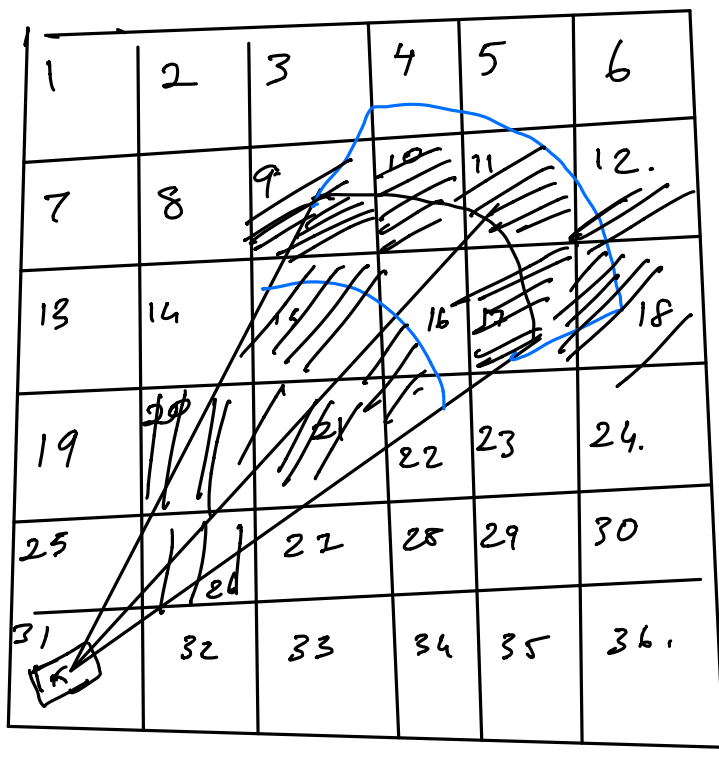


Occupancy Mapping:



Compute the occupancy probability of all cells within the cone. Let each cell be denoted.

as $C_i \ i = \{1, \dots, 36\}$.

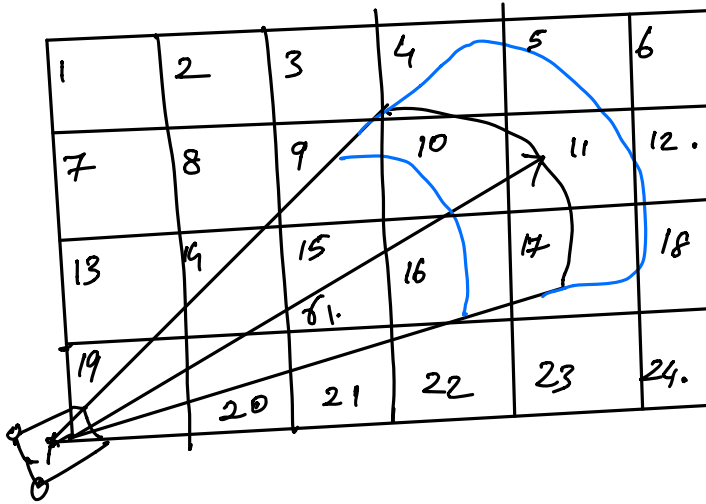
$$P(C_i / r_i) \rightarrow (1)$$

The probability that the cell C_i is occupied given the measurement r_i .

$$P(\bar{C}_i / r_i) \rightarrow (2)$$

The probability that the cell C_i is

unoccupied given the measurement z .



From the sensor model $f(r, \alpha)$ which gives high occupancy values to cells 4, 5, 10, 11, 16 and 17 and high non-occupancy values to cells 9, 14, 15, 19, 20, 21. we compute the probability values for the cells.

$$P(C_4 | r_1) = 0.8 \quad P(\bar{C}_4 | r_1) = 0.2.$$

[These probabilities come from a sensor model or measurement model].

Normalize the probabilities so that

$$P(C_4 | r_1) = \frac{0.8}{0.8 + 0.4} = \frac{2}{3} \rightarrow (2)$$

$$P(\bar{C}_4 | r_1) = \frac{0.4}{0.4 + 0.8} = \frac{1}{3} \rightarrow (3)$$

In the same vein compute

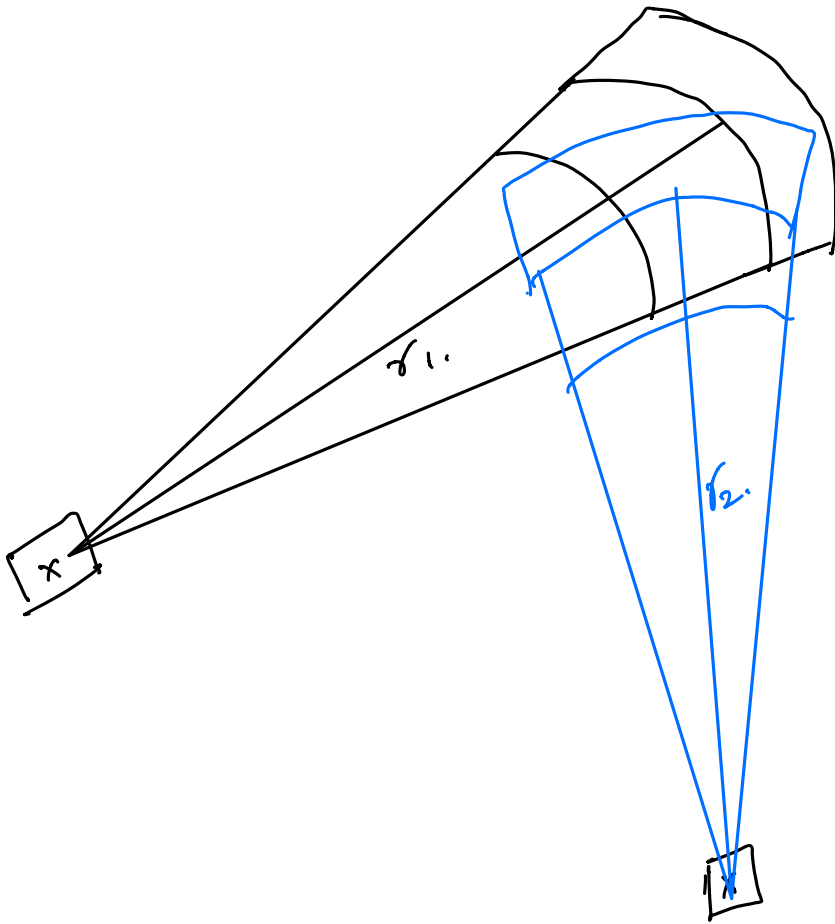
$$P(C_5 | r_1), P(\bar{C}_5 | r_1) \dots P(C_7 | r_1), P(\bar{C}_7 | r_1).$$

$$P(C_{15} | r_1) = 0.3, P(\bar{C}_{15} | r_1) = 0.9$$

$$P(C_{15} | r_1) = \frac{0.3}{0.3 + 0.9} = 0.25 \rightarrow (4)$$

$$P(\bar{C}_{15} | r_1) = \frac{0.9}{0.9 + 0.3} = 0.75 \rightarrow (5)$$

In the same vein compute for all those cells where the unoccupied probability is high i.e. $P(C_{14} | r_1)$, $P(\bar{C}_{14} | r_1) \dots P(C_{21} | r_1), P(\bar{C}_{21} | r_1)$



How to fuse the probabilities of the cells that have more than one measurement touching them.

$$P(C_i | r_2, r_1) = P(r_2 | C_i, r_1) \cdot \underbrace{P(C_i | r_1) / P(r_2 | r_1)}_{\rightarrow (6)}$$

$$[P(A/B, c) = P(B/A, c) \cdot P(A/c) / P(B/c)]$$

$$= P(r_2 | C_i) \cdot P(C_i | r_1) / P(r_2 | r_1) \rightarrow (7)$$

(Markov Assumptions)

$$= \frac{P(C_i/r_2) \cdot P(C_i/r_1) \cdot P(r_2)}{P(r_2/r_1) P(C_i)} \rightarrow (8)$$

$$= \frac{1}{k} P(C_i/r_2) \cdot P(C_i/r_1) \rightarrow (9)$$

In the same vein

$$P(\bar{C}_i/r_2, r_1) = \frac{1}{k} P(\bar{C}_i/r_2) P(\bar{C}_i/r_1) \rightarrow (10)$$

The constants get taken care of in the prior normalization.

[Note that $k = \bar{k}$].

$$\text{Hence } P(C_i/r_2, r_1) = \frac{(9)}{(9) + (10)} \rightarrow (11)$$

$$P(\bar{C}_i/r_2, r_1) = \frac{(10)}{(9) + (10)} \rightarrow (12)$$