

广东工业大学考试试卷（A）

2019 — 2020 学年度第 2 学期

课程名称: Advanced Mathematics A(2) 学分 5.5 试卷满分 100 分

考试时间: June 21, 2020 (16th Week Sunday) 考试形式: Open exam

题 号	一	二	三	四	五	六	七	八	九	十	总分
评卷得分											
评卷签名											
复核得分											
复核签名											

Please answer in CHINESE or in ENGLISH or Bilingualism!

1、 Fill the correct answer in the blanks (4 points each, 16 points in all)

- (1) If $a = i - 2j + 2k$ and $b = i + j + k$, then $a \times b =$ _____.
- (2) Let $xz + xy^2 + yz = 3$, then $\frac{\partial z}{\partial x} =$ _____.
- (3) Let $u = xy^2 + z^3 - xyz$ at the point (1,1,2) in the direction ℓ (where $60^\circ, 45^\circ, 60^\circ$ are the direction angle of ℓ), then the directional derivative of $\frac{\partial u}{\partial \ell} \Big|_{(1,1,2)} =$ _____.
- (4) Find the double limits of $\lim_{(x,y) \rightarrow (0,0)} (x+y) \sin(\frac{1}{x^2+y^2}) =$ _____.

2. Multiple choice (3 points each, 12 points in all)

- (1) The radius of convergence of the power series $\sum_{n=1}^{\infty} nx^n$ is ().
- (A) 2 (B) 3 (C) 1 (D) 4

(2) Let $z = xy + \frac{x}{y}$, then $\frac{\partial z}{\partial y} \Big|_{(1,1)} = (\quad)$.

- (A) $\frac{1}{2}$ (B) $\frac{1}{3}$ (C) $-\frac{1}{2}$ (D) $-\frac{1}{3}$

(3) By Green's formula, evaluate the line integral of

$$I = \oint_{(C)} x^2 y dx - xy^2 dy = (\quad), \text{ where } (C) \text{ is the circle } x^2 + y^2 = R^2 \text{ with}$$

the positive direction.

- (A) $\frac{1}{2}$ (B) $\frac{\pi}{4} R^4$ (C) $-\frac{\pi}{4} R^4$ (D) 0

(4) Let $f(x, y, z) = x^2 + 2y^2 + 3z^2 + xy + 3x - 2y - 6z$,

then $\text{grad} f(0,0,0)$ is (\quad) .

- (A) $(3, -2, -6)$ (B) $(6, 3, 0)$ (C) $(3, 2, 6)$ (D) $(-3, -2, 6)$

3、Directions: There are 7 questions in this part. Evaluate the following questions and write steps: (72 points in all)

(1) **(10 points)** Find an equation of the plane that passes through $(2, -3, 5)$ and is parallel to the plane $3x + 5y - 7z = 11$

(2) **(10 points)** Find the radius of convergence, convergence interval and

convergence domain of the power series $\sum_{n=1}^{\infty} \frac{(-1)^n}{n} \left(\frac{1}{1+x} \right)^n$.

(3) **(10 points)** Suppose that $z = \sin(u + v)$, $u = xy$, $v = x^2 + y^2$. Find

$$\frac{\partial z}{\partial x}, \frac{\partial z}{\partial y}.$$

(4) **(10 points)** Find the maximum and minimum of the function

$$f(x, y) = (x-1)^2 + (y-2)^2 + 1$$

in the region $D = \{(x, y) | x^2 + y^2 \leq 20\}$.

(5) **(10 points)** Let $x^2 - 2y^2 + z^2 - 4x + 2z - 5 = 0$, Find $\frac{\partial z}{\partial x}, \frac{\partial z}{\partial y}$

(6) **(10 points)** Evaluate the double integral $\iint_D \frac{\sin(x+1)}{x} d\sigma$, where the domain of integration D is bounded by the line $y = x$ and the parabola $y = x^2$

(7) **(12 points)** Evaluate the triple $\iiint_{(\Omega)} y dv$, where the domain of integration (Ω) is bounded by $y = -\sqrt{1-x^2-z^2}$, $x^2 + z^2 = 1$ and $y = 1$.