

# Chapter 6

## Bottom-Up Parsing

# A Bottom-up Parse

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int \* int + int

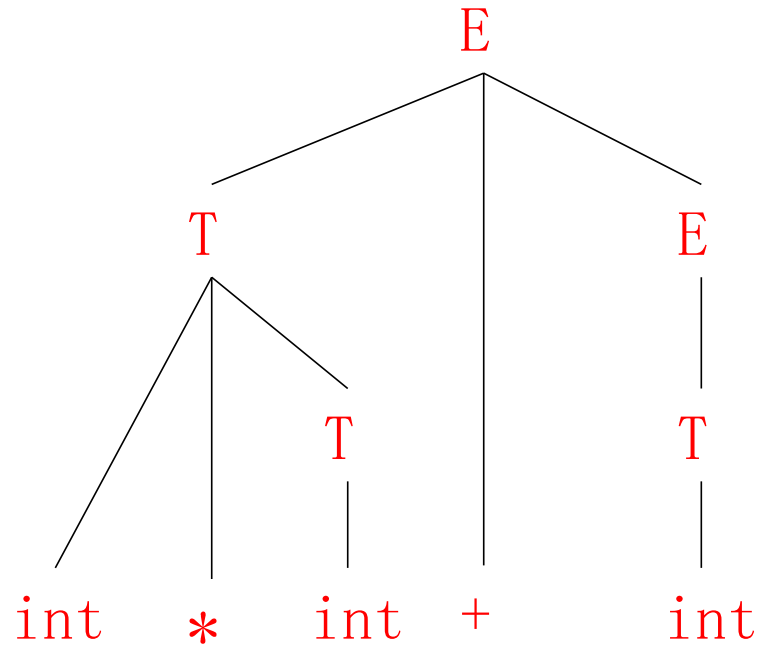
int \* T + int

T + int

T + T

T + E

E



## A Bottom-up Parse in Detail (4)

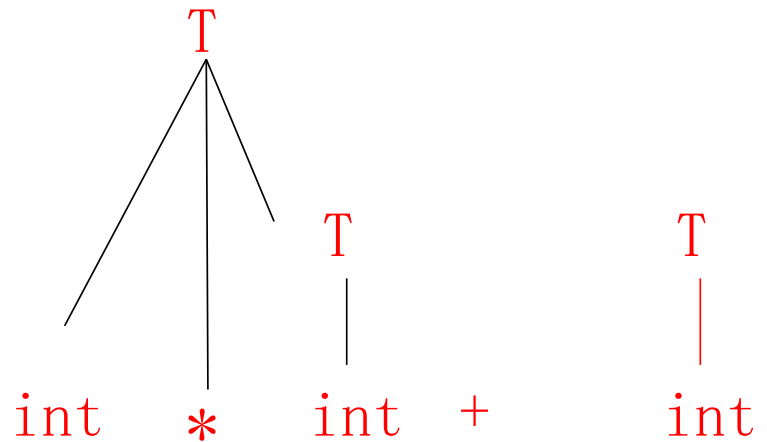
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int \* int + int

int \* T + int

T + int

T + T



# A Shift-Reduce Parse in Detail (11)

| int \* int + int

int | \* int + int

int \* | int + int

int \* int | + int

int \* T | + int

T | + int

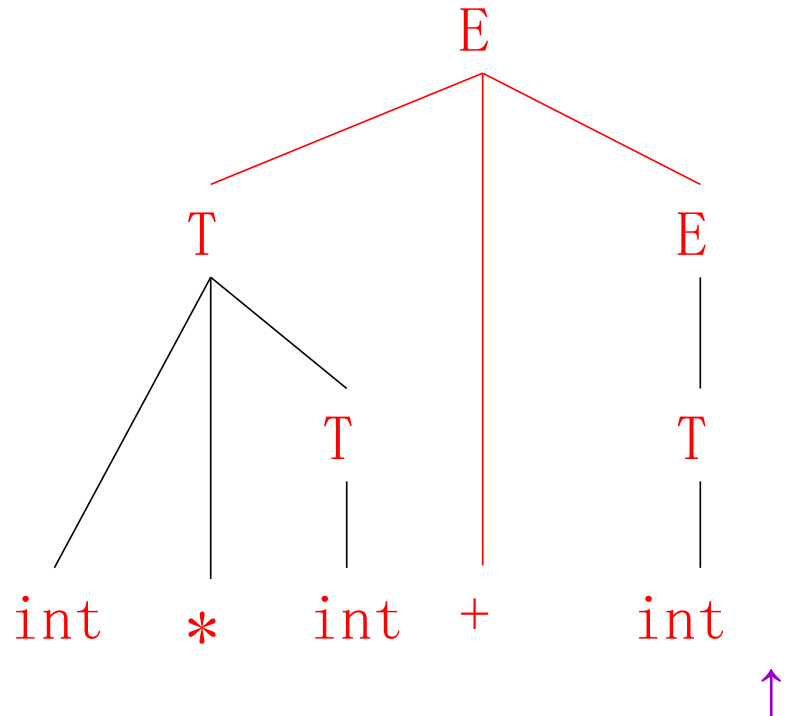
T + | int

T + int |

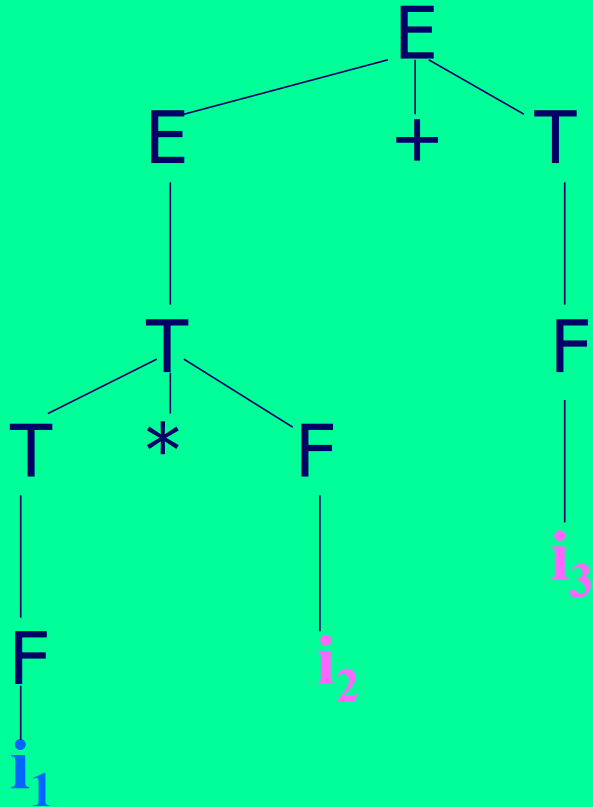
T + T |

T + E |

E |



Example :  $i*i+i$



$G[E]: E \rightarrow E+T \mid T$

$T \rightarrow T*F \mid F$

$F \rightarrow (E) \mid i$

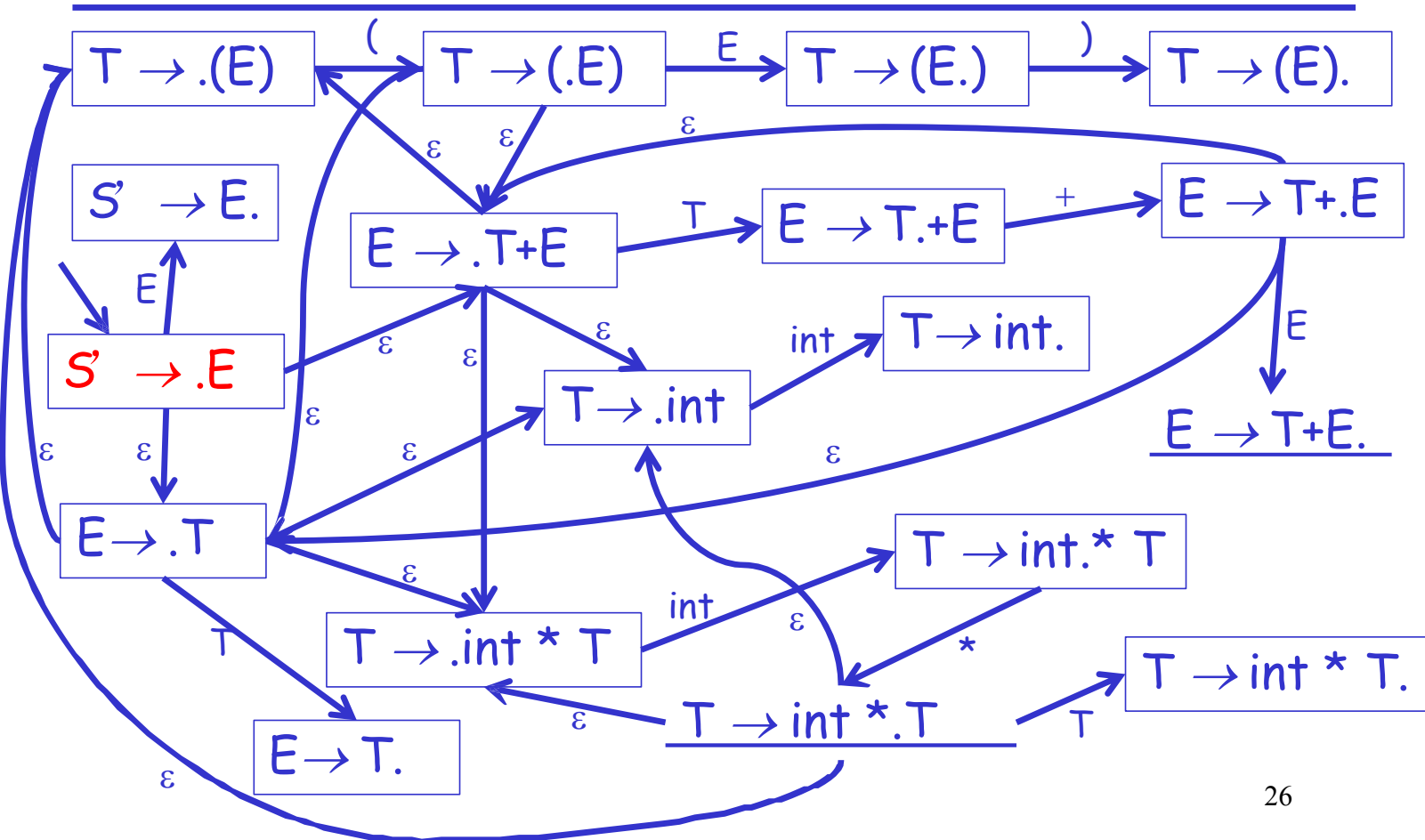
Pattern:  $i*i+i$

Phrase:  $i_1*i_2+i_3$ ,  $i_1*i_2$ ,  $i_1$ ,  $i_2$ ,  $i_3$

Immediate phrase:  $i_1$ ,  $i_2$ ,  $i_3$

Handle:  $i_1$

# NFA for Viable Prefixes

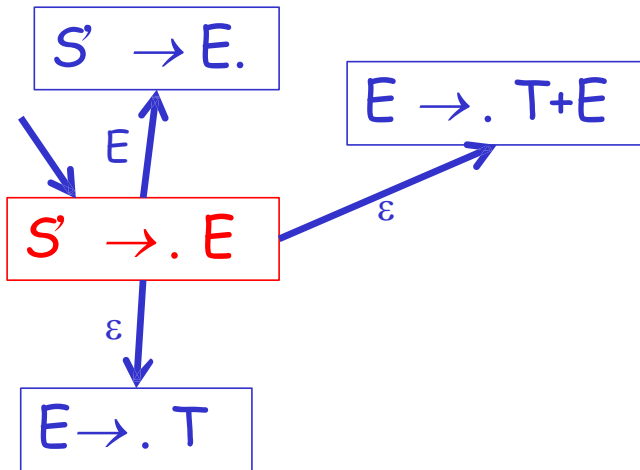
$$\begin{aligned} S' &\rightarrow E \\ E &\rightarrow T + E \mid T \\ T &\rightarrow \text{int} * T \mid \text{int} \mid (E) \end{aligned}$$


$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

# NFA for Viable Prefixes

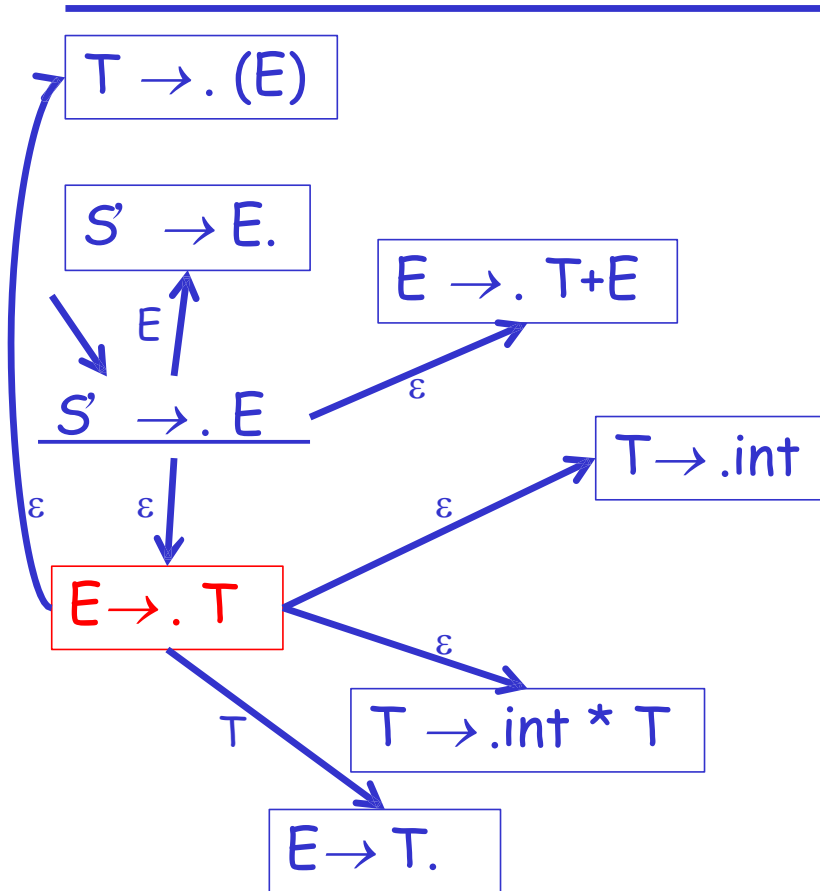
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$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

## NFA for Viable Prefixes

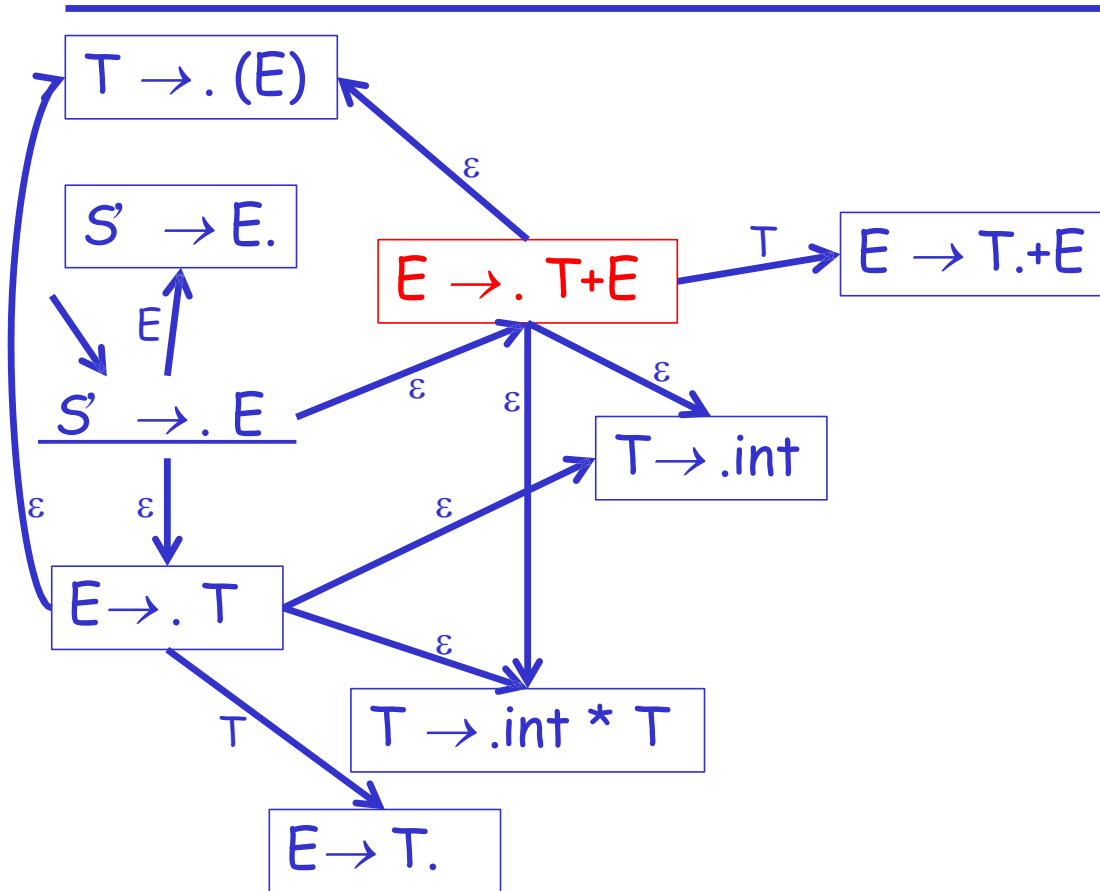




$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

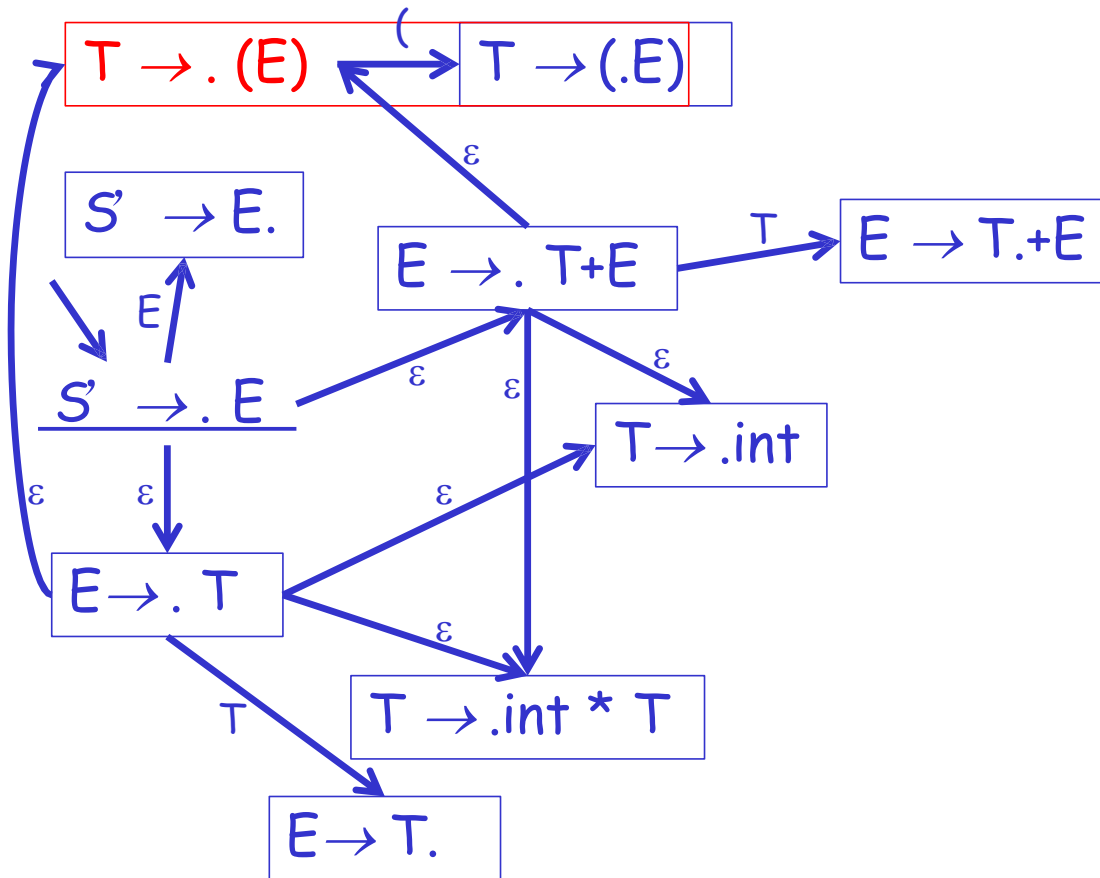
## NFA for Viable Prefixes



$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

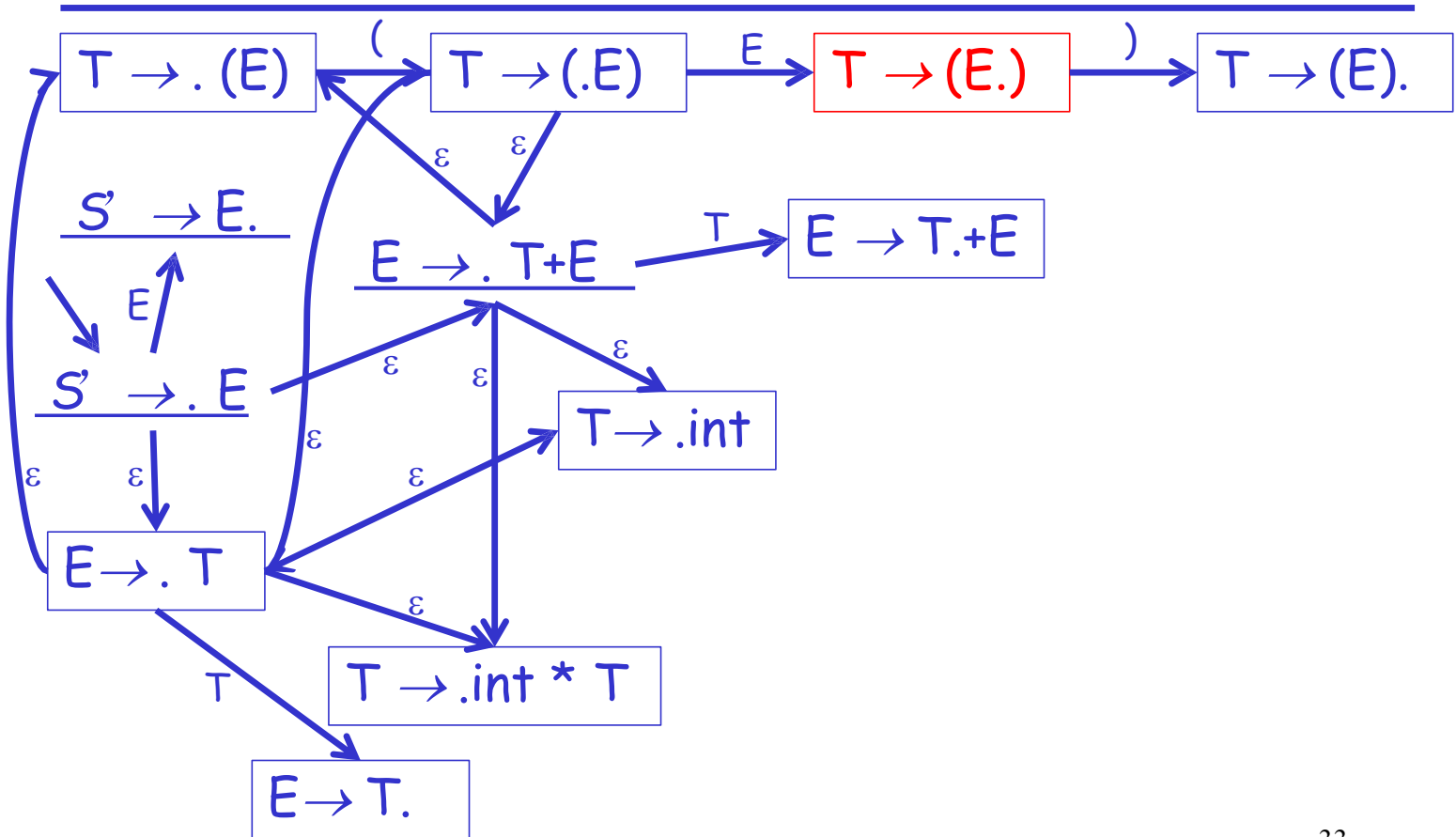
# NFA for Viable Prefixes



$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

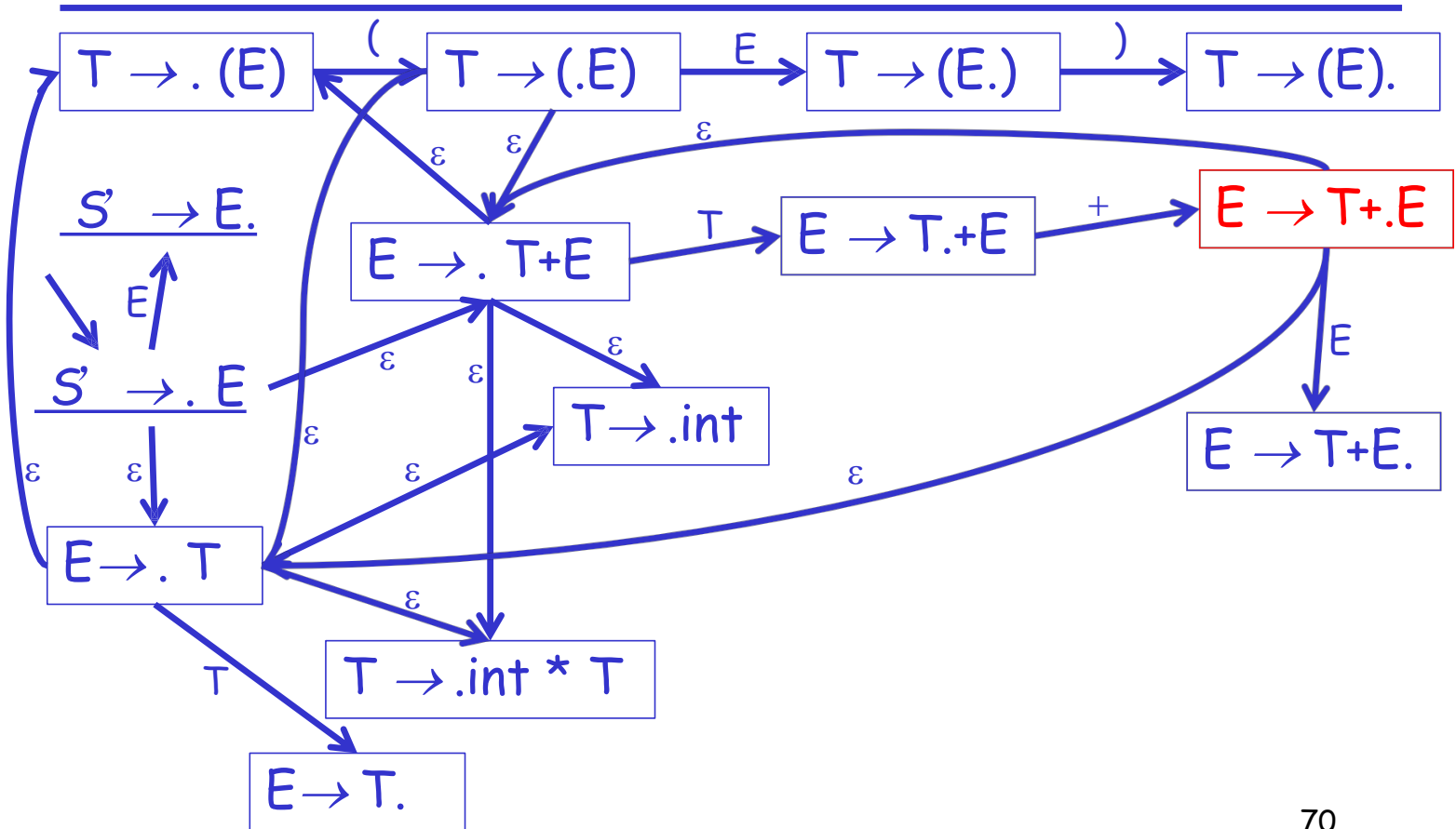
## NFA for Viable Prefixes



$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

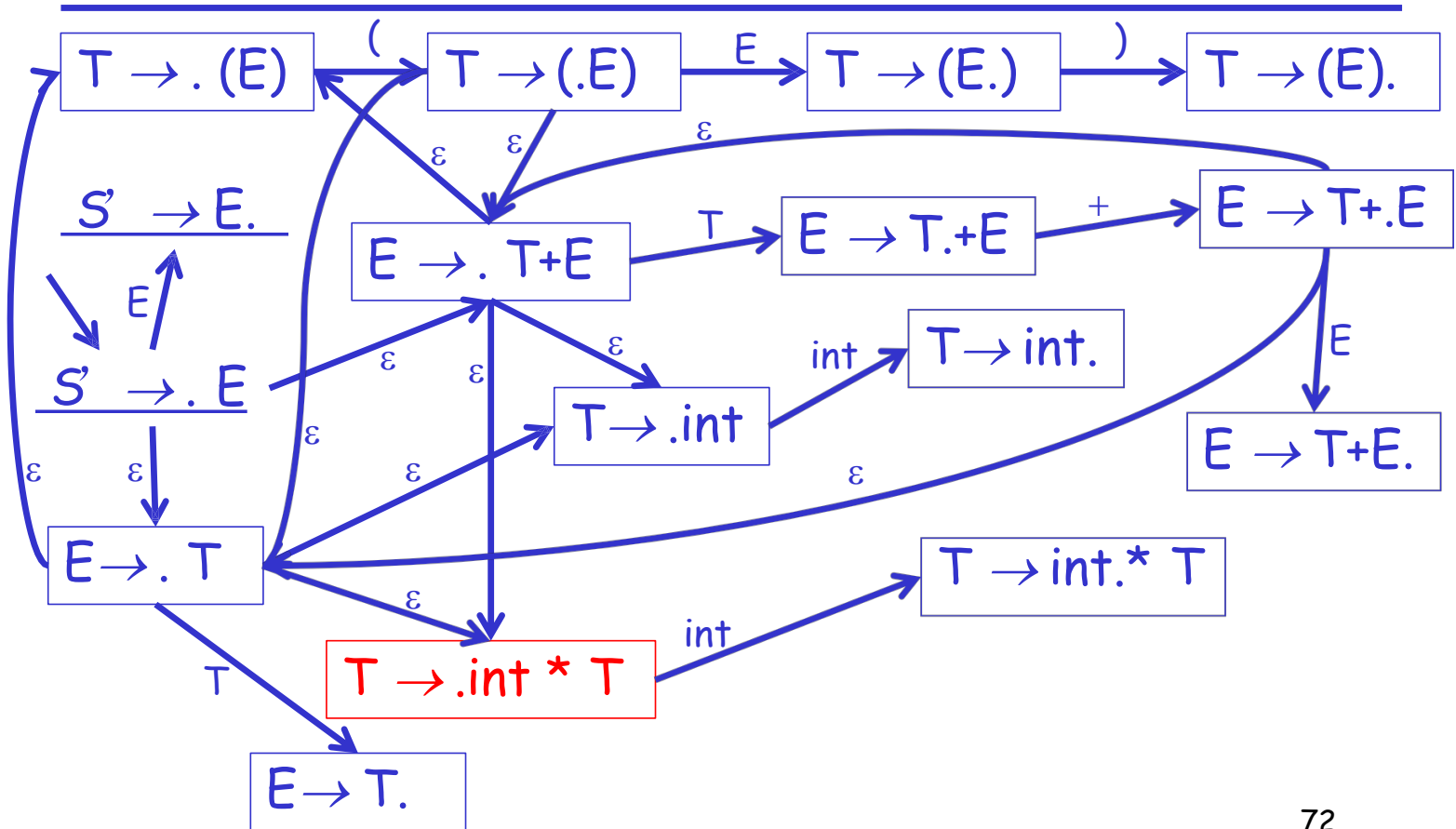
## NFA for Viable Prefixes



$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

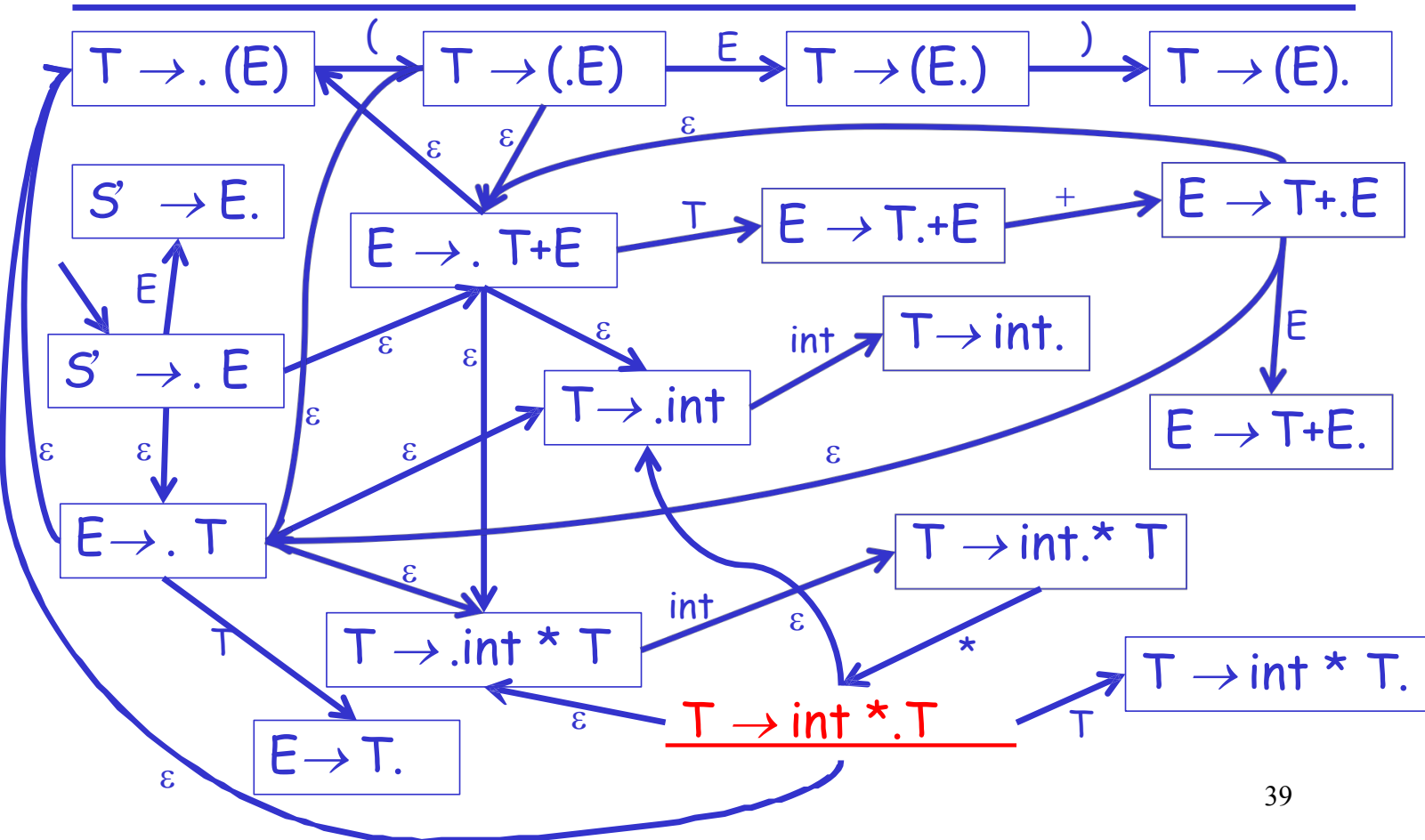
## NFA for Viable Prefixes



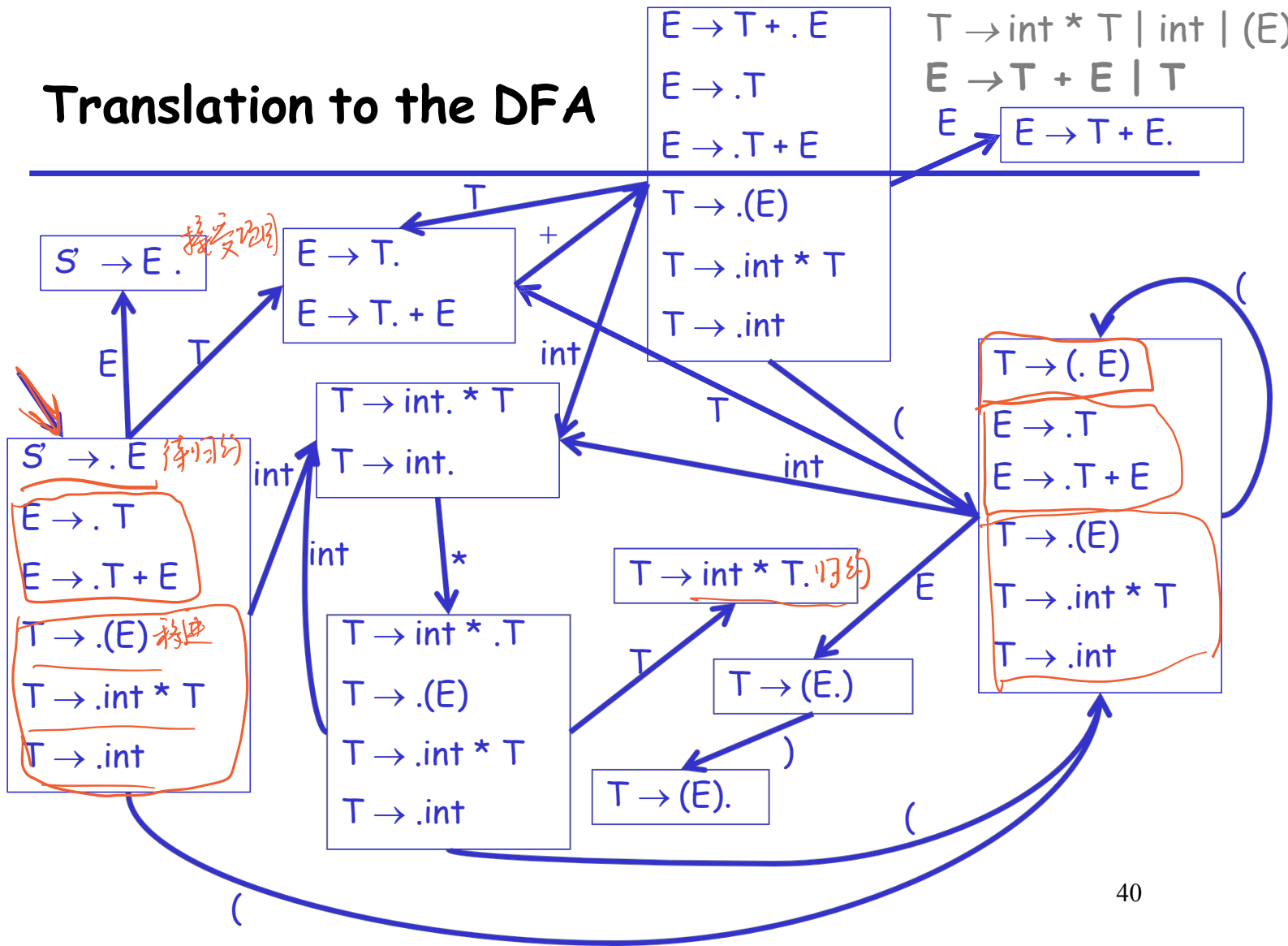
$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

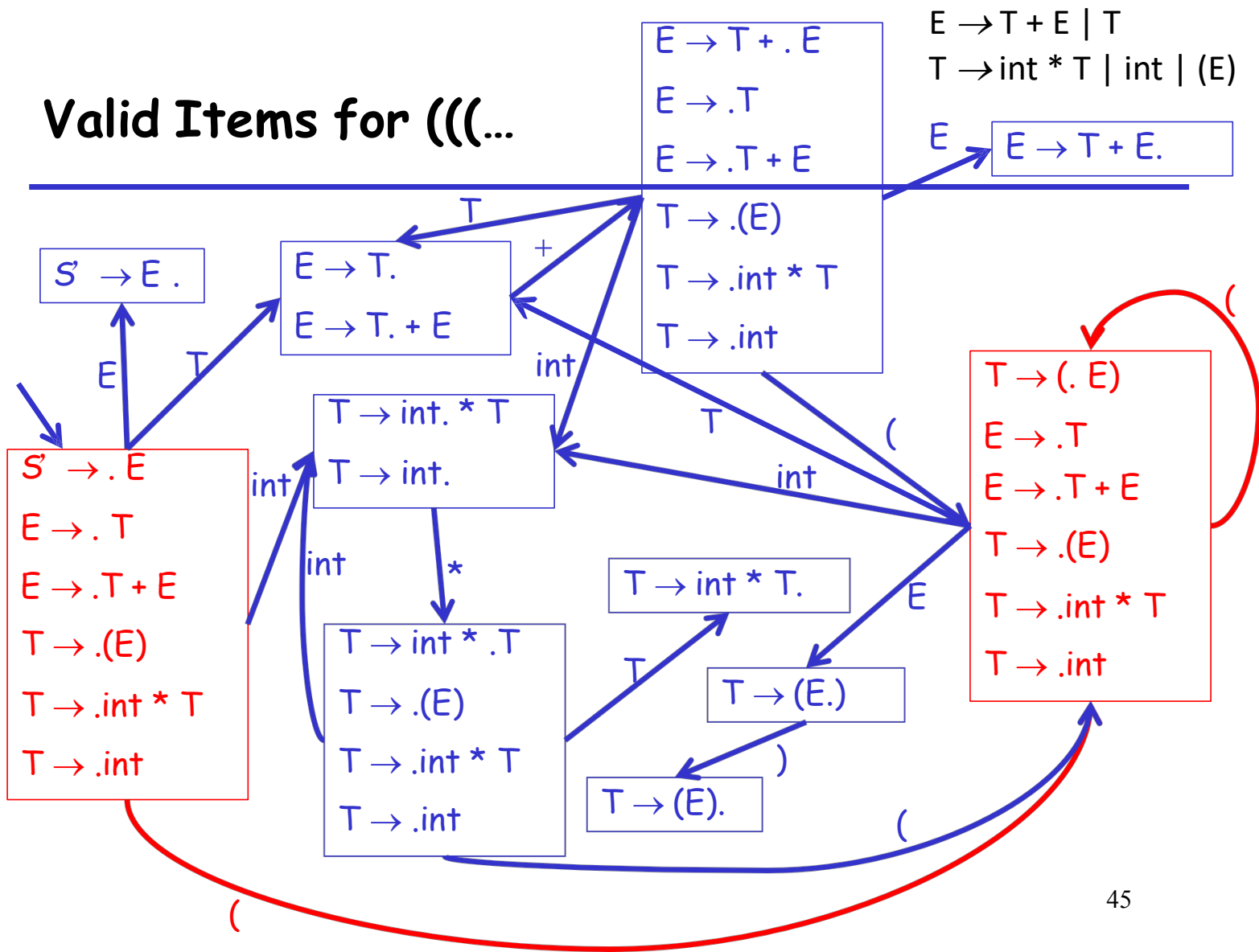
# NFA for Viable Prefixes



## Translation to the DFA



# Valid Items for (((...





# Example

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**G[S]:**

**$S \rightarrow a A c B e$**

**$A \rightarrow b$**

**$A \rightarrow Ab$**

**$B \rightarrow d$**

$S' \rightarrow S$

$S \rightarrow \mathbf{a} A \mathbf{c} B \mathbf{e}$

$A \rightarrow \mathbf{b}$

$A \rightarrow A \mathbf{b}$

$B \rightarrow \mathbf{d}$

$I_1: S' \rightarrow S \cdot$

$I_0: S' \rightarrow \cdot S$

$S \rightarrow \cdot \mathbf{a} A \mathbf{c} B \mathbf{e}$

$I_2: S \rightarrow \mathbf{a} \cdot A \mathbf{c} B \mathbf{e}$

$A \rightarrow \cdot \mathbf{b}$

$A \rightarrow \cdot A \mathbf{b}$

$I_4: A \rightarrow \mathbf{b} \cdot$

$I_6: A \rightarrow A \mathbf{b} \cdot$

$I_3: S \rightarrow \mathbf{a} A \cdot \mathbf{c} B \mathbf{e}$

$A \rightarrow A \cdot \mathbf{b}$

$I_5: S \rightarrow \mathbf{a} A \mathbf{c} \cdot B \mathbf{e}$

$B \rightarrow \cdot \mathbf{d}$

$I_8: B \rightarrow \mathbf{d} \cdot$

$I_7: S \rightarrow \mathbf{a} A \mathbf{c} B \cdot \mathbf{e}$

$I_9: S \rightarrow \mathbf{a} A \mathbf{c} B \mathbf{e} \cdot$

# LR(0) Parsing Table

[illegible]