

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

## Lecture: 04

### Queuing System

Problem: A banking queuing system in a cash counter have several data is given below:

Customer	1	2	3	4	5	6
Inter arrival time	-	2	4	1	2	6
Service Time	2	1	3	2	1	4

Calculate the Average waiting time, Utilization and Service time of this system. Also calculate the chronological ordering of events with graph.

Solution:

Customer	Inter arrival time	Arrival Time	Service Time	Time Service Begin	Waiting Time	Time Service End	Idle Time
1	-	0	2	0	0	2	0
2	2	2	1	2	0	3	0
3	4	6	3	6	0	9	3
4	1	7	2	9	2	11	0
5	2	9	1	11	2	12	0
6	6	15	4	15	0	19	3
<b>Total</b>			<b>15</b>		<b>4</b>	<b>19</b>	<b>6</b>

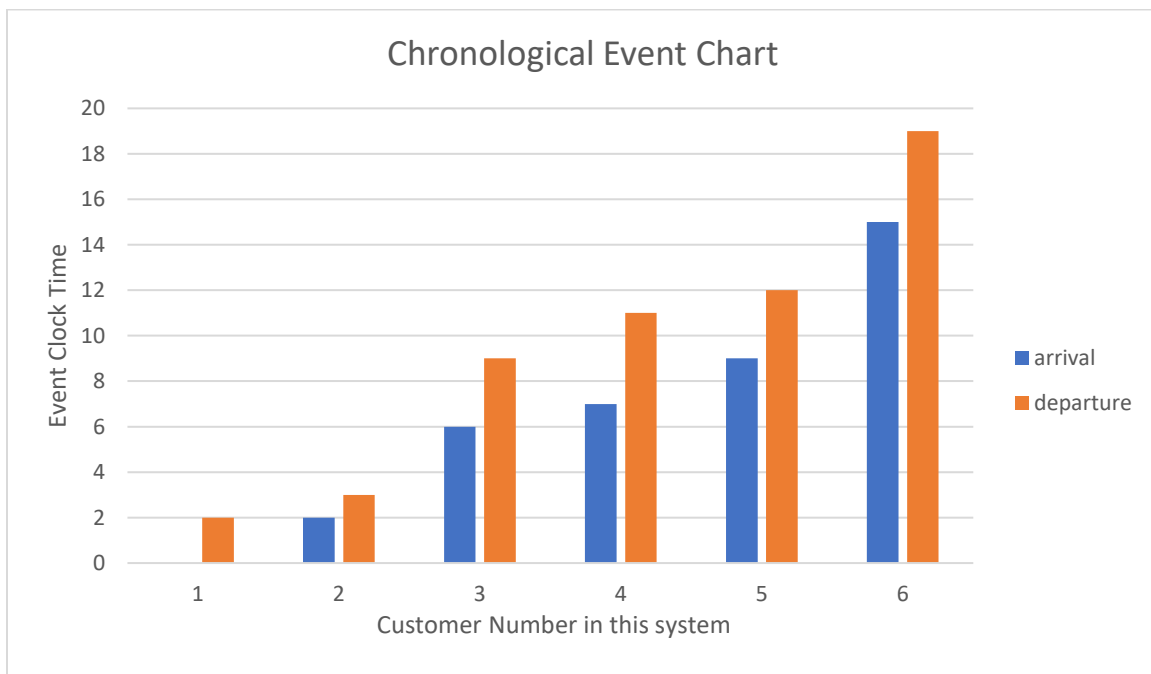
Average Waiting Time:  $4/6 = 0.67$

Utilization:  $\frac{\text{end time} - \text{idle time}}{\text{end time}} \times 100 = \frac{19-6}{19} \times 100 = 68.42\%$

Total Service Time: **15**

### Chronological Ordering of events:

Event type	Customer Number	Event Clock
Arrival	1	0
Departure	1	2
Arrival	2	2
Departure	2	3
Arrival	3	6
Arrival	4	7
Departure	3	9
Arrival	5	9
Departure	4	11
Departure	5	12
Arrival	6	15
Departure	6	19



## Random Number Generator

### LCM (Linear Congruential Method)

$$X_{i+1} = (a \cdot X_i + C) \bmod m$$

$$R_i = \frac{X_i}{m}$$

$X_0$  = Seed element

a= multiplier

C= increment

m= Module

if C=0 => multiplicative LCM

C ≠ 0 => mixed LCM

**Problem 1:** Using LCM generate a sequence of random number with  $X_0 = 3$ , a= 5 C=1 and m= 8

**Solution:**

$$X_0 = 3 ; R_0 = \frac{3}{8} = 0.37$$

$$X_{0+1} = (5 * 3 + 1) \bmod 8 = 0 ; R_1 = \frac{0}{8} = 0$$

$$X_2 = (5 * 0 + 1) \bmod 8 = 1 ; R_2 = \frac{1}{8} = 0.125$$

$$X_3 = (5 * 1 + 1) \bmod 8 = 6 ; R_3 = \frac{6}{8} = 0.75$$

$$X_4 = (5 * 6 + 1) \bmod 8 = 7 ; R_4 = \frac{7}{8} = 0.875$$

$$X_5 = (5 * 7 + 1) \bmod 8 = 4 ; R_5 = \frac{4}{8} = 0.5$$

$$X_6 = (5 * 4 + 1) \bmod 8 = 5 ; R_6 = \frac{5}{8} = 0.625$$

$$X_7 = (5 * 5 + 1) \bmod 8 = 2 ; R_7 = \frac{2}{8} = 0.25$$

$$X_8 = (5 * 2 + 1) \bmod 8 = 3 ; R_8 = \frac{3}{8} = 0.37$$

**Sequence: 3, 0,1,6,7,4,5, 2,3**

**Random Number: 0.37, 0, 0.125, 0.75, 0.875, 0.5, 0.625, 0.25**

**Problem 2 (try yourself):** Using LCM generate a sequence of random number with  $X_0 = 27$ ,  $a = 17$ ,  $C = 43$  and  $m = 100$

**Solution:**