Problem 1

$$\alpha_1(t) = 3\cos(10t+1)$$
 $\alpha_2(t) = 3\sin(4t-1)$

$$T_1 = \frac{2\pi}{10} = \frac{\pi}{5}$$

Fundamental period To

$$T_{o} = LCM\left(\frac{\pi}{5}, \frac{\pi}{2}\right) = \frac{LCM(\pi, \pi)}{HCP(5,2)} = \frac{\pi}{2}$$

Period of 1 is undefined

$$\alpha_2(t) = i \frac{12\pi \sqrt{5}}{2}$$

$$T_2 = 2K \times \frac{5}{2K} = 25$$

Fundamental period To

Problem 2

$$\chi \left(+ + T_0 \right) = \chi \left(+ + \frac{\pi}{2} \right) = 2 \cos \left(4 \left(+ + \frac{\pi}{2} \right) + \frac{\pi}{3} \right)$$

=
$$2 \cos \left(4t + 2T + \frac{7}{3}\right)$$

= $2 \cos \left(4t + \frac{7}{3}\right) = \chi(t)$

: This signal is periodic

Fundamental period = T/2 //.

b)
$$\alpha(t) \cdot \left[\sin(2t - \frac{\pi}{4})\right]^2 = 1 - \sin^2(2t - \frac{\pi}{4})$$

$$= \frac{1}{2} - \frac{1}{2}\sin(4t - \frac{\pi}{2})$$
Assume $\alpha(t)$ is periodic
then fundamental period $T_0 = \frac{2\pi}{4} = \frac{\pi}{2}$

$$\alpha(t + T_0) \cdot \alpha(t + \frac{\pi}{2}) = \frac{1}{2} - \frac{1}{2}\sin(4t + \frac{\pi}{2}) - \frac{\pi}{2}$$

$$= \frac{1}{2} - \frac{1}{2}\sin(4t + \frac{\pi}{2}) - \frac{\pi}{2}$$

$$= \frac{1}{2} - \frac{1}{2}\sin(4t - \frac{\pi}{2})$$

· X(t) is periodic

Period 2 T/2

 $x[n] = \sin\left(\frac{6\pi}{7}n + 1\right)$ For z[n] to be periodic x[n] = x[n+N] $\operatorname{Sin}\left(\frac{6\pi}{7}n+1\right) = \operatorname{Sin}\left(\frac{6\pi}{7}(n+N)+1\right)$ $\frac{6\pi n}{7} + 1 + 2\pi k = 6\pi (n+N) + 1 \qquad k \in \mathbb{Z}$ K 23 N N 2 7 K · x[n] is periodic with N= 3

 $\frac{2\sin\left(\frac{6\pi}{7}+1\right)}{2} = \chi\left(\frac{n}{7}\right)$ $\frac{2\sin\left(\frac{6\pi}{7}+1\right)}{3} = \chi\left(\frac{n}{7}\right)$ $\frac{2\sin\left(\frac{6\pi}{7}+1\right)}{2} = \chi\left(\frac{n+7}{7}\right)$ $\frac{2\sin\left(\frac{6\pi}{7}+6\pi+1\right)}{7} = \sin\left(\frac{6\pi}{7}+1\right) = \chi\left(\frac{n}{7}\right)$ $\frac{2\sin\left(\frac{6\pi}{7}+6\pi+1\right)}{7} = \sin\left(\frac{6\pi}{7}+1\right) = \chi\left(\frac{n}{7}\right)$ $\frac{2\cos\left(\frac{\pi}{7}+2\right)}{2\cos\left(\frac{\pi}{7}+2\right)}$

[2] [2] [2] [2] [2] [3] [3] [3] [3] [3]For DT tunction x(n), we need to find a finite, non-zero integer Nst x(m) = n(n+N) of all n The smallest integer N for which this holds is the fundamental period, .. We need. $\cos\left(\frac{\pi}{8}n^2\right) = \cos\left(\frac{\pi}{8}(n+N)^2\right)$ $\frac{\pi n^2 + 2\pi k^2 \pi \left(n^2 + 2nN + N^2\right)}{8}$ KEE 2K 2 1 (2DN+N2) N2 + 20N 2 16K for any value or when N28

$$64 + 16n = 16k$$
 $16(n+4) = 16k$
 2

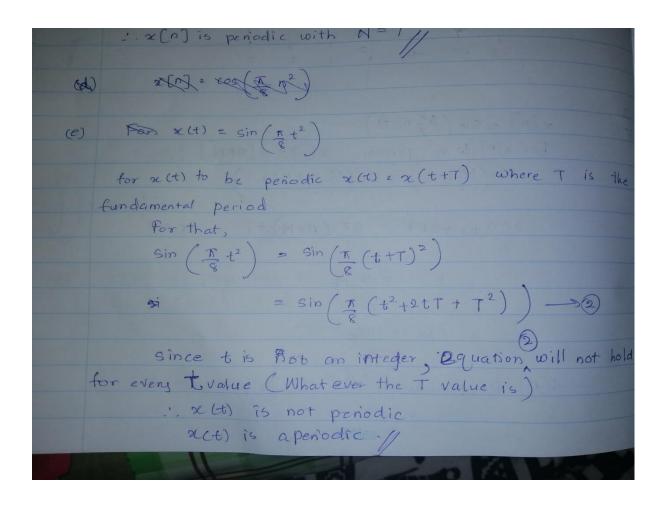
$$\cos\left(\frac{\pi}{8}(n^{\frac{2}{8}}8)^{2}\right) = \cos\left(\frac{\pi}{8}(n^{2} + 16n + 64)\right)$$

$$= \cos\left(\frac{\pi}{8}n^{2} + 2\pi n + 8\pi\right)$$

Since nez

$$\cos\left(\frac{\pi}{8}n^2 + 2\pi n + 8\pi\right) = \alpha[n]$$

.. a[n] is periodic with a period N=8/



(f)
$$\times [n] : \cos(\frac{\pi}{2}n) \cos(\frac{\pi}{4}n)$$

$$= \frac{1}{2} \left\{ \cos(\frac{\pi}{2} + \frac{\pi}{4})n + \cos(\frac{\pi}{2} - \frac{\pi}{4})n \right\}$$

$$\alpha[n] : \frac{1}{2} \left\{ \cos \frac{3\pi}{4}n + \cos \frac{\pi}{4}n \right\}$$

Assume &(n) is periodic

Then
$$\chi_{1}(t) = \cos \frac{3\pi}{4} n$$
 $\chi_{2}(t) = \cos \frac{\pi}{4} n$
 $\chi_{2}(t) = \cos$

Then fundamental period would be

So if N=8

If
$$\alpha(n)$$
 is periodic $\alpha(n) = \alpha(n+N)$

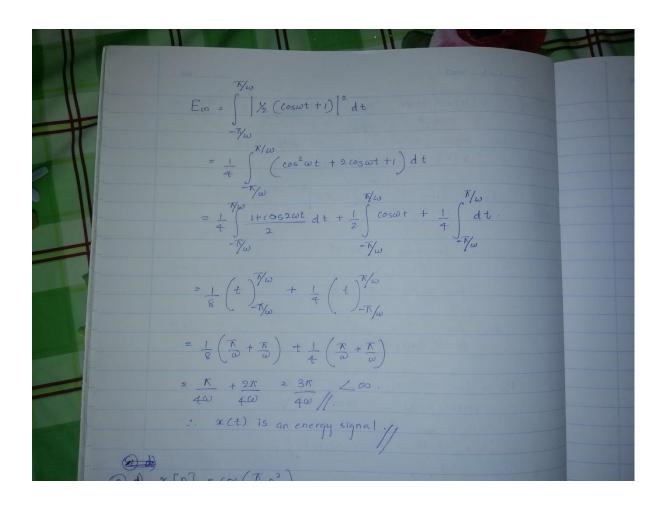
$$\alpha(n+8) = \cos\left(\frac{\pi}{2}(n+8)\right)\cos\left(\frac{\pi}{4}(n+8)\right)$$

$$= \cos\left(\frac{\pi}{2}n+4\pi\right)\cos\left(\frac{\pi}{4}n+2\pi\right)$$

$$= \cos\left(\frac{\pi}{2}n+4\pi\right)\cos\left(\frac{\pi}{4}n\right)$$

$$= \alpha(n)$$

 $3(a) \quad \chi[n] = \begin{cases} \cos \pi n & n \geq 0 \\ 0 & o \neq \omega \end{cases}$ When n>0, x [n] is periodic with n=2 : 2[n] is a power signal. $P_{\infty} = \lim_{N \to \infty} \frac{1}{2N+1} \sum_{n=0}^{N} |\cos \pi n|^{2}$ Since for every no nezt Then cosAn = coso' = 1 Pao 2 lim 1 12 N-300 2N+1 $P_{\infty} = \lim_{N \to \infty} \frac{N - 0 + 1}{2} = \lim_{N \to \infty} \frac{1 + 1}{2} = \frac{1}{2}$: x[n] is a power signal /. $\alpha(t) = \sqrt{2} \left(\cos \omega t + 1 \right) - \sqrt{2} \omega \angle t \angle \sqrt{2} \omega$ $0 \qquad 0 / \omega$ (b) Fundamental period of 1/2 (cosot +1) · - K < t L K there is only I period. $\frac{1}{2}\left(\cos\omega t + 1\right) \text{ is not periodic within } -\frac{\pi}{\omega} \angle t \angle \sqrt{y_{\omega}}.$.. se (t) is an energy signal.



Problem 5

(a)
$$x(t) = \cos 4\pi t$$

$$a_{K} = 2 \int \cos 4\pi t e^{-j4\pi t} k dt$$

$$K=0$$
 $A_0 = 2 \int \cos 4\pi t \, dt = 20$
 Y_2

(b)
$$y(t) = \sin(4\pi t)$$
 $\omega_0 = 4\pi$
 $\alpha_K = 2 \int \sin(4\pi t) e^{-jKA\pi t} dt$

$$a_{1} = \frac{1}{2j}$$
 $a_{-1} = -\frac{1}{2j}$
 $a_{0} = 0$

(c)
$$Z(t) = x(t) y(t)$$

$$z(t) y(t) \cdot \left(\frac{1}{2}e^{j4\pi t} + \frac{1}{2}e^{-j4\pi t}\right) \left(\frac{1}{2j}e^{-j4\pi t}\right)$$

$$= \frac{1}{4j}e^{j4\pi t} + \frac{1}{4j} - \frac{1}{4j}e^{-j8\pi t}$$

$$= \frac{1}{4j}e^{j2\pi t} - \frac{1}{4j}e^{-j8\pi t}$$

$$= \frac{1}{4j}e^{j2\pi t} - \frac{1}{4j}e^{-j8\pi t}$$

$$C(1) = \frac{1}{4j} \qquad Q_{-1} = \frac{1}{4j}$$

$$Q_{0} = Q_{0}$$

Fundamental period of Z(t) # 15

Fundamental frequency co. 28th

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Sing
$$\pi$$
 t = $\frac{1}{2j}$ e $\frac{1}{4j}$ e $\frac{1$

$$a_{\uparrow} = \frac{1}{4j}$$
 $a_{-1} = \frac{-1}{4j}$ $a_{0} = 0$

(a)
$$x(t) = \begin{cases} 1 & |t| < 1 \\ 0 & 1 < |t| < 2 \end{cases} \quad \text{Period } \cdot 4$$

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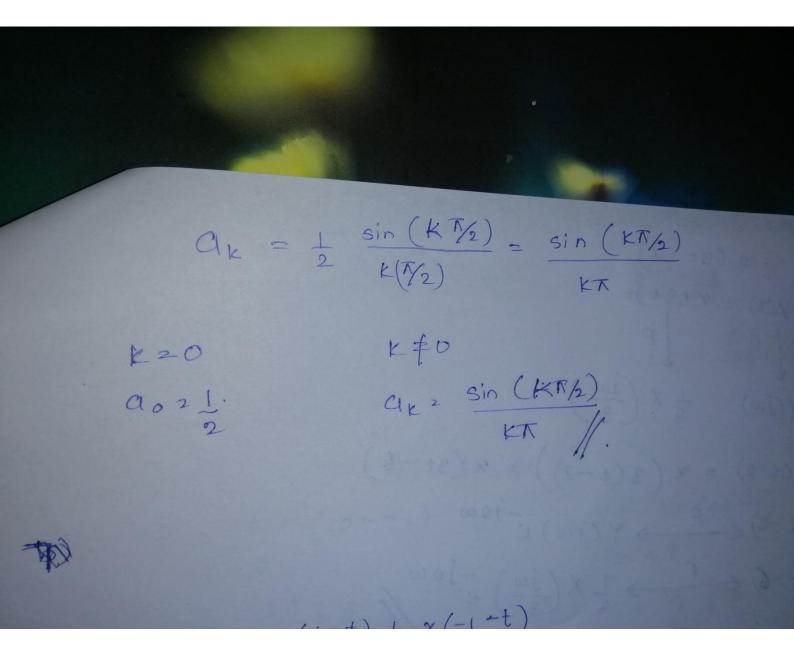
$$x(t) = \begin{cases} 1 & |t| < 2 \end{cases} \quad \text{Period } \cdot 4$$

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$$x(t)$$

Kwo 2 mT

 $K_2 \frac{m\pi}{\omega} = m\pi \times \frac{2}{\pi} = 2m$ $K_2 2m$

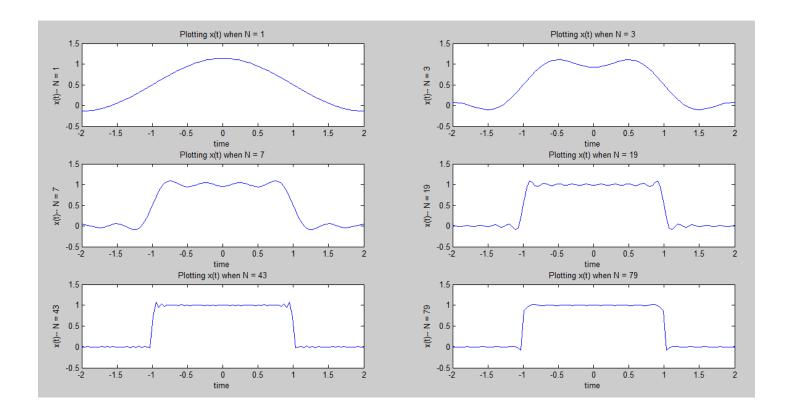


Problem 6

```
b) t=linspace(-2,2);
    N = [1,3,7,19,43,79];
    asex6(t,N);

function y = asex6(t,N)
    x = 1;
    for g = 1:length(N)
        for n = 1:length(t)
        k = -1*N(g);
        y(n) = 0;
    while k <= N(g)
        if k == 0
        a = 0.5;
    else</pre>
```

```
a = \sin(k*pi*0.5)/(k*pi);
                end
                y(n) = y(n) + a*exp(1i*pi*0.5*k*t(n));
                k = k + 1;
            end
        end
        plotting the x(t)
        subplot(3,2,x);
        plot(t,real(y));
        xlabel('time');
        ystr = sprintf('x(t)-- N = %d',N(g));
        ylabel(ystr);
        titstr = sprintf('Plotting x(t) when N = %d', N(g));
        title(titstr);
        %calculate percentage overshoot
        povershoot = real((max(y)-1)*100);
        fprintf('percentage overshoot when N is %d =
      %.2f%%\n',N(g),povershoot);
        x = x+1;
    end
end
```



c) percentage overshoot when N is 1 = 13.63% percentage overshoot when N is 3 = 10.02% percentage overshoot when N is 7 = 9.21% percentage overshoot when N is 19 = 8.55% percentage overshoot when N is 43 = 8.39% percentage overshoot when N is 79 = 1.43%

(7) a)
$$x_{i}(t) = x(i-t) + x(-i-t)$$

$$x(-t) \leftarrow \begin{array}{c} p & x(-j\omega) \text{ (time reversal)} \\ y(t), & x(-j\omega) \\ y(t), & x(-j\omega) \\ y(t-i) & = x(-(t-i)) = x(-t+i) \\ y(j\omega) = \begin{array}{c} p & x(-i\omega) \\ p & y(t+i) \\ p & y(t+i) \end{array}$$

$$x(-t+i) \leftarrow \begin{array}{c} p & x(-j\omega) \\ p & y(t+i) \\ p & y(t+i) \end{array}$$

$$x(-t+i) \leftarrow \begin{array}{c} p & x(-j\omega) \\ p & y(t+i) \end{array}$$

$$x(-t-i) \leftarrow \begin{array}{c} p & x(-j\omega) \\ p & y(t+i) \end{array}$$

$$x(-t-i) \leftarrow \begin{array}{c} p & y(-t+i) \\ p & y(-j\omega) \end{array}$$

$$x(-t-i) \leftarrow \begin{array}{c} p & y(-j\omega) \\ p & y(-j\omega) \end{array}$$

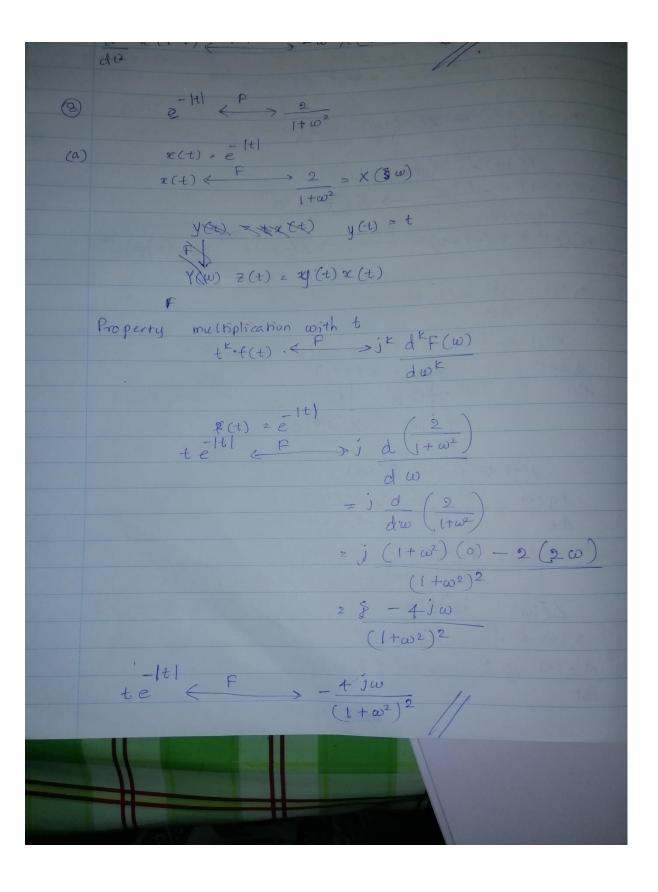
$$x(-t-i) \leftarrow \begin{array}{c} p & y(-j\omega) \\ p & y(-j\omega) \end{array}$$

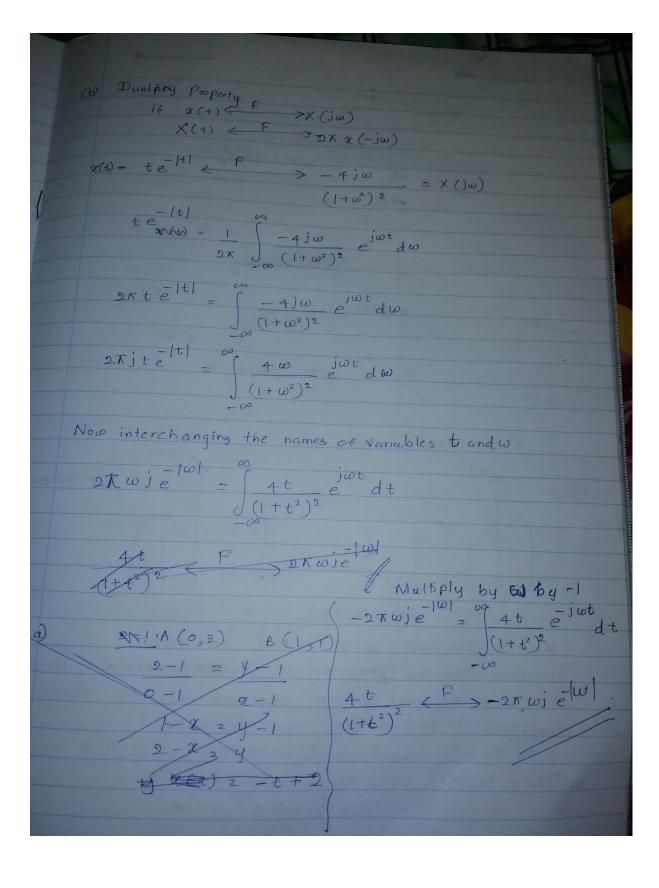
$$x(-t-i) \leftarrow \begin{array}{c} p & y(-j\omega) \\ p & y(-j\omega) \end{array}$$

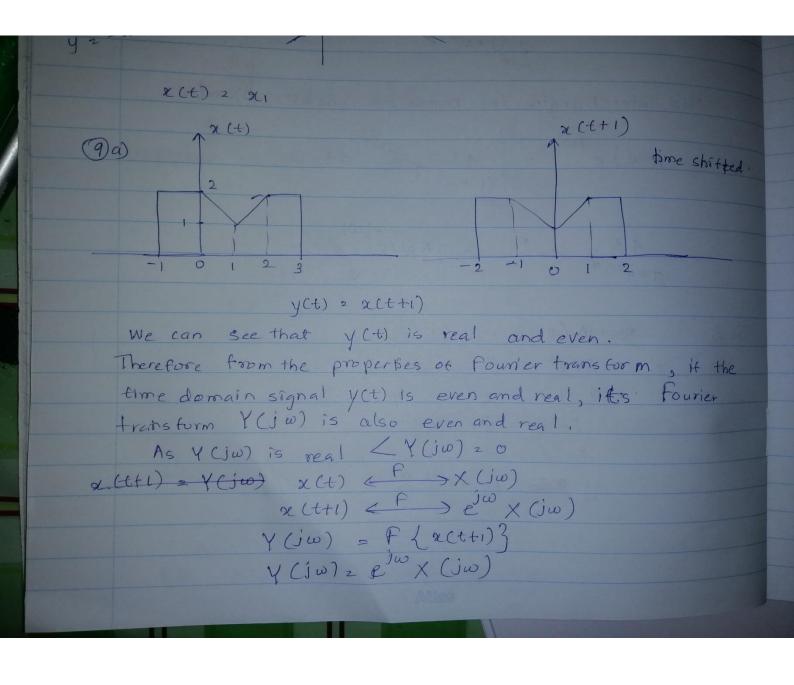
$$x(-t-i) \leftarrow \begin{array}{c} p & y(-j\omega) \\ p & y(-j\omega) \end{array}$$

$$x(-t-i) \leftarrow \begin{array}{c} p & y(-j\omega) \\ p & y(-j\omega) \end{array}$$

(b)
$$x_0(t) = 2(st-b)$$
 $y(t) = x(st)$
 $\downarrow F$
 $\uparrow F$
 $Y(j\omega) = \frac{1}{3} \times \left(\frac{j\omega}{3}\right)$
 $y(t-2) = x(s(t-2)) = x(st-6)$
 $y(t-2) = F$
 $\uparrow Y(j\omega) e^{-j\omega\omega}$
 $x_0(t) = z(st-6) = F$
 $\downarrow Y(j\omega) e^{-j\omega\omega}$
 $x_0(t) = \frac{d^2}{dt^2} \times (t-1)$
 $x(t) = \frac{d^2}{dt^2} \times (t-1)$
 $x(t) = x(t-1)$
 $x(j\omega) = x(j\omega)$
 $x(j\omega) = y(j\omega)$
 $x(j\omega) = y(j\omega)$







$$x(j\omega) = e^{j\omega} Y(j\omega)$$

$$= x(j\omega) = -i\omega + 2 Y(j\omega)$$

$$= -i\omega + 6$$

$$x(j\omega) = -i\omega + 6$$

$$x(j$$

