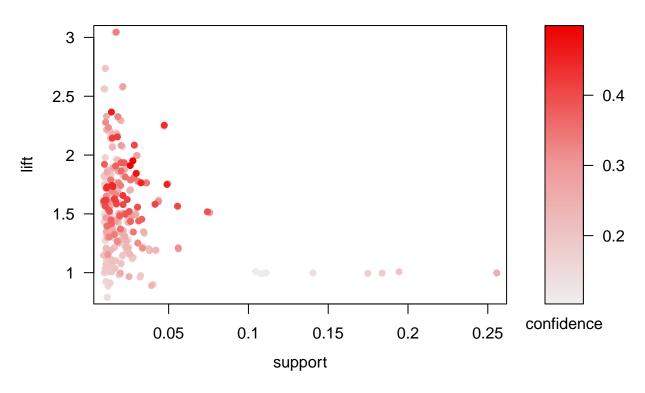
Figure 3.1 Top 5 items with highest support



In order to find various association rules I used 'apriori' function with support = 0.01, confidence= 0.1 and maximum length of 2. By doing so, I got a set of 339 rules. Then, I checked the items with highest support. As seen in the figure, top 5 items with highest support are whole milk, other vegetables, rolls/buns, soda and yogurt.

Figure 3.2 Plot of Association rules





In order to find strong associations, we need the association rules with high lift and high confidence. For picking up thresholds for lift and confidence, I made a plot of the association rules. As we can see in the figure 3.2, we do not have lot of points above the confidence of 0.3 and above the lift of 2. Therefore, I used threshold of 0.3 for the confidence and 2 for the lift. This give 9 association rules.

```
##
       lhs
                               rhs
                                                   support
                                                               confidence coverage
## [1] {onions}
                            => {other vegetables} 0.01423488 0.4590164
                                                                          0.03101169
   [2] {berries}
                            => {yogurt}
                                                   0.01057448 0.3180428
                                                                          0.03324860
  [3] {hamburger meat}
                            => {other vegetables} 0.01382816 0.4159021
                                                                          0.03324860
   [4] {cream cheese}
                            => {yogurt}
                                                   0.01240468 0.3128205
                                                                          0.03965430
   [5]
       {chicken}
                            => {other vegetables} 0.01789527 0.4170616
                                                                          0.04290798
  [6] {beef}
                            => {root vegetables}
##
                                                   0.01738688 0.3313953
                                                                          0.05246568
  [7] {curd}
                            => {yogurt}
                                                   0.01728521 0.3244275
                                                                          0.05327911
   [8] {whipped/sour cream} => {other vegetables} 0.02887646 0.4028369
                                                                          0.07168277
   [9] {root vegetables}
                            => {other vegetables} 0.04738180 0.4347015
                                                                         0.10899847
##
##
       lift
                count
  [1] 2.372268 140
   [2] 2.279848 104
   [3]
      2.149447 136
  [4] 2.242412 122
  [5] 2.155439 176
   [6] 3.040367 171
  [7] 2.325615 170
## [8] 2.081924 284
```

[9] 2.246605 466

We can see that almost all of associations that make sense. The first association in table shows that onions implies other vegetables. These two items definitely go together. Beef and root vegetables are also consumed together. Likewise, the association between hamburger meat and other vegetable also makes right sense.

Figure 3.3 Groceries association rules

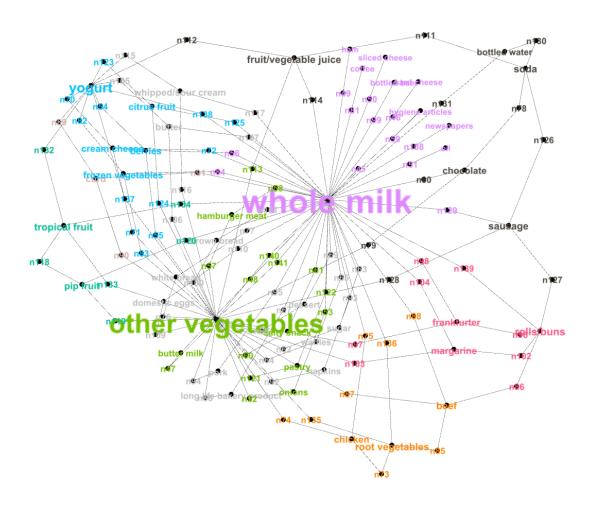


Figure 1: Groceries rules

The figure 3.3 can help us visualize the item sets. We can see other vegetables, butter milk, hamburger meat, onions form a set, which does make sense. Likewise, items like margarine, roll buns and frankfurter which are consumed together make a set. Similarly, we can see that items like citrus fruit, yogurt and cream cheese are grouped together. From an association point of view, it also makes perfect sense.

Author Attribution

<<DocumentTermMatrix (documents: 2500, terms: 32241)>>

```
## Non-/sparse entries: 473695/80128805
## Sparsity
                       : 99%
## Maximal term length: 49
## Weighting
                       : term frequency (tf)
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
##
     0.000
             5.802
                     7.822
                              8.754
                                    10.403
                                             37.594
```

I started by making a corpus containing all the 2500 documents by 50 authors from the training directory, after which I did some pre-processing and tokenization. I converted everything to lower case, removed numbers, removed punctuations, striped excess white-space, and removed stop words. After tokenization I created a document term matrix which contain 2500 rows, each row representing a document, and 32241 columns, each of which represent a term. I then deleted all the sparse terms. I removed all those terms with zero countsin more that 95% of the documents, after which I was left with 660 terms. I then created matrix of TF-IDF weighs using the document term matrix.

```
## Importance of first k=15 (out of 644) components:
##
                              PC1
                                      PC2
                                               PC3
                                                       PC4
                                                               PC5
                                                                       PC6
                                                                                PC7
## Standard deviation
                          3.61251 2.90050 2.59588 2.56025 2.43294 2.40581 2.23539
## Proportion of Variance 0.02026 0.01306 0.01046 0.01018 0.00919 0.00899 0.00776
## Cumulative Proportion
                          0.02026 0.03333 0.04379 0.05397 0.06316 0.07215 0.07991
##
                              PC8
                                      PC9
                                              PC10
                                                      PC11
                                                              PC12
                                                                      PC13
## Standard deviation
                          2.17112 2.14298 2.07460 2.04517 2.01322 1.89647 1.89484
## Proportion of Variance 0.00732 0.00713 0.00668 0.00649 0.00629 0.00558 0.00558
## Cumulative Proportion 0.08723 0.09436 0.10104 0.10754 0.11383 0.11941 0.12499
##
                             PC15
                          1.85654
## Standard deviation
## Proportion of Variance 0.00535
## Cumulative Proportion 0.13034
```

In the next step, I scrubbed off all the columns with entries equals to zero, after which I was left with 644 columns. Then, I conducted the Principal Component Analysis (PCA) with rank 15. 15 principal components were able to capture 13% variation of the data. After conducting the PCA, I created a new column named 'author' and entered author names corresponding to their respective documents.

After dimensionality reduction using PCA, I conducted multinomial logistic regression, k-nearest neighbors regression and random forest model with 15 principal components for prediction of author of a particular document.

After building the models using training set, I created a corpus from the testing set. The testing data also contained 50 authors and 50 documents per author totaling to 2500 documents. I repeated the tokenization steps and conducted other pre-processing step which I did with the training data, and created a document term matrix. Like before, I removed the terms that had count of zero in more than 95% of the documents and constructed a matrix of TF-IDF weights from document term matrix. In the next step, I scrubbed off all the columns with entries equals to zero after which I was left with 660 columns. Like for the training set, I conducted the Principal Component Analysis (PCA) with rank 15. 15 principal components were able to capture 13% variation of the data for the testing set as well. After conducting the PCA, I created a new column named 'author' and entered author names corresponding to their respective documents.

```
## <<DocumentTermMatrix (documents: 2500, terms: 33048)>>
## Non-/sparse entries: 480577/82139423
## Sparsity : 99%
## Maximal term length: 48
## Weighting : term frequency (tf)
```

```
##
      Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
##
     0.000
             5.783
                     7.671
                             8.602 10.244
                                            42.143
## Importance of first k=15 (out of 660) components:
##
                              PC1
                                      PC2
                                               PC3
                                                       PC4
                                                               PC5
                                                                       PC6
                                                                                PC7
                          3.70364 2.92879 2.63165 2.57208 2.44603 2.37248 2.24411
## Standard deviation
## Proportion of Variance 0.02078 0.01300 0.01049 0.01002 0.00907 0.00853 0.00763
## Cumulative Proportion 0.02078 0.03378 0.04427 0.05430 0.06336 0.07189 0.07952
                                                     PC11
                                                                     PC13
##
                              PC8
                                      PC9
                                              PC10
                                                             PC12
                                                                             PC14
                          2.20491 2.17896 2.09630 2.0391 2.01742 1.96086 1.95260
## Standard deviation
## Proportion of Variance 0.00737 0.00719 0.00666 0.0063 0.00617 0.00583 0.00578
                          0.08689 0.09408 0.10074 0.1070 0.11321 0.11903 0.12481
## Cumulative Proportion
##
                            PC15
## Standard deviation
                          1.8709
## Proportion of Variance 0.0053
## Cumulative Proportion 0.1301
```

Prediction accuracy of Multinomial logistic regression

[1] 0.0272

Prediction accuracy of k-nearest neighbours

[1] 0.0052

Prediction accuracy of randomforest

[1] 0.0344

In the next step, I made predictions on the test set using the models which I built using training data. I created confusion matrices for each of the 3 models and calculated accuracy rates. The highest level of accuracy that I could obtain was just 3.5 percetn using random forest